

## Creating a Lactation Model for 305-Day Milk Yield with Different Resampling Techniques (Bagging Mars) in Mars Modeling

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### Abstract

The main purpose of this research is to obtain a prediction model for milk yield by using Multivariate Adaptive Regression Splines (MARS) and Bagging MARS algorithms as a non-parametric regression technique. For this purpose, the effects on milk yield of 305 days were investigated by using lactation parameters in dairy cattle. In the study, 9337 lactation milk yield records belonging to 37 animals belonging to the 2022-2023 period were used and the data set was created by randomly ordering the animals. Data on milk yield results were analyzed with MARS and Bagging MARS algorithms. For dairy cattle; it was modeled with explanatory variables such as lactation month (month), service period (SP), last 7 days average milk yield (L7DMMY), animal's first birth age (FP), animal's age (Age), number of lactations (LN). Correlation coefficient ( $r$ ), coefficient of determination ( $R^2$ ), Adjusted  $R^2$ , Root of Square Mean Error (RMSE), standard deviation ratio (SD ratio), mean absolute percent error (MAPE), mean absolute for MARS algorithm estimating total average milk yield deviation (MAD) and Akaike Information Criteria (AIC) values are 0.9986, 0.997, 0.977, 0.142, 0.052, 0.2389, 0.086 and -88, respectively. Similar statistics for the Bagging MARS algorithm are 0.754, 0.556, 0.453, 1.8, 0.666, 3.96, 1.47, and 115, respectively. It has been observed that MARS and Bagging MARS algorithms provide correct results according to the goodness of fit statistics. In this study, it was revealed that MARS algorithm gave better results in milk yield modeling of 305-day lactation.

**Keywords:** Lactation, Milk yield, MARS, Dairy Cattle, Bagging.

## Süt Sığırlarında 305 Günlük Süt Verimi için Mars Modellemesinde Farklı Yeniden Örnekleme Teknikleri (Bagging Mars) ile Laktasyon Modeli Oluşturma

### Öz

Bu araştırmanın temel amacı, parametrik olmayan bir regresyon tekniği olarak Çok Değişkenli Uyarlanabilir Regresyon Splines (MARS) ve Bagging MARS algoritmalarını kullanarak süt verimi için bir tahmin modeli elde etmektir. Bu amaçla çalışmada süt sığırlarında laktasyon parametreleri kullanılarak 305 günlük süt verimi üzerine etkileri incelenmiştir. Çalışmada 37 tane hayvana ait 2022-2023 dönemine ait 9337 adet laktasyon süt verimi kaydı kullanılmış ve hayvanlar rastgele sıralanarak veri seti oluşturulmuştur. Süt verimi sonuçlarına ilişkin veriler MARS ve Bagging MARS algoritmaları ile analiz edilmiştir. Laktasyon ayı (month), Servis periyodu (SP), son 7 günlük ortalama süt verimi (L7DMMY), hayvanın ilk doğum yaşı (FP), hayvanın yaşı (Age), laktasyon sayısı (LN) gibi açıklayıcı değişkenler ile modellenmiştir. Toplam ortalama süt verimini tahmin eden MARS algoritması için korelasyon katsayısı ( $r$ ), belirleme katsayısı ( $R^2$ ), Düzeltilmiş  $R^2$ , Hata Kareler Ortalamasının Karekökü (RMSE), standart sapma oranı (SD oranı), ortalama mutlak yüzde hatası (MAPE), ortalama mutlak sapma (MAD) ve Akaike Bilgi Kriterleri (AIC) değerleri sırasıyla 0.9986, 0.997, 0.977, 0.142, 0.052, 0.2389, 0.086 ve -88'dir. Bagging MARS algoritması için benzer istatistikler sırasıyla 0.754, 0.556, 0.453, 1.8, 0.666, 3.96, 1.47 ve 115'tir. MARS ve Bagging MARS algoritmalarının uyum iyiliği istatistiklerine göre doğru sonuçlar ortaya koyduğu gözlemlenmiştir. Bu çalışmada, MARS algoritmasının 305 günlük laktasyona ait süt verimi modellemesinde daha iyi sonuçlar verdiği ortaya çıkmıştır.

**Anahtar Kelimeler:** Laktasyon, Süt verimi, MARS, Süt Sığırları, Bagging.

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## 1. Introduction

It is important to select animals with high milk yield in order to reach milk production in developed countries and to meet the milk needs of individuals in our country. The Holstein breed is very important for this purpose. Producers in Türkiye prefer farm breeds with higher meat and milk yields than local breeds, and the share of these breeds in the total cattle population is increasing every year. While 18.94% of the total number of Turkish cattle was 9.8 million in 2002, breeding, 44.45% crossbreed and 36.58% domestic cattle breeds, the total number of cattle in 2022 is approximately 17 million. The proportions of breeding cattle crossbred cattle and domestic cattle breeds in the total are 49.2%, 43.4% and 7.3%, respectively (TUIK, 2023).

Lactation period, on the other hand, is the period from starting to ending of the milking. The average lactation period of dairy cattle is 305 days. This period may vary depending on care and feeding (Özyurt and Özkan, 2009). It is imperative to take into account their reproductive performance, which affects the productivity of dairy cows and has a major impact on the profitability of dairy production establishments. To this end; In many studies, calving interval, pregnancy rate, insemination number for pregnancy, service period, first insemination and first calving age have been used to evaluate reproductive performance (Bayril and Yilmaz, 2017; Boğa and Boğa, 2022; Çanga and Boğa, 2022; Doğan, 2003; Mee, 2004; Şahin and Ulutaş, 2010). Lactation curves can be used to calculate lactation continuity, which indicates the animals' ability to maintain a constant milk yield. Various methods have been proposed for calculating lactation persistence, but there is still no standard method. In studies conducted in different years on the average milk yield of 305 days in Holstein cows in Türkiye, varying results have been reported over the years (Gürses and Bayraktar, 2012; Omar, 2022; Orhan, Çetin Teke, and Karcı, 2018; Şahin and Ulutaş, 2010; Sarar and Tapkı, 2017; Yaylak and Kumlu, 2005).

However, many researches made have been done on milk production modeling and various models have been developed to explain the relationship between control day and milk production (Bayril and Yilmaz, 2017; Eydurhan, Yilmaz, Tariq, and Kaygisiz, 2013; Orhan et al., 2018). MARS (Multivariate Adaptive Regression Spline) decomposes multivariate nonlinear models and offers the ability to be explained by linear models (Grzesiak et al., 2010), described cows inseminated using statistical and machine learning methods (classification functions, logistic regression, neural networks and MARS). It was determined that the best results were obtained with artificial neural networks (ANN) and MARS methods. MARS, which will be used in this research, decomposes multivariate nonlinear models and offers the opportunity to be explained with linear models (Çanga, 2022; Faraz et al., 2021). Faraz et al., (2021), in their study, modeled with MARS, which is a non-linear method to estimate the body weight (BW, kg) of bovine animals. It has been reported that

models with high predictive power were obtained with the sheep's body length (BL, cm) and chest circumference (CG, cm) as explanatory variables with the model they presented. In this study, MARS data mining algorithm, which performs the best estimation among statistical methods, was used. The MARS data mining algorithm, which is an embodiment of the CART (Classification and Regression Tree) algorithm, does not require any assumptions about the distribution of the variables. However, the fact that it does not require a functional hypothesis between dependent and independent variables distinguishes this algorithm from other previously used algorithms (Turhan, 2020; Iqbal et al., 2021).

Re-sampling clustering (Bagging=Bootstrap+Aggregating) is an effective method specified by various classifications and regressions to improve prediction accuracy in large data sets. Resampling clustering can be used as a tool to reduce the variance of a predictor and increase the stability and power of predictions (Çanga and Boğa, 2020; Celik and Yilmaz, 2021; Otok, Putra, Sutikno, and Yasmirullah, 2020; Şengül et al., 2022). When the literature is reviewed, many researches have been done on milk production modeling and various models have been developed to explain the relationship between control day and milk production (Alıç, 2007; Bilgiç, 1999; Çetin and Alkoyak, 2018; Doğan, 2003; Orhan and Kaygısız, 2002; Şahin and Ulutaş, 2010).

In this research, it is aimed to predict the future milk yields with the results obtained by making Bagging and MARS separately, with models with less errors. Milk yield was estimated by MARS method by using independent variables of lactation period, service period, average milk yield for the last 7 days, age at first birth, age of animal, number of lactations in dairy cattle in Holstein cows.

## **2. Materials and Methods**

The research material was created from Holstein dairy cattle raised in a cattle farm in Niğde Bor district. There are approximately 100 cattle in the collection in the enterprise, and the primary target in the enterprise is milk production, and meat production is also contributed by fattening male animals in the region. For this reason, milk production, breeding heifer breeding and fattening activities are carried out in the enterprise. A total of 9561 milk data, 37 of which were milkers, were used.

### **2.1. Animal Material**

The research material includes the 305-day milk yield of 37 Holstein dairy cattle calving between 2022 and 2023 in a cattle farm in Niğde-Bor district. Lactation month (month), service period (SP), last 7 days average milk yield (L7DMMY), age at first birth (FP), age of animal (Age), number of lactations (LN) were taken as basis in fertility records.

## 2.2. Statistical Analysis

Data on lactation results obtained from dairy cattle were analyzed with MARS and Bagging MARS algorithms. In the statistical modeling studies conducted in the last ten years, the prediction performances of decision trees, artificial neural networks and MARS algorithms have been comparatively examined. The MARS algorithm, which is a modified version of the CART algorithm, has been the focus of attention of researchers in terms of defining the high-level relationships between the variables under consideration (Akin et al., 2020; Altay et al., 2022; Çanga, 2022; Çanga and Boğa, 2022; Tirink et al., 2022).

The MARS model was developed using the R software "earth" package and "ehaGoF" (Milborrow 2011; R Core Team 2024; Milborrow 2018; Eyduvan et al., 2019; Eyduvan and Gulbe 2020; Eyduvan and Duman 2020; Tirink et al., 2023). Among the observed and predicted values of in the study, the smallest GCV, SDRATIO, RMSE, MAPE, MAD, AIC, AICc and the MARS model with the highest determination coefficient ( $R^2$ ) and Pearson coefficient ( $r$ ) were accepted as the best.

### 2.2.1. Multivariate Adaptive Regression Spline (MARS)

MARS algorithm used by Friedman (1991) to capture nonlinear relationships between predictors and response variable(s) is a powerful approach that does not require assumptions about functional relationships between dependent and input variables. The model that emerges as the weighted total basic function including the  $BF_i(x)$  function is given by Equation 1 below (Akin et al., 2020; Eyduvan et al., 2020; Çanga 2022; Çanga and Boğa 2020; Çelik et al., 2021).

$$y = \sum_{i=1}^k a_i BF_i(x) \quad (1)$$

Mars algorithm is formed by the linear breakdown of the basic function of  $BF_i(x)$  with the following equation.

$$BF_1 = \max(0, x - t) \begin{cases} x - t, x > t \\ 0, x \leq t \end{cases} \quad (2a)$$

$$BF_2 = \max(0, x - t) \begin{cases} x - t, x > t \\ 0, x \leq t \end{cases} \quad (2b)$$

Here,  $x$  is the variable range;  $t$  is the node. The linear combination of the basic functions obtained accordingly:

$$Y_i = a_0 + a_1 BF_1 + a_2 BF_2 + \dots + a_k BF_k$$

and the estimation equation is obtained. Here  $Y_i$  dependent variable,  $a_0$  intercept, and  $a_1, \dots, a_k$  are coefficients of the related basic functions (Everingham and Sexton 2011, Emamgolizadeh et al., 2015; Çanga and Boğa 2021; Çanga et al., 2021; Akin et al., 2020; Akın et al., 2021).

The fact that it does not require assumptions not only about the distribution of the variables but also about the functional relationships between the variables, as well as providing an equation that shows the high-dimensional relationships between the variables makes the MARS algorithm very popular. In the MARS method, generalized cross-validation error (GCV) is the best criterion for choosing the best model. Because GCV takes into account both errors and model complexity (Grzesiak et al., 2010).

Bagging a method first introduced by (Breiman, 1994) is used to increase the stability and power of the estimator by reducing the variance of an estimator. The Bagging MARS algorithm is based on creating the desired number of Bootstrap samples based on the original data set (Çanga and Boğa, 2020; Kulekçi et al., 2022). Many generated examples are derived from datasets. If changes in the dataset cause significant changes, bagging can increase sensitivity. So the basic idea of Bagging is to use resembling to create an estimator with multiple versions; here, after combining the objectives, the result should be better than a single predictive index created to solve the same problem. The bootstrap example is the training set, and the group of observations that are not included in the bootstrap example serves as the test set (Kulekçi et al., 2022). In order to talk about the reliability of the established MARS model, it is important that the generalization ability is good. However, MARS analysis can be performed using Bootstrap, one of the resampling methods (Akin et al., 2020).

### 2.2.2. A MARS Model Application

Earth and ehaGoF packages were used for the MARS model in the study. With the earth package, the same basic functions are generated for MARS prediction models created simultaneously for more than one dependent variable. As can be seen, MARS models produced with the *earth* package have different coefficients. To make this estimate, the Generalized cross-validation (GCV) method, a computational solution for linear models that provide an estimated exclusion cross-validation error metric, is used. According to the GCV criterion, MARS generalizes the model by eliminating the terms. GCV is given by Equation 2, a form of regulation that balances model complexity with the goodness of fit (Eyduvan et al., 2019; Akin et al., 2020; Akin et al., 2021; Çanga et al., 2021)

$$\text{GCV} = \sum_{i=1}^N \frac{(y_i - \hat{y})^2}{\left(1 + \frac{c}{N}\right)^2} \quad (3)$$

Here,  $C = 1 + cd$ , is the number of items in the  $N$  dataset;  $d$  is a degree of freedom;  $c$  is the basic function addition penalty.  $y_i$  Is an independent variable and  $\hat{y}_i$  is an estimated value (Eyduran 2020; Akin et al., 2020).

### 2.2.3. Model validity:

The most common model fit criteria to be used in measuring the predictive accuracy of the MARS algorithm (Goodness of Fit Criteria) are the goodness of fit criteria such as R-square, RMSE and MAE mentioned below (Akin et al., 2020; Eyduran et al., 2019; Eyduran and Zaborski, 2017; Çanga et al., 2021; Nayana,et al., Chesneau, 2022). The model was evaluated according to these values.

Determination coefficient ( $R^2$ ):

It is the percentage of the total variation in the response variable explained by the regression line. The equation is expressed by X.

$$R^2 = 1 - \frac{SSE}{SST} \quad (a)$$

Where  $SSE = (y_i - \hat{y})^2$  is the sum of the squares of the differences between the predicted and the observed value, and  $SST = (y_i - \bar{y})^2$  is the sum of the squares of the differences between the observed and the overall average value.

The adjusted determination coefficient ( $Adj. R^2$ ) is calculated with the formula Equation 4b.

$$Adj. R^2 = 1 - \frac{R^2(n - 1)}{n - k - 1} \quad (4b)$$

It is preferred to be close to the  $R^2$  value. Average square error (RMSE), average estimation error (is the square root of the average square error). The formula is stated as follows:

$$RMSE = \sqrt{\sum_{i=1}^n (y_i - \hat{y})^2} \quad (5)$$

Average error (ME) is the average estimation error. It is less sensitive to outliers. It is given by the formula as follows

$$ME = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}) \quad (6)$$

Mean absolute deviation (MAD) is the mean absolute estimate error. It is less sensitive to outliers. The formula is given as follows:

$$MAD = \frac{1}{n} \sum_{i=1}^n |y_i - \hat{y}| \tag{7}$$

Pearson correlation coefficient between actual values and estimated values in terms of a dependent variable (r),

$$PC = r_{y_i \hat{y}} = \frac{Cov(y_i, \hat{y})}{S_{y_i} S_{\hat{y}}} \tag{8}$$

$Cov(y_i, \hat{y})$ : The covariance between actual and predicted values in terms of a dependent variable,

$S_{y_i}$  : The standard deviation of the actual values of the dependent variable and

$S_{\hat{y}}$ : It refers to the standard deviation of the mined values of the dependent variable. Akaike information criterion (AIC)

$$AIC = n \ln \left[ \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y})^2 \right] + 2k; \text{ Eğer } \frac{n}{k} > 4 \tag{9a}$$

$$AIC_c = n \ln \left[ \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y})^2 \right] + 2k + \frac{2k(k+1)}{n-k-1}; \text{ otherwise} \tag{9b}$$

Standard deviation ratio ( $SD_{ratio}$ ):

$$SD_{ratio} = \frac{S_m}{S_d} \tag{10}$$

$S_m$ : Standard deviation of model error terms,

$S_d$  : The standard deviation of the dependent variable,

The standard deviation ratio is calculated with the SD ratio formula, and values less than 0.20 are preferred for biometric studies. The smaller it is, the more acceptable it is (Eyduran et al. 2017):

$\hat{F}_e(x)$  being the Mars prediction model; The bagging MARS model is as expressed in equation 10 (Breiman, 1994):

$$\hat{f}_{\text{Bagging MARS}} = \frac{1}{E} \sum_{i=1}^E \hat{F}_e(x) \tag{10}$$

### 3. Findings and Discussion

#### 3.1. Findings

Introductory statistics of continuous variables related to lactation yield used in the study are given in Table 1.

**Table 1.** Descriptive statistics of the studied explanatory variables.

	Month	SP	Total_yield	L7DMMY	LN	Age	FPA
Vars	1	2	3	4	5	6	7
n	9553	9552	9552	9533	9452	9312	9312
Mean	6.72	211.69	30.87	31.26	2.68	56.99	23.30
Standart Deviation	3.44	150.29	9.77	8.39	1.02	14.18	1.76
Median	7.00	193.00	30.40	30.91	3.00	65.00	23.00
MAD	4.45	149.74	8.64	7.12	1.48	2.97	1.48
Min	1	0	8.77	9.01	1.00	24.00	20.00
Max	12	691.00	79.18	116.78	5.00	71.00	27.00
Standard Error	0.04	1.54	0.10	0.09	0.01	0.15	0.02

Total yield: Total average milk yield of lactation; SP: Service Period, L7DMMY: mean milk yield for the last 7 days; LN: number of lactations; Age: Age of the animal, FPA: Age at first birth of the animal.

Introductory statistics related to independent variables such as milk yield and lactation period (month), age at first birth (FPA), age of animal (Age), number of lactations (LN) used in the study are given in Table2, Table3, Table4, respectively.

**Table2.** Descriptive statistics of monthly average milk yield and number of lactations

LN/Total yield	Mean± SE	N	Minimum	Maximum
1	24.43±0.249	1235	5	62
2	33.26±0.176	2885	1	71
3	28.98±0.166	3618	4	79
4	34.96±0.238	1383	3	68
5	31.99±0.248	432	6	66
Total	30.63±0.102	9653	1	79

In the study, a sample R script file was created for the data set. The data set of the studied lactation was first divided into two subsets, 70% training and 30% testing. Then, 50 bootstrap samples were created with the resampling method to obtain 3 MARS models using different sampling methods for the training set in order to determine the appropriate number of terms and the degree of interaction(Akin, Eyduran, and Eyduran, 2020).



The ehaGoF package was used to measure the prediction performance and generalization capabilities of the established models (Eyduran,2020).The data set obtained from approximately 10,000 data used in the research is important in terms of the reliability of the results obtained, working on large samples in data mining studies. Goodness of fit statistics calculated for MARS and Bagging MARS algorithms are given in Table 3. The prediction performances of MARS and Bagging MARS in predicting Total\_MY were evaluated comparatively. The results of the fit criteria are summarized in Table 3.

**Table 3.** Predictive performance of MARS and Bagging Algorithms

Methods	r	R <sup>2</sup>	Adj.R <sup>2</sup>	RMSE	SDratio	MAPE	MAD	AIC
<b>MARS</b>	0.988	0.968	0.968	10.204	0.178	1.374	4.846	143.073
<b>Bagging MARS</b>	0.762	0.436	0.435	7.364	0.751	4.515	5.405	735.927

**RMSE:** Root-mean-square error, **SD ratio:** Standard deviation ratio, **MAPE:** Mean absolute percentage error, **MAD:** Mean absolute deviation, **AIC:** Akaike Information Criteria

When Table 3 is examined, the order of superiority in the prediction accuracy of the mentioned algorithms is MARS > Bagging MARS according to the estimated model evaluation criteria. As can be seen, the prediction performance of the MARS algorithm was found to be better than Bagging MARS. The results of the MARS algorithm for cattle are presented in Table 4.

The model equation of the MARS algorithm is as follows. Total\_yield = 41.87 + 4.016 \* label13 + 3.385 \* label21 - 6.265 \* label4 + 2.017 \* label40 + 2.8 \* label45 - 1.392 \* Monthjune\_22 + 0.02707 \* max(0, 75 - SP) - 0.0177 \* max(0, SP - 75) + 0.02061 \* max(0, SP - 417) - 0.2831 \* max(0, L7DMMY - 32.32) - 0.7361 \* max(0, 41.5 - L7DMMY) + 0.4114 \* max(0, L7DMMY - 41.5) - 0.1251 \* max(0, 66 - Age) - 0.4353 \* max(0, Age - 66) + 0.9208 \* max(0, 22 - FPA) + 0.3967 \* max(0, FPA - 22)

**Table 4.** Coefficients of the MARS model and results of MARS analysis

Terms	Basis Functions (BF <sub>i</sub> )	Coefficients
	Intercept	41.87
BF1	Label13	4.016
BF2	Label21	3.385
BF3	Label4	- 6.265
BF4	Label40	2.017
BF5	Label45	2.8
BF6	Monthjune_22	-1.392
BF7	max(0, 75 - SP)	0.02707
BF8	max(0, SP - 75)	-0.0177
BF9	max(0, SP - 417)	0.02061
BF10	max(0, 41.5 - L7DMMY)	-0.7361
BF11	max(0, L7DMMY - 41.5)	0.4114
BF12	max(0, 66- Age)	-0.1251
BF13	max(0, Age - 66)	-0.4353
BF14	max(0, 22 -FPA)	0.9208
BF15	max(0, FPA - 22)	0.3967

Among the independent variables, the most important and highest positive effects are the variables belonging to Label13, Label21, Label40 cattle, respectively. When the variable numbered Label 13 is selected, that is, label 13=1, an increase of 4.016 units is expected in the total milk yield (Total\_MY)(Table3). Similarly, when Table 4 is examined; When the variable label 4 is selected, that is, when Label 4=1, a decrease of 6.265 units is expected in the total milk yield (Total\_MY).In addition, when the seventh term max(0, 75 - SP) and positive coefficient(0.02707) for Total\_MY of the service period (SP) are examined; For a variable with SP= 75 months or SP > 75, the positive effect of the service period (due to the coefficient) on Total\_MY will be masked. However, for a variable with SP<75, the time to last calving (SP) is expected to have an increasing effect (due to the coefficient) on Total\_MY. Although the SP value is 1 unit less than 75 months, an increase of 0.02707 liters is expected in the Total\_MY amount. The relative importance values of the independent variables are presented in Table 5. As seen in Table 5, the highest importance values are respectively; L7DMMY (100%), SP (28.6%), Label13 (22.8%), Age (20.3%), label21 (15.3%), Label4 (12.3%), Monthjune\_22 (12.3%), Label4 (12.3%), Label4 (Obtained for 9.6%, label40 (8.3%), label45 (7.1%), FPA (5.3%)

**Table 5.** Relative importance of independent variables in the model

Variables	Nsubsets	GCV	RSS
L7DMMY	16	100.00	100.00
SP	15	28.6	29.9
Label13	14	22.8	24.3
Age	13	20.3	21.9
label21	11	15.3	17.1
label4	9	12.3	14.1
Monthjune_22	6	9.6	11.2
label40	5	8.3	9.8
label45	4	7.1	8.5
FPA	3	5.3	6.7

(Akin, Eyduran, Eyduran, and Reed, 2020) and some previous authors (Boğa and Boğa, 2022; Çanga and Boga, 2019; Çanga and Boğa, 2022; Çelik et al., 2021; Turhan, 2020) and, as highlighted by the results of the current study, predicted that MARS captures linear, nonlinear and interaction effects of important factors in regression-type problems. This difference can be attributed to the overfitting problem that may occur in MARS. The problem is that the MARS model contains redundant terms that reduce the predictive quality. Therefore, redundancies should be removed from the MARS model, which has the maximum complexity in the forward transition, by using the backward pruning method (Eyduran et al., 2019). The best way to understand the overfitting problem is to estimate the  $R^2$  values for Cross-validation, training and test sets (Grzesiak and Zaborski, 2012), emphasized that if the standard ratio value of an established regression model is 0.10 or 0.40, there is good or very good fit. When Table 6 is examined, all coefficients for milk yield were found to be statistically very significant.

**Table 6.** Results of the MARS algorithm

<i>Coefficients:</i>	<i>Estimate Std</i>	<i>Std. Error</i>	<i>t value</i>	<i>Pr(&gt; t )</i>
(Intercept)	41.872269	0.347857	120.372	< 2e-16 ***
bx[, -1]max (L7DMMY-41.5014)	0.411366	0.062027	6.632	3.50e-11 ***
bx[, -1]max (41.5014-L7DMMY)	-0.736077	0.024382	-30.189	< 2e-16 ***
bx[, -1]max (SP-75)	-0.017704	0.001196	-14.800	< 2e-16 ***
bx[, -1]max (75-SP)	0.027067	0.005402	5.010	5.53e-07 ***
bx[, -1] max(Age-66)	-0.435297	0.107400	-4.053	5.10e-05 ***
bx[, -1] max(66-Age)	-0.125130	0.010561	-11.848	< 2e-16 ***
bx[, -1] label13	4.016018	0.453965	8.847	< 2e-16 ***
bx[, -1]Label21	3.385252	0.471059	7.186	7.16e-13 ***
bx[, -1]max (SP-417)	0.020615	0.002866	7.192	6.88e-13***
bx[, -1] label4	-6.265041	0.939251	-6.670	2.70e-11***
bx[, -1]max (FPA-22)	0.396662	0.087689	4.524	6.16e-06 ***
bx[, -1] max(22-FPA)	-1.391727	0.195930	4.700	2.64e-06***
bx[, -1] Monthjune_22	-1.922e+01	0.263221	-5.287	1.27e-07***
bx[, -1] max(L7DMMY-32.3214)	-0.283084	0.049394	-5.731	1.03e-08***

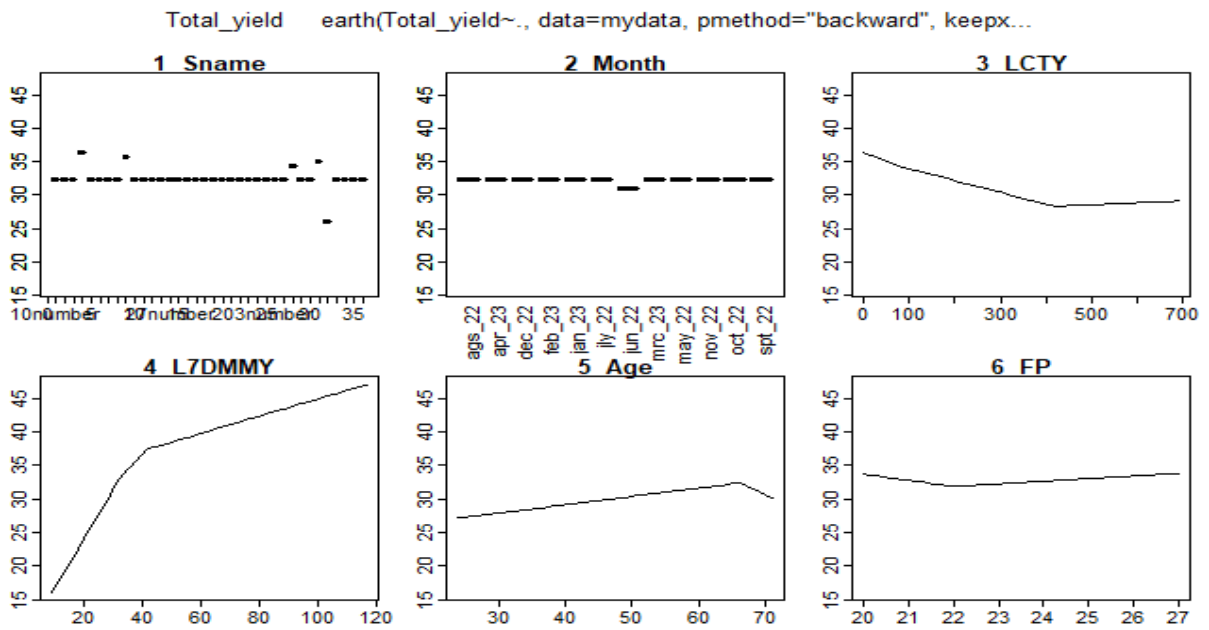
bx[, -1]label45	2.799577	0.557498	5.022	5.22e-07 ***
bx[, -1]label40	2.016650	0.472066	4.272	1.96e-05 ***
Significance codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1				

The prediction equation of the Bagging MARS algorithm is as follows:

$$\begin{aligned}
& 34.07 - 2.30 * \text{label11} + 2.39 * \text{label13} - 5.68 * \text{label37} - 6.63 * \text{label4} + 2.04 * \text{label40} - 3.33 \\
& * \text{label43} - 1.78 * \text{LN3} + 0.01 * h(410\text{-SP}) - 0.60 * h(39.31\text{-L7DMMY}) + 0.24 * h(\text{L7DMMY}\text{-}39.31) \\
& - 0.11 * h(66\text{-Age}) \\
& + 43.83 + 2.35 * \text{label13} - 6.63 * \text{label37} - 8.32 * \text{label4} + 2.70 * \text{label45} + 1.44 * \text{Monthfeb\_23} \\
& + 2.26 * \text{Monthmarch\_23} + 1.60 * \text{LN2} + 0.03 * h(71\text{-SP}) - 0.02 * h(\text{SP}\text{-}71) + 0.02 * h(\text{SP}\text{-}384) - \\
& 0.28 * h(\text{L7DMMY}\text{-}33.35) + 11.67 * h(\text{L7DMMY}\text{-}45.03) - 0.69 * h(45.30\text{-L7DMMY}) - 11.65 * \\
& h(\text{L7DMMY}\text{-}45.30) + 0.765 * h(\text{L7DMMY}\text{-}78.55) - 0.12 * h(66\text{-Age}) \\
& + 37.69 + 2.94 * \text{label13} + 3.39 * \text{label21} + 4.20 * \text{label24} - 8.21 * \text{label4} + 2.13 * \text{label40} + 5.70 \\
& * \text{label45} - 2.32 * \text{label9} - 2.09 * \text{Monthjune\_22} - 2.08 * \text{Monthmay\_22} - 1.13 * \text{Monthsept\_22} + \\
& 1.22 * \text{LN2} + 0.02 * h(379\text{-SP}) - 0.02 * h(\text{SP}\text{-}379) - 0.28 * h(\text{L7DMMY}\text{-}34.18) - 1.22 * h(\text{L7DMMY}\text{-} \\
& 41.02) + 7.31 * h(\text{L7DMMY}\text{-}44.53) - 0.64 * h(45.64\text{-L7DMMY}) - 6.08 * h(\text{L7DMMY}\text{-}45.64) + \\
& 0.76 * h(\text{L7DMMY}\text{-}77.37) - 0.12 * h(66\text{-Age}) / 3
\end{aligned}$$

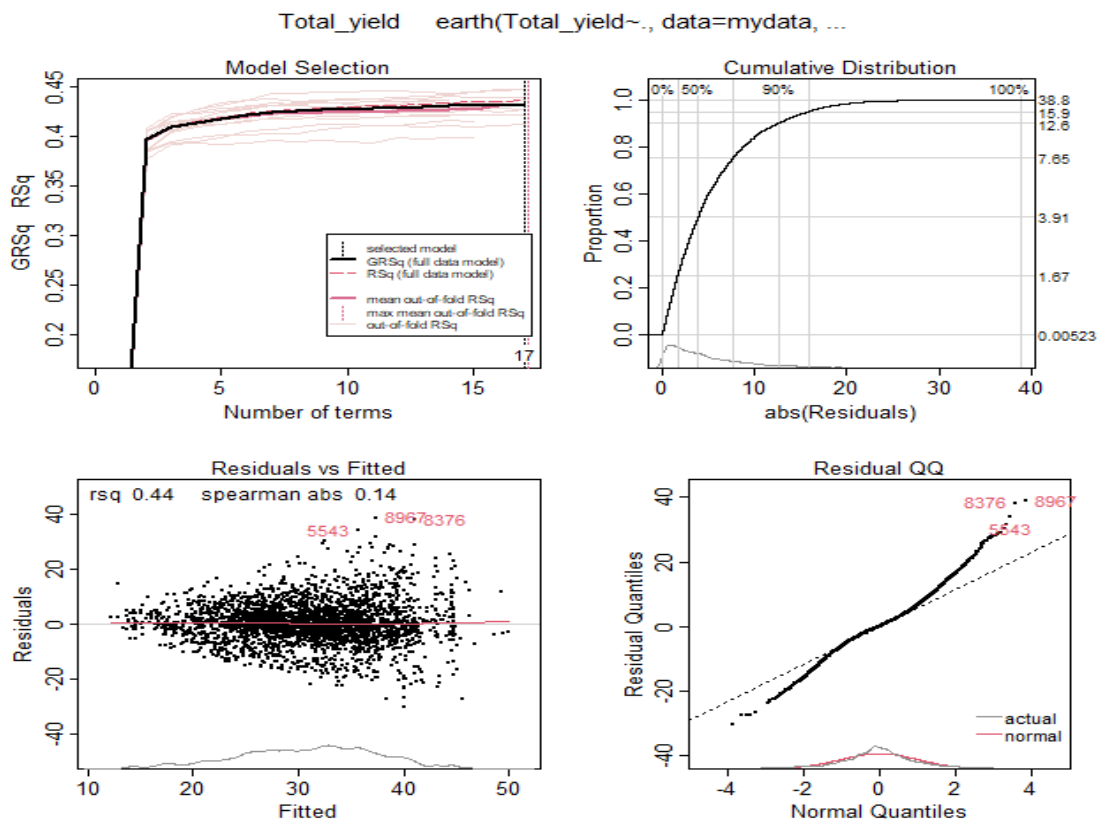
According to this obtained equation, in the first bootstrap equation, there is a negative decrease of 1.78266 units when lactation order = 3. The highest negative effect (- 6.634773) was caused by the variable number 4 on the label, while an increase of 0.0168345 units was observed when  $SP < 410$ , while a negative effect of -0.1068442 and -0.5982774 units was observed when  $L7DMMY < 39.31$ , respectively. In the second bootstrap equation, Monthfeb\_23 (1.444099), Monthmarch\_23 (2.268667), LN2(1.603694) contribute positively, while minor reduction is expected when  $Age \leq 66$  in all three bootstrap equations. The relationship between the predicted and observed predictive values of the Bagging MARS algorithm is shown in Figure 1.

In the Bagging MARS model, there is a binary interaction between the variables.



**Figure 1.** Relationship graphs between dependent variable and independent variables in Bagging Mars

Model selection, cumulative distribution of absolute errors, error values, distribution of predicted values and error QQ graphs of normal distribution of error values are given below for the MARS model selected according to cross validation instead of GCV(Figure2).



**Figure2.** Bagging MARS Model selection and graphs of error terms

### 3.2. Discussions

In the study, the effect of 4 different parameters (average milk yield in the last 7 days, service period, animal number 13, Age) on milk yield in cattle was found to be significant (Table 5). In this study, when the reproductive characteristics of cattle are examined; For the MARS model estimation equation for optimum milk yield, the corresponding optimum values for the independent variables Label, Month, SP, L7DMMY, LN, Age, FPA, respectively; 20, feb\_23, 194(day), 30,96286(lt), 3, 65(month), 23(month). These threshold values, which are created by the multi-response MARS model equation that constitute the basic functions, are the most common (Akin et al., 2020; Akin et al., 2020).

First gestational age, starting the productive life of heifers as early as possible is one of the factors that directly affect the profitability of the enterprises and this value varies according to the breeds. In this study, when we subtract the gestational age from the average gestational age (FPA), which was calculated as 23 months for the Holstein breed, the gestational dates for the first of the animals can be determined as an average of 14 months. These values are in agreement with the averages reported by the mean for the same breed (16.5, 18.3 months, and 16.8 months, 14.9, respectively (Alkoyak, 2016; Asan, 2021; Çetin and Alkoyak, 2018; Eyduran et al., 2008; Omar, 2022). The found service period obtained in this study was found to be 123 days and this value was 127 days in the study conducted by (Gürses and Bayraktar, 2012). Gürses and Bayraktar (2012) in TİGEM Ceylanpınar, Dalaman, Koçuş and Tahirova Agricultural Enterprises, on the same breed, while it was 127 days in Aydın province In the study conducted by the company Gürses (2019), (Gürses, 2019) it is shorter as 144 days; In the study conducted by Sarar and Tapkı (2017) (Sarar and Tapkı, 2017) in Koçuş Agricultural Enterprise, 106 days; In a study conducted by Arı (2019) in a private enterprise in Aydın province, 109 days, (Arı, 2019, Kopuzlu et al., 2008). Kopuzlu et al. (2008) in the Eastern Anatolia Agricultural Research Institute, it was found to be 119.9 days, (Omar, 2022) as 73.19 days by Omar (2022). Omar (2022) which is higher than the averages reported in the same breed.

Goodness-of-fit statistics are important in comparing data mining and other statistical methods used to predict any trait in cattle as well as in all animals. In recent years, many studies have used MAE, mean square error (MSE),  $AdjR^2$  to compare artificial neural network, MARS, correlation coefficient (r), RMSE and mean absolute models. and Akaike information criteria (AIC) statistics were used (Akin et al., 2020; Altay et al., 2022; Boğa and Boğa, 2022; Çanga, 2022; Çanga and Boga, 2019; Çanga and Boğa, 2022; Eyduran et al., 2019; Eyduran et al., 2020; Kulekçi et al., 2022; Şengül et al., 2022; Tirink et al., 2022). Although the goodness of fit statistics used by the authors in their studies are similar, the conditions for using the MARS method and the calculation conditions, correlation coefficient and RMSE statistics differ. In terms of the results obtained with other methods

and several different goodness-of-fit statistics used, the dependent variable was estimated (Şengül et al., 2022). Şengül et al. (2022) reported that the final body weights of Kıvırcık lambs were evaluated on the basis of MARS and Bagging MARS algorithms, and showed excellent performance as a robust algorithm without overfitting (Akin, Eyduvan, Eyduvan, et al., 2020). Akin et al. (2020) predicted that MARS captures linear, nonlinear and interaction effects of important factors in regression-type problems, as emphasized by some previous authors (Eyduvan et al., 2020; Öztürk, 2022) and those obtained in the current study.

In the current study, the average milk yield according to the lactation order in Table 2 varies between 24.43 and 34.96 (Omar, 2022). In the study of Omar (2022) the milk yield of Holstein and Simmental cattle was calculated as 305 days milk yield as 9690.02. When this result is divided by 305 days to calculate the average daily milk yield, it is  $9690.02/305=31.71$ , which is consistent with this value. In different studies conducted between 2005-2021 (Asan, 2021; Çetin and Alkoyak, 2018; Genç and Soysal, 2018; Keskin and Boztepe, 2011; Şahin and Ulutaş, 2010; Sarar and Tapkı, 2017; Tırnık, 2021; Yaylak and Kumlu, 2005) was reported to vary between 5395.11-8264.70 kg and these values are among the values of the current study.

#### **4. Conclusions and Recommendations**

Considering the results of this research, it was revealed that MARS algorithm gave better results in milk yield modeling of 305-day lactation. Many of the generated samples are derived from datasets, increasing the bagging precision. Thus, it is possible to compare the goodness of fit criteria by using resampling to create an estimator with more than one version. It is expected that this study will inspire data mining research that want to discuss the results using MARS and Bagging MARS algorithms in the future.

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## Competing of Interest

The author declared no competing interests.

## Author Contributions

DÇB conceived and supervised the study. DÇB statistical analysis and writing the manuscript. DÇB contributed to the critical revision of the manuscript and have read and approved the final version.

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