



# Re-examining the law of energy conservation-A Euclidean geometric proof

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## Abstract

The law of energy conservation is a cornerstone of physics, limiting energy use and dictating the efficiency of thermodynamic processes. The primary objective of this paper is to challenge the traditional acceptance of the law of energy conservation as an unprovable axiom by presenting a novel, provable, and purely geometric approach within the framework of Euclidean geometry, thereby re-evaluating its theoretical and empirical foundations. Driven by the ongoing pursuit of solutions to energy crises, the paper critically examines attempts to disprove the law and the search for alternative energy sources. Contrary to prevailing beliefs, it posits two key viewpoints: the lack of rigorous proof establishing the law's validity and the obscured motivations driving the invention of new energy sources. Highlighting the gap between theoretical acceptance and empirical evidence, the paper introduces a geometric framework to elucidate the empirical limitations and precision of energy conservation. Through this lens, it challenges the law's universal applicability, particularly debunking the notion of perpetual motion machines as proof of its validity. The findings include a geometric and practical redefinition of isolated systems, a proof of Newton's laws of motion, a geometric derivation of the Newtonian kinetic energy equation, and the demonstration of these geometric concepts' practicality independent of experiments. These insights call for a re-evaluation of the traditional understanding of energy conservation and offer transformative implications for future energy exploration and innovation.

**Keywords:** Energy conservation; Thermodynamics; Energy; Perpetual motion; Descartes; Spinoza; Leibniz; Euclid; Inverse points; Euclidean geometry

## 1 Introduction

The concepts of matter, motion, and energy have enthralled the best minds in philosophy and science for more than a century. The principle of conservation of energy is one of the most fundamental ideas relating these concepts in classical physics (Newton, 1687) [1,2]. Henri Poincaré, a prominent mathematician and physicist, argued that experiments cannot definitively prove foundational concepts like the uniformity of time, the law of inertia, and the principle of energy conservation [3]. He pointed out that experiments themselves rely on conventions, such as the definition of time units, which can be chosen differently (Poincaré, 1904) [3,4]. Despite this, the correctness of the underlying principles is not compromised (Einstein, 1916) [5]. From various perspectives, the principle of energy conservation has been viewed as an unprovable axiom due to the lack of a direct, empirical verification (Mach, 1883 [6]), [7,8]. The primary objective of this paper is to challenge this assumption by presenting a novel, provable, and purely geometric approach for the principle within the framework of Euclidean geometry. Considerably, it is important to remember that while experiments play a crucial role in physics, the ultimate goal of scientific theories is to establish their consistency with the observed world [9,10]. This geometric proof serves as a formal demonstration of the principle's internal coherence, independent of specific measurement conventions. This paper specifically addresses two key gaps in existing literature: the lack of a rigorous, formal proof for the principle of energy conservation and the disconnection between theoretical frameworks and practical

applications. First, it develops a purely geometric proof of energy conservation, drawing upon Euclidean axioms to establish a theoretical foundation that is both universal and logically irrefutable. Second, the paper redefines the relationship between isolated systems and material particles to clarify energy redistribution across various forms, including kinetic and potential energy. These contributions not only fill existing theoretical voids but also provide a robust platform for re-evaluating the empirical limitations and precision of energy-related laws, offering fresh perspectives on their validity and applicability. While a defining characteristic of scientific theories is their provisional nature and openness to revision [11,12], the principle of energy conservation has held a remarkably rigid position for centuries, seemingly defying this very principle. This enduring quality of the principle motivates us to explore why, despite the lack of a rigorous proof, it has remained universally accepted. It is intriguing to consider that a serious attempt at proving energy conservation could lead to unexpected discoveries about our current understanding of physics. This novel "physics-geometry" review hinges on the distinction between "energy/matter" and "energy system/matter system". A pivotal aspect of this work is its integration of philosophical discourse into the geometric proof framework. Philosophical debates on the nature of foundational principles—ranging from Poincaré's views on the provisional nature of physical laws to Kant's emphasis on inherent understanding—serve as a backdrop for re-examining energy conservation. By bridging philosophical reflections with rigorous geometric methodologies, this

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paper highlights the relationship between abstract reasoning and empirical insights. This synthesis not only contextualizes the geometric proof within a broader intellectual tradition but also challenges entrenched assumptions about the unprovability of energy conservation, advocating for a deeper alignment between philosophical principles and scientific practice. The primary aim here is to characterize the fundamental unity between these concepts. Specifically, the foundation of this review lies in the relationship between a thermodynamically isolated energy system and how particulate systems interact within this hypothetical framework. Considerably, the paper acknowledges that physics itself does not operate on the concept of “proof” in the strict sense. Unlike mathematics, which is a deductive science [13-15], physics is inherently inductive, relying on observations to build theories (Karl Popper, 1959 [16]), [17]. The closest equivalent to proof in physics involves creating a mathematical model of a classical system, deriving mathematical consequences within that model, and then interpreting those consequences back into the physical world [12,18]. Therefore, the concept of absolute proofs for physical principles is more relevant to the domain of pure mathematics and has limited applicability to scientific disciplines. This paper advocates for the establishment of scientific norms that enable rigorous proofs in physics, extending beyond mere mathematical consequences within physical models. A central premise is that the absence of such proofs fosters misconceptions about fundamental physics concepts, such as energy and the principle of energy conservation in physical systems. Consequently, this paper presents a novel type of proof – a geometric demonstration of energy conservation – that departs from the usual approach in physics by deriving the principle from fundamental geometrical truths, mirroring Euclid’s axiomatic approach in geometry. The paper argues that the lack of well-defined methods for rigorous proofs in physics is not an intrinsic limitation of scientific reasoning itself. The strong link between physics and mathematics presents a significant opportunity to establish verifiable scientific concepts that are both theoretically robust and experimentally independent. Accordingly, this paper calls for a shift from justifications based solely on observation and experimentation within physical models towards a more rigorous “proof-oriented” approach for scientific concepts. The current paradigm often relies on an inherent understanding of the fundamental nature of things based on our everyday experiences (Immanuel Kant, 1781 [19]), [20]. This paper challenges the notion that the principle of energy conservation is unprovable by establishing a geometric proof analogous to Euclid’s demonstrations in geometry. Building upon Newton’s Laws of Motion and the concept of energy redistribution across particulate structures in all material systems, this paper offers a geometric perspective on certain physical and philosophical concepts. The principle of mechanical energy is extended to encompass various energy forms by leveraging the particulate nature of material systems. Crucially, material systems are fundamentally composed of interacting particles, ranging from elementary

particles to those classically understood and relevant to our understanding of the world [21].

## 2 Literature review

The concept of proof in physics, particularly in the context of energy conservation, differs significantly from its mathematical counterpart [12,18]. While mathematics seeks absolute certainty, physics often relies on the construction of mathematical models that approximate real-world phenomena. These models, when subjected to rigorous analysis, can provide compelling evidence for the conservation of energy. This section will delve into the key mathematical frameworks used to demonstrate energy conservation in classical systems, such as the Lagrangian formalism [22,23], Noether’s theorem [24,25], and the Hamiltonian framework [26]. While these methods offer powerful insights, it is essential to acknowledge their limitations, especially when dealing with anomalous cases such as the electrical short circuits modeled in this paper. The applicability of these methods is subject to certain limitations, including the assumption of idealized systems [22,25], the distinction between discrete and continuous systems, the presence of non-conservative forces [1], and the emergence of energy conservation as a property of complex systems [1,2,27]. For instance, many mathematical proofs of energy conservation assume idealized conditions, such as frictionless surfaces or point masses, which may not accurately reflect real-world scenarios. Additionally, while these methods primarily focus on continuous systems, real-world systems often involve discrete elements or quantum phenomena, which can introduce complexities not fully captured by classical models. Non-conservative forces, such as friction or air resistance, can also introduce energy dissipation, making the conservation of total mechanical energy less straightforward. Moreover, in complex systems, energy conservation may be a property that emerges from the interactions of many individual components, making it challenging to derive the conservation law directly from the fundamental properties of the system.

### 2.1 The Lagrangian approach to energy conservation

In classical mechanics, the principle of energy conservation is most commonly derived from the Lagrangian formulation [1,22,28]. The Lagrangian function, denoted by  $L$ , is defined as the difference between the system’s kinetic energy  $T$  and potential energy  $V$ :  $L = T - V$ . Using the Euler-Lagrange equation, the equations of motion for the system can be expressed as:  $\frac{d}{dt} \left( \frac{\partial L}{\partial \dot{q}_i} \right) - \frac{\partial L}{\partial q_i} = 0$ ; where  $q_i$  are the generalized coordinates of the system and  $\dot{q}_i$  are their velocities. If the Lagrangian does not explicitly depend on time, the system is time-independent, leading to the conservation of energy. The energy is expressed through the Hamiltonian  $H$ , which is derived from the Lagrangian as:  $H = \sum_i \dot{q}_i \frac{\partial L}{\partial \dot{q}_i} - L$ . The Hamiltonian corresponds to the total energy of the system and remains constant if the system’s dynamics are time-invariant. This process—constructing a model using the Lagrangian, deriving the equations of motion, and interpreting the Hamiltonian as a conserved

quantity-serves as the closest analog to proof in physics for energy conservation. However, while the Lagrangian formalism is mathematically rigorous, its assumptions often fail to hold in practical physical scenarios. The model assumes a closed system where all forces are conservative [22,29,30], and it breaks down in systems that involve non-conservative forces such as friction or electrical resistance. For example, in the case of an electrical short circuit (modeled in Figure 8), the rapid dissipation of energy as heat due to minimal resistance introduces non-conservative effects that are not accounted for by this framework. The inability to describe energy dissipation means that the derived model does not fully capture the physical behavior of systems with irreversible processes, highlighting the limitations of applying the Lagrangian approach universally.

### 2.2 Noether's theorem and conservation laws

Noether's theorem is another mathematical framework that models physical systems and derives conservation laws [24,25]. The theorem states that for every continuous symmetry of the action (integral of the Lagrangian), there is a corresponding conserved quantity. In the case of time-translation symmetry, Noether's theorem leads to the conservation of energy. If the Lagrangian  $L$  is invariant under time translations  $t \rightarrow t + \epsilon$ , the energy, expressed by the Hamiltonian  $H$ , is conserved according to:  $\frac{dH}{dt} = 0$ . This result provides a profound connection between symmetries in the mathematical model and the physical conservation of energy. The application of Noether's theorem involves constructing a model of the system based on its symmetries and interpreting the mathematical consequences of these symmetries as physical conservation laws. While this approach is robust and elegant, it assumes ideal conditions where system symmetries are perfect. However, physical systems often exhibit deviations from these idealizations. For instance, in standard circuit theory, an electrical short circuit exemplifies an anomalous event where energy is rapidly dissipated as heat. Such events disrupt the time-translation symmetry upon which Noether's theorem relies, leading to observable deviations from energy conservation. These disruptions highlight the limitations of the theorem in describing non-ideal, dissipative systems. The detailed empirical and theoretical proof of how an electrical short circuit violates the law of energy conservation, including the specific mechanisms through which time-translation symmetry is broken, is a complex topic requiring comprehensive mathematical and physical analysis. This specific investigation is thoroughly addressed in a separate article dedicated to the subject. For this discussion, the focus remains on the theoretical foundation provided by Noether's theorem and its limitations under idealized conditions.

### 2.3 Modeling energy conservation with Hamiltonians

Hamiltonian mechanics is another framework that models classical systems and derives energy conservation laws. The Hamiltonian  $H$ , which represents the total energy of the system, evolves according to Hamilton's equations:  $\dot{q}_i = \frac{\partial H}{\partial p_i}$ ,  $\dot{p}_i = -\frac{\partial H}{\partial q_i}$ , where  $q_i$  are the generalized coordinates

and  $p_i$  are the conjugate momenta [1,31]. In time-independent systems, the Hamiltonian is conserved, representing the total energy as a constant of motion. This approach is often used to model isolated systems where energy transformations are fully reversible. While Hamiltonian mechanics provides a rigorous mathematical model for energy conservation, it assumes that all energy transformations are reversible and that no energy is lost to non-conservative processes. Again, in the case of electrical short circuits, where energy is rapidly dissipated as heat due to minimal resistance, the Hamiltonian framework cannot capture the irreversible nature of energy loss. The model's assumptions break down, as it is unable to account for the non-conservative forces at play in real-world systems. Thus, while Hamiltonian mechanics models energy conservation effectively in idealized settings, it is limited in scope when applied to systems with significant dissipative effects.

### 2.4 Conservation of energy in non-conservative systems

In systems that involve non-conservative forces, such as friction or electrical resistance, the traditional proofs of energy conservation derived from Lagrangian or Hamiltonian mechanics fail [32,33]. The work-energy theorem, which accounts for both conservative and non-conservative forces, provides a more accurate model for these systems. The total mechanical energy is no longer conserved, as energy is dissipated. This can be expressed mathematically as:  $\Delta T = W_{nc} + W_c$ ; where  $\Delta T$  is the change in kinetic energy,  $W_{nc}$  is the work done by non-conservative forces, and  $W_c$  is the work done by conservative forces. In the context of electrical short circuits,  $W_{nc}$  represents the energy dissipated as heat (the chaos expanded in Equation (45)), illustrating that the total mechanical energy decreases over time. This dissipation is a physical consequence that cannot be derived from the traditional models discussed earlier, further demonstrating their limitations. In such cases, these models, while mathematically consistent, fail to fully capture the complexities of non-ideal, real-world systems.

### 2.5 A geometric perspective on energy conservation in complex systems

As discussed, in modern physics, the law of energy conservation has primarily been approached through advanced mathematical frameworks such as the Lagrangian and Hamiltonian formulations, and Noether's theorem. These methods are highly effective within the context of ordered systems and scenarios governed by well-defined constraints. However, they often lose clarity when dealing with chaotic, disordered, or complex systems, where the behavior of energy is less predictable [33,34]. The reliance on abstract mathematical representations, while powerful, can obscure the intuitive physical interpretations of the systems they model. This creates a gap, particularly when attempting to reconcile energy conservation in chaotic or less-structured classical systems, thus opening a need for alternative approaches that offer both rigor and clarity. One such alternative approach lies in the principles of Euclidean geometry [35], which provide a constructive and physically interpretable foundation for addressing the conservation of

energy in both ordered and chaotic systems. Euclidean geometry not only allows for the geometric construction of fundamental operations but also provides tools for proving solutions to polynomial problems, such as those explored by Descartes in his geometric operations [36,37]. This imperial geometric approach emphasizes a tangible, visual form of reasoning, grounded in constructability, which contrasts with the abstract symbolic manipulation found in modern physics and non-Euclidean methods [38-40].

### 2.5.1 Theoretical rigor and physical limitations in energy conservation

The Lagrangian, Hamiltonian, and Noether's theorem models, while providing a rigorous mathematical approach to energy conservation in classical systems, are ultimately limited by their characteristic assumptions of isolated, reversible, and symmetric systems [1,25]. These methods, designed for ordered and well-defined systems, struggle to capture the complexity of chaotic or disordered systems, where energy dissipation and non-conservative forces are prevalent [34,41]. Lagrangian mechanics, based on the principle of least action, offers a powerful framework for systems with smooth energy distribution and conservation. However, its reliance on differential equations can hinder its ability to interpret chaotic systems, where energy flows unpredictably. Similarly, Hamiltonian mechanics, while effective for simplifying certain dynamical problems, relies heavily on mathematical abstraction and provides little insight into the practical and geometric nature of energy in classical physics. Both Hamiltonian and Lagrangian methods are tailored for smooth, deterministic systems, limiting their use in chaotic or discontinuous systems. Noether's theorem, which links symmetries of a physical system to conservation laws, provides profound insight into the nature of energy conservation [25]. However, this method requires the existence of continuous symmetries, which may not be present in disordered or chaotic systems. Furthermore, Noether's theorem, while elegant, offers a highly formal mathematical explanation that can lose sight of the tangible, constructive essence of physical laws. These methods, though immensely valuable, demonstrate a clear disconnect between the abstract mathematical domain and the physical, tangible reality that geometric methods address more directly.

### 2.5.2 Euclidean geometry-A constructive foundation for energy conservation

Euclidean geometry, in contrast to modern mathematical frameworks, offers a constructive framework for understanding the physical properties of energy conservation. Geometric principles emphasize the creation of shapes, lines, and figures through definable operations, which can be directly visualized and understood [42-44]. In classical systems, where chaotic dynamics or complex polynomials emerge, Euclidean geometry offers a practical and concrete method for exploring how energy distributes and conserves within the system (this notion is elaborated in Theorem 2). For instance, Descartes' geometric solutions to polynomials demonstrate how physical principles, such as equilibrium points or energy distribution, can be explored

using constructible operations [44]. Geometric proofs based on Euclidean principles can ensure that solutions are not merely abstract but grounded in operations that can be performed with basic tools like a straightedge and compass [40,43]. This physicality aligns with the classical interpretations of energy, where forces and motions can be visualized and constructed geometrically. In this light, the conservation of energy can be understood as a geometric construct: energy conservation in a system implies that no matter the transformation or configuration, the geometric properties of the system—such as its area or volume—remain constant. This geometric invariance echoes the physical invariance of energy in a closed system, providing a clearer, more intuitive model for understanding the law of energy conservation.

### 2.5.3 Applicability to chaotic and classical systems

In chaotic systems, where the smooth predictability of modern physics methods breaks down, geometric principles can offer an alternative interpretation. By understanding the system through geometric constructions, we can establish models that track how energy flows and redistributes in ways that are physically realizable. For instance, a chaotic pendulum or turbulent fluid can be described in terms of its geometrically conserved properties, such as rotational symmetry or volume in phase space. Euclidean geometry allows us to visualize how energy moves through such systems in a concrete way that Lagrangian or Hamiltonian methods might only approximate abstractly. Moreover, Euclidean geometric operations offer a rigorous model for solving polynomial equations or modeling systems where energy flows through non-linear interactions [44]. In classical systems, the trajectory of energy flow can be constructed geometrically, allowing for a physical interpretation of conservation laws that transcends mere symbolic representation.

#### *Physical interpretation of energy conservation through geometry.*

The constructive nature of Euclidean geometry directly maps onto the physical interpretation of energy conservation. In classical physics, energy conservation is often represented as a principle that holds across all transformations of a system. Geometrically, this can be understood as the invariance of certain properties—such as area or distance—under transformations like rotation, translation, or scaling. For example, the area of a triangle remains constant under rotation or reflection, just as the total energy in a system remains constant, even as it transforms from kinetic to potential forms. By grounding energy conservation in imperial geometric operations, we move away from abstract, mathematically complex descriptions and towards a physical interpretation that is intuitive, constructive, and visually realizable. As demonstrated in Definition 10, this approach provides a direct, physical model for energy conservation, one that applies not only in well-ordered systems but also in chaotic and disordered systems where energy distribution may be harder to capture with modern physics methods.

## 2.6 Analyzing energy conservation

This paper explores the principle of energy conservation from two complementary perspectives. First, it analyzes the interaction between material particles using Newton's Laws of Motion (Newton, 1687) [45]. This analysis demonstrates that during any interaction, energy transfers between the particles in equal amounts, thus conserving the total energy. Conversely, when particles do not interact, their individual energies remain constant, again leading to overall energy conservation. This concept provides a foundation for extending the reasoning behind energy conservation to any system. Second, the paper introduces the Euclidean geometric system as a practical framework for translating the quantities "geometric points" into physical systems composed of particles (*point-particle* (Definition 1)). This perspective allows for viewing energy conservation through a geometric lens. Euclidean geometric models are established within this paper to represent the relationships between material structures on a Newtonian scale.

## 2.7 Natural forces and geometric equivalence

The principle of energy conservation itself is remarkably simple, yet it manifests in a vast array of forms. This universality and unity between simplicity and complexity can make it challenging to recognize the underlying simplicity within intricate phenomena. Classically, the existence of any structure in nature (material system) is definitively described by its inertial mass and the "structural" interacting forces between its components (Ernst Mach, 1883), [46]. These forces can be understood as a form of "natural symmetry" or "forceful competition" that allows the structure to exist in spacetime. If these forces are unbalanced, the structure becomes unstable and may collapse (refer to Section 4 for a detailed analysis using Newton's Laws). Following this principle, the net action forces acting on a system must be balanced by the sum of the net reaction forces and the net inertial forces [47,48]. Through the succeeding sections of the paper, these natural physical relationships between forces in equilibrium states will be observed and preserved by translating the interactions between material systems to geometric quantities while invoking the concept of equality, as presented in [49]. The employed translation involves establishing geometric constructs that directly correspond to our physical understanding. These constructs are based on the concept of a "Point-Particle" (Definition 1) within a in a "Euclidean-Plane" (Definition 2). This approach ensures a perfect comparison between the physical and geometric domains.

## 3 Contextual background

This section lays the groundwork for understanding the newly presented proof of the Law of Energy Conservation (LEC). It delves into three key areas-Section 3.1 (Foundational Philosophical Concepts) explores the core philosophical principles that serve as the bedrock for the proof. Section 3.2 (Historical Narrative) traces the historical evolution of LEC understanding, providing crucial context for appreciating the significance of the new proof. Section 3.3 (Re-evaluating Efforts to Challenge the Law) analyzes

the persistent, yet unsuccessful, attempts to defy the LEC. By examining these historical efforts, this section establish a strong foundation on which the new proof is built, highlighting the need for a more rigorous framework.

### 3.1 Foundational philosophical concepts

Despite its fundamental role in physics, the exact nature of energy remains a subject of philosophical debate [50,51]. While most scientists define energy as the capacity to do work, a more precise understanding may be required. In the domain of physics, the concept of energy is tightly linked to experiments that measure various quantities assumed to be driven by energy. However, the term "energy" can sometimes be used loosely as a catch-all explanation for phenomena that are not fully understood through established physical relationships. Due to the inherent complexity of the energy concept, some scientists attempt to bridge the gap by focusing on the relationship between energy and matter [52-54]. This approach leverages the well-defined properties of matter to gain a better grasp of the underlying principles governing energy. At the very least, it allows us to work with measurable aspects of matter and then translate those observations back to the concept of energy. Historical writings often described matter as possessing a mysterious essence [50,51,55], which this paper identifies as energy. Scientific discoveries have revealed the interchangeability of energy and matter under specific physical conditions [50,56]. This paper leverages the unifying principle that all known forms of energy can transform into matter and vice versa. Within this context, a material particle is treated as an energy carrier or equivalent. Throughout history, philosophers have debated the infinite divisibility of matter [57-59]. However, this paper focuses on a scientific approach grounded in evidence. To maintain focus on the proof, we posit the existence of a fundamental particle within Euclidean space, the smallest possible unit describable. This particle will possess characteristics of both Euclidean geometry and mathematical analysis. Furthermore, we assume the existence of a "Euclidean space (a geometric plane)" (Definition 2) where, for an arbitrary "point-particle"  $A$  accessible about a point  $O$ , the arithmetic operations of geometric multiplication (denoted as  $G_m \Rightarrow A \otimes B$  (Definition 8)) and geometric division (Denoted as  $G_d \Rightarrow A \oslash B$ ) can be performed using straightedge and compass constructions. Building on this framework, we define the physical quantity "point-particle" as follows.

#### Definition 1 (Point-Particle as a fundamental unit).

Let  $S$  be an infinite set of particles in Euclidean space (written otherwise, imagine an infinite set of particles in a flat, geometric space). According to the power set axiom, we assume that  $S$  can be scaled to a set  $P_p(S) = \{x \mid (\forall y (y \in x \Leftrightarrow y \subseteq S))\}$ , where  $\forall_y$  is a geometric arithmetic quantification (either  $G_m$  or  $G_d$ ) over the entirety of all sets and  $P_p(S)$  is a member of that totality. Thus, we call the member  $P_p(S)$ , a *point-particle*.

A simple notion of energy as an interchangeable quantity is explicitly established by [50] through logical operations

similar to those used in [Definition 1](#) to equate concrete (material) entities.

### A unifying perspective on matter and energy.

[Definition 1](#) combines logic with a physical perspective that resonates with ancient ideas about the nature of matter. It inherently implies the construction of fundamental quantities on a plane, encompassing both relativistic and ordinary (Newtonian) scales. Crucially, this definition applies specifically to a Euclidean geometric system, emphasizing the arrangement of objects within a Euclidean plane, not simply their projection using real numbers. As outlined, the Euclidean geometric system prohibits the direct use of real numbers to represent geometric quantities [39,40,60]. However, this paper also acknowledges that Euclid allowed for the inclusion of special types of numbers arising from geometric operations, like ratios [39]. This paper assumes the existence of both real numbers and geometric magnitudes, considering them not as direct substitutes for but, as representations of analogous quantities (objects) within the Euclidean framework. This is based on the understanding that Euclidean geometry lacks a formal definition for magnitude, and contextually disallows negative numbers and zero, suggesting geometric magnitudes cannot measure such ratios. Furthermore, the modern view on numbers does not necessarily imply their inherent existence in physical systems. Therefore, it is crucial to differentiate between using real numbers within geometry and using them in physics. This distinction creates challenges, but by strictly limiting how we interpret real numbers, we can integrate them with geometric magnitudes within the same physical context. In this context, this section posits that a set of point-particles, denoted as  $P_p(S)$  establishes a distinct relationship between the Euclidean geometric system and the physical description of matter. Consequently, when considering  $P_p(S)$  within a Euclidean space and utilizing solely positive real numbers as representations for  $P_p(S)$ , [Definition 1](#) logically embodies both intuitionistic and analytical characteristics for any instance of  $P_p(S)$ . This definition serves as a cornerstone for the subsequent sections of the proof.

### 3.2 Historical narrative (Perspectives on the LEC)

The law of energy conservation (LEC) has a rich historical background. Early formulations focused on the concept of mechanical energy within a conservative force field. The notion of mechanical work itself emerged alongside the development of mechanics principles. The terms “*mechanical work*” (*travail mécanique*) and “*quantity of motion*” are credited to Gaspard-Gustave Coriolis (1792-1843), [61] and René Descartes (1596-1650) [18,62,63], respectively. The modern understanding simplifies the concept by comparing the gains in kinetic energy and losses in potential energy for objects falling in a gravitational field, and vice versa for objects ascending. This paper utilizes the axiomatic Euclidean geometric model (for the established geometric rigor see [63-65]) as a foundation for a unique proof. This model leverages the strengths of logic to construct a proof that bridges the gap between the Euclidean

geometric system and analytical models. However, a key challenge arises when attempting to integrate a Euclidean plane with the modern mathematical structure reliant on coordinate systems. The coordinate system designates an arbitrary point  $O$  in the Euclidean plane as the “*origin*”. It has two perpendicular lines through  $O$  called the “ $x$  – *axis*” and “ $y$  – *axis*”. Any other point is describable on this plane by two real numbers  $(x, y)$ , which are thought of as the side lengths of a rectangle whose sides are perpendicular to the  $x$  – *axis* and  $y$  – *axis*. By recalling the earlier established restriction to the origin  $(x, y)$ ; where  $x \neq 0$  and  $y \neq 0$ , the translation from a Euclidean plane to coordinate plane allows us to identify the Euclid’s plane with the set  $\mathbb{R}^2$  of pairs of real numbers. In this context, the  $\mathbb{R}^2$  plane becomes a model of Euclid’s axioms (a mathematical structure that satisfies a specific interpretation of those axioms). This translation is the hurdle to overcome when establishing a physics proof analogous to geometric proofs within the Euclidean system.

### Motion and energy.

In Cartesian physics, the concept of motion is central. Descartes, in his work *Principia Philosophiae* [66], proposed that God was the primary cause of motion and maintained a constant quantity of motion within the universe. Energy, on the other hand, remains a concept beyond direct experience. While its existence is widely accepted, its exact nature is still debated [67]. This paper builds upon the concept of particulate structures as equivalent to energy models. However, this paper avoids delving into the historical debates surrounding energy that often carry religious undertones. While the core focus of this paper is the theoretical foundation of motion, energy, and matter, it recognizes the importance of understanding their historical development. This broader perspective enriches the understanding of these concepts by tracing their evolution and appreciating the intellectual journey that led to our current understanding. René Descartes, for instance, argued that both motion and inertia are universally constant, though their distribution can vary depending on location and time within the cosmos [68]. He viewed the universe as an extension of matter and motion. Building on Descartes’ ideas, Baruch Spinoza (1632-1677) adopted a propositional and proof-based approach in his work (as described by [69]). Similar to Descartes, Spinoza established a law of motion conservation, again relying on theological reasoning. He believed that God predetermined everything, including the nature of motion. Considerably, perspectives on these concepts can vary greatly. As a result, this paper remains focused on the theoretical framework, avoiding religious interpretations of energy. Gottfried Wilhelm Leibniz (1646-1716) challenged Descartes’ notion of absolute motion conservation [70]. Leibniz argued that while the total amount of motion in nature might not be constant, motion in any specific direction is conserved. While Descartes believed in a constant total amount of motion, Leibniz’s ideas on motion largely align with the geometric experiment established in [Definition 1](#) of this paper. This paper builds upon the concept of a “*point-particle*” to unify ideas analogous to the views of Descartes and Leibniz on motion and energy. The proofs

throughout this paper are fundamentally based on the models defined; *ETIS* (Definition 3) and *TIS* (Definition 5).

### 3.3 Re-evaluating efforts to challenge the law of energy conservation

The history of attempts to challenge the law of energy conservation reveals a fascinating, yet often misguided, trajectory. Early efforts, fueled by genuine scientific curiosity, aimed to explore the frontiers of energy generation. However, over time, these endeavors have become increasingly plagued by scientific misconceptions and a lack of rigorous frameworks [71-75]. This section delves into these issues and proposes a novel approach for establishing the law's validity.

#### Flawed use of perpetual motion machines (PMMs).

A common misconception among those who doubt the law of energy conservation is the belief in the possibility of perpetual motion machines (PMMs). These devices are often envisioned as mechanisms that can produce energy indefinitely without an external energy input [74-76]. This misunderstands the fundamental nature of energy – it is not a substance that can be created or destroyed. Instead, it is a fundamental property of matter and its interactions. The law of energy conservation, also known as the first law of thermodynamics, states that the total energy within a closed system remains constant. This means that energy can neither be created from nothing nor disappear without a trace. While energy can be transformed from one form to another, in the ordered states, the total amount of energy within the system always remains the same [77]. The second law of thermodynamics, a cornerstone of physics, provides further clarity on this matter. It states that in any isolated system, the entropy, or disorder, always tends to increase over time. This means that any process that appears to generate energy from nothing would inevitably violate the second law. As a result, the concept of a perpetual motion machine, while appealing, is fundamentally impossible.

#### The need for rigorous frameworks and a shift in perspective.

The historical lack of success in defying the Law of Energy Conservation (LEC) through traditional methods suggests the need for a fresh perspective. While the core principles of the LEC remain widely accepted, the frameworks used to establish its validity might require re-evaluation. This re-examination aims to address the concerns of skeptics and provide a clearer understanding of the conditions under which the LEC could potentially be violated. The historical reliance on experiments, while valuable (as championed by Descartes' view on the accessibility of experiments through logic, even without physical execution [78-80]), needs to be complemented by more robust theoretical frameworks. A rigorous mathematical proof, grounded in established physical principles, would provide a more solid foundation for understanding and applying the law. This paper addresses this critical need by presenting the first-ever proof of the law of energy conservation at the interface of Euclidean

geometry and physics. This unique approach leverages the well-defined principles of Euclidean geometry to construct a framework within which the law's validity can be demonstrably established. By translating geometric operations into a physical context, the paper offers a new lens for reasoning about energy conservation, one that surpasses the limitations of relying solely on the concept of perpetual motion.

#### The need for proof and its implications for sustainability.

The law of energy conservation has served as a cornerstone of physics for centuries, guiding our understanding of energy transformations and resource limitations. However, the historical lack of a rigorous proof has left room for misinterpretations and misguided attempts to defy the law. The sheer number of unsuccessful endeavors aimed at breaking the law underscores the importance of establishing a definitive proof beyond simple observation. While the law's practical applications have been evident for centuries, a provable foundation strengthens our understanding and paves the way for innovative solutions. In the face of the ever-growing energy crisis [81-83], a robust foundation for energy conservation becomes paramount for developing sustainable solutions. Through providing a rigorous proof, this paper aims to bridge the gap between theoretical understanding and practical application, ultimately leading to a more sustainable future.

#### The logic of proof.

The existence of a rigorous proof fosters trust in the law's validity, encouraging further scientific exploration. Without a solid foundation, skepticism and misunderstandings can hold back progress. A proof establishes a clear point of reference, allowing scientists to build upon established knowledge and explore new avenues for energy generation and utilization within the framework of the law. Scientific understanding is a continuous process [79,80], constantly evolving through new discoveries and reinterpretations of existing knowledge. This paper's contribution lies in its introduction of a novel proof within the unique context of Euclidean geometry and physics. Recognizing the limitations of past frameworks allows us to refine our understanding and develop more robust approaches to fundamental principles like energy conservation.

#### Breaking free from misconceptions.

Through addressing scientific misconceptions and presenting a novel proof, this paper opens the door to a new era of energy exploration. With a deeper grasp of the law of energy conservation, scientists can confidently explore alternative energy sources and devise innovative solutions to the global energy crisis. Moving beyond the constraints of perpetual motion machines and relying on rigorous frameworks heralds a future where energy production and utilization are anchored in sound scientific principles, ultimately fostering a more sustainable world.

#### 4 Geometric characterization of the proof

This section aims to establish a geometric configuration characterization of the proof within a *Euclidean-*

*Thermodynamic Isolated System (ETIS)* (Definition 3). Traditionally, a gap exists between rigorous Euclidean geometric proofs and the more characteristic, less rigorous proofs found in physics. The prevailing view often considers the Euclidean geometric system incompatible with physics, as exemplified in studies of general relativity [84]. However, this paper argues against such a definitive conclusion. The Euclidean geometric system inherently offers a robust framework for proofs that build upon the specifics of a problem, rather than imposing a pre-existing structure. This allows for both deductive and inductive proofs within the Euclidean framework, potentially extending its applicability to scientific reasoning. While physics traditionally relies on inductive approaches based on established practices [18,79], ongoing research highlights the limitations of proofs solely reliant on experimental observations and experiences for validation. This paper questions the necessity of always adhering to purely inductive methods in physics, which will be further elaborated upon later. Therefore, this paper challenges the assumed incompatibility between rigorous Euclidean geometric proofs and characteristic physics proofs. While the Euclidean geometric system leaves concepts like “Magnitude”, “Plane”, and “Equality” undefined, their corresponding terms, “Quantity”, “Space”, and “Equality” – often possess more concrete and tangible scientific interpretations. However, the challenge in this section lies in establishing a consistent mnemonic to bridge this gap throughout the analysis.

#### 4.1 Important terminologies

**Definition 2 (Euclidean Plane [Plane used interchangeably for Space]).**

In Euclid’s Elements, the term “plane” is employed contextually without a precise definition [35]. It appears that Euclid regarded a geometric plane as the inherent existence (here, carefully avoiding the philosophical notion of existence) of a geometric structure, representing the potential for a geometric quantity or magnitude, or the consideration upon which these geometric concepts can be conceived. This paper adopts a similar approach, defining a geometric plane as the *Euclidean Plane (or Space)* based on its intuitive and contextual understanding. This means that a plane is simply the underlying framework or space in which geometric figures and relationships can be defined and studied.

**Definition 3 (Euclidean-Thermodynamic Isolated System (ETIS)).**

Building upon Definitions 1 and 2, an *ETIS* is arbitrarily defined as a system comprising a minimum of two “point-particles”, each corresponding to distinct geometric objects referred to as points within a Euclidean plane.

#### Remark 1.

In many physical contexts, point-particles are commonly assumed to be identical. In the context of an *ETIS*, we interpret the similarity feature among point-particles geometrically, relying on the concept of equality within the

system’s geometries. This equality between geometric points holds a unique significance, as it does not describe the geometric configurations per se but provides an account of the relationships between geometric magnitudes (refer to lemma 1).

To proceed, we position point-particles at points  $A, B, O, U,$  and  $Z,$  with points  $O$  and  $U$  characterizing the geometries of the *ETIS*, and points  $A, B$  and  $Z$  constituting matter interactions within and outside the *ETIS*. Using straightedge and compass operations, and inverting point  $A$  in a Euclidean plane to basepoints  $O$  and  $U,$  the resulting inverse points  $A$  and  $B$  create a geometric singularity on a locus centered at the point of inversion (point  $O$ ). The subsequent proof demonstrates that Definition 3 describes a geometric configuration equivalent to the scientific understanding of an isolated thermodynamic system. As per empirical definitions, an isolated thermodynamic system is rigid, immovable, non-conductive of heat, perfectly reflective of all radiation, and impervious to all types of matter and forces [85,86].

#### 4.2 Formalizing Definition 3

This section rigorously establishes Definition 3 using the principles of Euclidean geometric constructions, specifically those achievable with straightedge and compass. The proof centers around demonstrating the geometric inversion of a point relative to a pair of distinct base points within a Euclidean plane. We begin by introducing the concept of “invasion” (defined precisely later), followed by the formal proof itself. For clarity, this section temporarily departs from the established concept of a point-particle. Instead, it utilizes the pure language of Euclidean geometry to build a solid geometric foundation. The concept of a “point-particle” will be reintroduced later when interpreting and translating the established geometric proof into the context of physics. For the conclusive steps of this proof, consider the following geometric experiment.

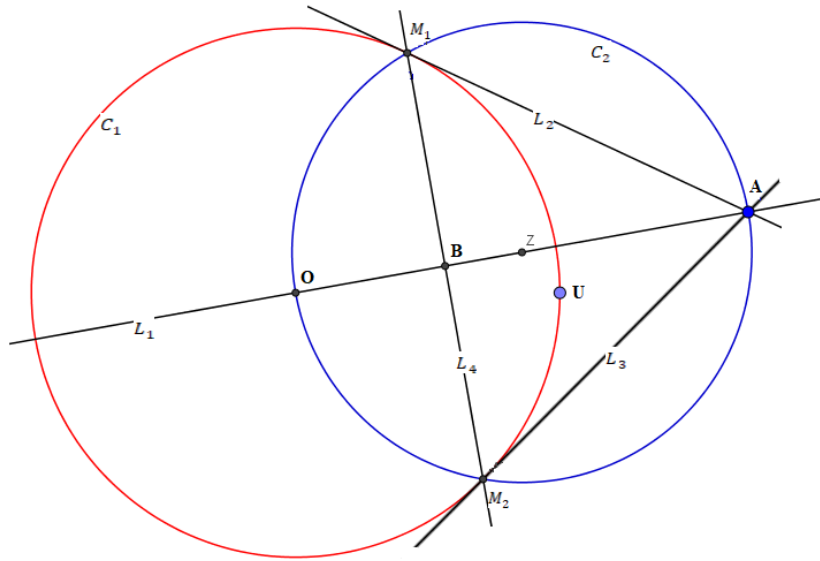
##### 4.2.1 A geometric experiment within an ETIS

The goal of this experiment is to illustrate the characteristics of a thermodynamically isolated system (*ETIS*) within a Euclidean Plane through a geometric approach. Employing Euclidean inversion techniques relative to distinct basepoints, the experiment showcases the behavior of point-particles within the *ETIS* under the influence of external forces originating from nearby particles. The geometric construction involves establishing circles, lines, and intersection points to demonstrate the motion and interaction of these particles within the system.

**Definition 4 (Euclidean inversion of a point  $A$  relative to a pair of basepoints  $O$  and  $U$ ).**

The Euclidean inversion of point  $A$  concerning distinct basepoints  $O$  and  $U$  is characterized by the geometric relation  $((OM_1)^2 = OB \times OA),$  where  $OM_1, OB,$  and  $OA$  represent valid geometric magnitudes subjected to a  $G_m$  operation. This inversion, designated as  $A^{-1},$  is established through a construction involving the points  $\{O, U, A\}.$





**Figure 1.** Geometric characterization of Euclidean-thermodynamic isolated system (*ETIS*) in a Euclidean Plane. (This figure articulates the Euclidean inversion process of point *A* relative to distinct basepoints *O* and *U*. This geometric characterization provides a detailed representation of the Euclidean-Thermodynamic Isolated System (*ETIS*) within a Euclidean Plane).

1. If  $U \cong O$ , construct the point *O*. Otherwise, proceed to step (2).
2. Construct circle  $C_1$  centered at the point *O* though point *U*.
3. Construct line  $L_1$  passing points *O* and *A*.
4. Construct the point *Z*, a bisection of  $L_1$ .
5. Construct circle  $C_2$  centered at the point *Z* though point *O*.
6. Let the points  $M_1$  and  $M_2$  denote the intersection points of the circle  $C_2$  and circle  $C_1$ .
7. Construct line  $L_2$  passing through the points *A* and  $M_1$ .
8. Construct line  $L_3$  passing through the points *A* and  $M_2$ .
9. Construct line  $L_4$  passing through the points  $M_1$  and  $M_2$ .
10. Construct point *B*, the intersection points of  $L_4$  and  $L_1$ .

Figure 1 illustrates the points *O* and *U*, delineating the geometric configuration of a circular plane, which we refer to as the Euclidean-Thermodynamic Isolated System (*ETIS*) in subsequent discussions. In this experiment, let the point *B* symbolize matter within the *ETIS*, denoted as a “point-particle” labeled as *n*. The objective is to show that the point *B* experiences motion solely under the influence of a force originating from another nearby “point-particle” in the vicinity  $C_1$ . This principle extends to any other particle (*n*) subjected to external forces, presumed to originate from the point *A*. For illustrative purposes, we propose that the circumference created by  $C_1$  acts as a permeable isolation wall, allowing the force from the point *A* to affect the point *B*. This implies that even if the isolated system defined by  $C_1$  is closely surrounded by other systems, its contents could still be influenced by external interactions. While somewhat aligning with the physics definition of an isolated system, this notion diverges significantly. In standard physics, a truly

isolated system remains impervious to external interactions, encompassing both matter and energy exchanges [85,86].

#### Distinct characteristics of the thermodynamically isolated system.

Furthermore, we conceive of this wall as naturally occurring, embodying the environmentally independent characteristic of a truly isolated system. This establishes a unique relationship between the interior of the system and its external environment. Within this thermodynamically isolated system, we assert two primary properties;

- **Physical Isolation.** The system operates independently from other systems, maintaining its internal characteristics without exporting its contents.
- **Information Preservation.** The system’s information structure remains intact, even upon the entry of foreign material.

#### Revelations from the geometric experiment.

The geometric experiment reveals that as the point *A* moves towards the circumference of  $C_1$ , the point *B* shifts towards the curvature of  $C_1$ , ultimately converging at the circumference. Further movement of the point *A* within  $C_1$  results in the dissolution of the geometric form of the circular plane, erasing information pertaining to the points *B*,  $M_1$  and  $M_2$ , along with the connecting lines  $L_2$ ,  $L_3$ ,  $L_4$ , and  $C_2$ . Notably, as the point *B* approaches the circumference  $C_1$ , point *Z* moves in the opposite direction.

#### Challenging traditional definitions of isolated systems.

This illustrative geometric experiment challenges the validity of commonly assumed physics definitions for a

thermodynamically isolated system. Traditional definitions typically fall into two categories.

- **Defn 1 (Infinite Separation).** The system is located infinitely far from surrounding systems, precluding any exchange of matter and energy (Figure 3 provided by [85]).
- **Defn 2 (Rigid Barrier).** The system is equipped with a rigid isolation wall obstructing matter and energy exchange with the surroundings [87].

This geometric experiment suggests that a truly isolated system might necessitate a different conceptualization, potentially amalgamating elements of both these traditional definitions while emphasizing the preservation of information within the system.

**Proposition 1.**

In physical settings, an isolated thermodynamic system maintains balance in its contents (matter-energy), signifying it as a self-sustaining model. The assertion of the physical relation  $E_s = 0$  (with  $E_s$  as the total energy within the isolated system) [77,88,89] challenges the assumed characteristics of thermodynamic isolated systems (Defn 1 and Defn 2), revealing them as a significant misconception of matter-energy content in such systems.

**Remark 2**

Expanding upon proposition 1, the proposition that the energy relationship  $E_s = 0$  is universally applicable [77,89] prompts consideration of the entire universe as a thermodynamically isolated system. In defining this isolation (Defn 2), it is suggested that the universe, in its physical essence, possesses an intrinsic boundary, mirroring an isolation wall, representing a perfect thermodynamically isolated system. However, the unknown size of the universe challenges this assertion, with projections indicating its indeterminability. The indeterminate size of the universe contradicts (Defn 2), as the isolation wall remains undefined. Consequently, assuming the validity of the relation  $E_s = 0$  for the entire universe renders (Defn 1) incorrect, as it implies isolation from other systems that cannot be part of the entire universe-an untenable scientific notion. Proposition 1 necessitates the rejection of conflicting definitions of a thermodynamically isolated system, leading to the introduction of a more rational definition (Definition 5) aligned with the constructed ETIS at the interface between the Euclidean geometric system and physics.

**Definition 5 (Thermodynamics isolated system-TIS).**

The Euclidean plane defined by the relationship  $(E_s \leftrightarrow M_s) \cong 0$  signifies a balanced interchangeability between total energy ( $E_s$ ) and matter ( $M_s$ ) within a system exhibiting the following characteristics:

- It is a Euclidean plane that is inherently geometrically extensible, in accordance with Euclid’s postulate on straight line extensibility [42].

- The system’s configuration establishes a rigid arbitrary structure, naturally preventing the exchange of  $E_s$  and  $M_s$  from both external sources into the system and from the system to the external environment.

In the subsequent sections, we will denote this system as *Thermodynamics Isolated System (TIS)*. Specifically, when implemented on a Euclidean plane, it will be denoted as *ETIS*.

Consider Theorem (1), facilitating the translation of this geometric proof into a more comprehensive scientific framework.

**Theorem 1.** For any given circle of inversion ( $C_{inv}$ ) with a center of inversion  $O$  and the radius  $\overline{OM}_1$ , the point  $A$  is an inversion of the point  $B$  outside the  $C_{inv}$  such that in its square, the magnitude  $\overline{OM}_1$  corresponds to the  $G_m$  of the magnitudes  $\overline{OB}$  and  $\overline{OA}$  where  $\overline{OA} > \overline{OB}$  and  $A$  is the point of intersections between the tangents to the  $C_{inv}$ .

Consider Figure 2 (an extended result of Figure 1) obtained by a construction from the points  $\{O, U, A\}$  as follows.

1. Construct a straight line segment  $L_5$  passing through the points  $O$  and  $M_1$ .
2. Construct a straight line segment  $L_6$  passing through the points  $O$  and  $M_2$ .

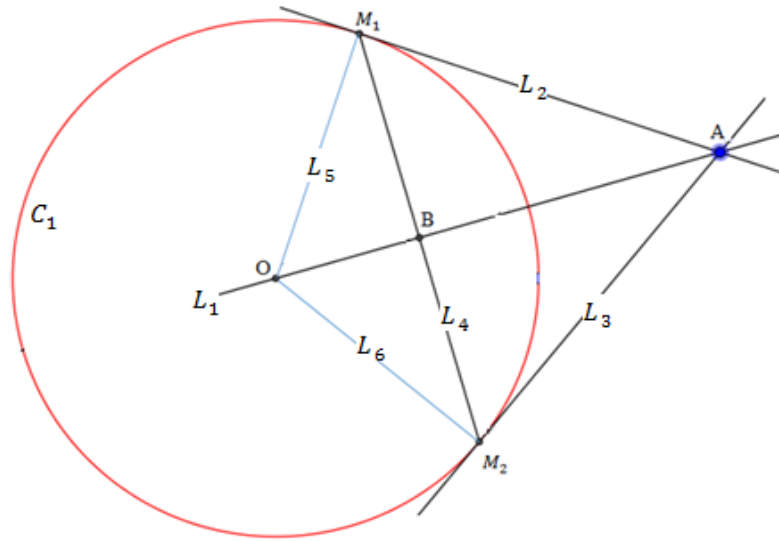
Through this construction, we derive two geometrically symmetrical triangles;  $OAM_1$  and  $OAM_2$  in Figure 2. Applying the theory of similar triangles to Figure 2 facilitates the proof of Theorem (1), subsequently establishing Definition 3. By considering the congruence property (Side-Angle-Side-(SAS)) for the similar triangles  $OM_1A$  and  $OBM_1$ , we deduce the relation  $\frac{OM_1}{OB} \cong \frac{OA}{OM_1}$ . This leads to the following geometric deduction.

$$\frac{OM_1}{OB} \cong \frac{OA}{OM_1} = (OM_1)^2 \cong OB \otimes OA \tag{1}$$

Equation (1) shows that the point  $B$  and the point  $A$  are geometric inverse points and the inversion is expressible in the form  $B = A^{-1}$ .

4.2.2 Interpretation and translation of the proof

Equation (1) represents a critical juncture in this paper. It translates geometric relationships with the precision of the Euclidean geometric system, specifically adhering to the principles outlined in the first six books of Euclid’s Elements [42]. The equation can also be interpreted scientifically using coordinate geometry (analytical geometry) within a physical context.



**Figure 2.** Geometric inversion of a point inside the circle of inversion to a point outside the same circle (The Geometric Characterization of a *ETIS*). (The figure demonstrates the construction from points  $\{O, U, A\}$ , leading to the creation of triangles  $OAM_1$  and  $OAM_2$ . The resulting geometric relationships, guided by the theory of similar triangles, provide evidence for [Theorem \(1\)](#) and contribute to the establishment of [Definition 3](#)).

**From a Euclidean geometric perspective.**

From a Euclidean standpoint, [Equation \(1\)](#) naturally involves operations between geometric magnitudes of the same kind, exemplified by magnitudes  $OM_1$ ,  $OB$  and  $OA$  in [Figure 2](#). Applying Euclid’s theory of proportions based on magnitudes of similar kinds to the geometric ratio  $\frac{OM_1}{OB} \cong \frac{OA}{OM_1} \cong \aleph$  (where  $\aleph$  is a positive real integer), the ratio  $\aleph$ , according to Euclid’s geometric scheme, possesses essential characteristics; it is a positive real number and non-zero [\[39,42\]](#). Under these conditions, [Equation \(1\)](#) can be carefully translated into an equivalent analytical geometric interpretation.

**Translation to analytical geometry.**

With systematic consideration for points in the Cartesian coordinate system, we arbitrarily designate a point of origin as  $(x,y)$  where  $x \neq 0$  and  $y \neq 0$ . We adhere to the conditions of the Cartesian coordinate system, acknowledging that no geometric magnitude can be zero in the Euclidean system. This disregards the analytic notion that the Cartesian origin (often denoted as  $(0,0)$ ) serves as a point of reference. The focus here is on geometric magnitudes, leading us to set conditions that  $OM_1 \neq 0$ ,  $OB \neq 0$ ,  $OA \neq 0$ , and that  $OM_1$ ,  $OB$  and  $OA$  are non-negative. This confines operations to real positive integers, allowing for their use as both geometric objects and descriptive language. Euclid’s Proposition 10 in Book 1 affirms the possibility of bisecting any straight line segment through straightedge and compass operations [\[90,91\]](#). This paper posits that any straight line segment can be infinitely bisected using these procedures. In analytical systems, a straight line segment is perceived with a material essence expressible on the coordinate system. Considering [Definition 1](#) and aligning with scientific

understanding, atoms are known to be theoretically infinitely divisible [\[92,93\]](#). To complete the proof, we assume the existence of an infinitesimally short line segment in the *ETIS*, corresponding to a perceptibly infinitesimal point-particle in the *TIS* perspective. Referring to [Figure 2](#), let the geometric magnitudes  $OM_1$ ,  $OB$  and  $OA$  represent the infinitesimally small interacting point-particles within the *ETIS*. This allows for quantifying the inherent properties (whether matter or energy) of these point-particles as objects using real numbers. This contrasts with the traditional Euclidean geometric system, which worries about the application of real numbers as representation of geometric magnitudes, and not as abstract expressions for the inherent properties of objects. Thus, the approach is within the inherent territory set up earlier in the paper.

**Physical interpretation.**

In a physics context, [Equation \(1\)](#) can be interpreted for *ETIS* with the center of inversion  $O$  and the radius of inversion  $(\overline{OM_1})$  given that point-particle  $A$  is the inverse of point-particle  $B$  outside the *ETIS* of inversion. In this interpretation, within its square, the particle system  $(OM_1)^2$  corresponds to a  $G_m$  on the point-particles  $A$  and  $B$  expressed as  $OB \otimes OA$ .

**Remark 3.**

The statement of [Theorem \(1\)](#) omits consideration of [\(Defn 1\)](#) and [\(Defn 2\)](#) as crucial components of an ideal *TIS*. This results in a naturally free system resilient to gains or losses of content similar to its structure and genetic contents. This scenario also applies when point-particle  $B$  is outside the inversion circle and point-particle  $A$  is inside it. Thus, [Definition 3](#) is established for a naturally existing *ETIS*.

**Remark 4.**

In the modern perspective, with the aid of a TIS, Definition 3 is established in a spherical model denoted by  $\mathbb{C}^3$  (extending beyond a Euclidean plane). Due to a lack of comprehensive understanding regarding the appropriate geometric models for describing the entire physical universe, it is prudent to characterize the properties of the universe from a Euclidean plane, as these properties remain independent of the system's geometries. Here, we associate the universe's infinitude with the indeterminate concept of infinity in the Euclidean context.

**Rethinking isolated systems**

**Remark 5 (A Consequences of Definition 3).**

According to traditional physics definitions (Defn 1), a thermodynamically isolated system is either incredibly distant from other systems or enclosed by rigid, impenetrable walls (Defn 2). However, proving Definition 3 using the described geometric experiment suggests these traditional definitions might be incomplete. In Figure 1, point B is closer to the assumed isolation wall ( $C_1$ ) compared to point A. yet the interaction between points B and A demonstrates an even meeting on the circumference  $C_1$ . This demonstrates that the distance between a system and its isolation wall is not the sole factor in isolation. Therefore, we propose a new way to understand a Thermodynamically Isolated System (TIS). A TIS inherently prevents the transfer of matter and energy in or out, potentially representing a self-sustaining system. While Equation (1) applies at any scale in our geometric model, the existence of observable Extremely Thermodynamically Isolated Systems (ETIS) in the physical world is beyond the scope of this paper. To ensure adherence to the Law of Energy Conservation, all geometric operations in this paper will be confined within an ETIS, aligning with the physics concept of a thermodynamically isolated system.

**4.3 Proving Newton's laws of motion**

A thorough examination of energy conservation theory underscores the necessity of involving Newtonian physics to rigorously prove LEC, particularly when considering the concept of motion between interacting bodies. To ensure balance, this paper significantly engages in providing geometric treatments for Newton's laws of motion. Emphasizing the law of inertia as a central component in two of Newton's three laws, this section focuses on proving Newton's first law ( $N^{1st}$ ) and the third law ( $N^{3rd}$ ), illustrating their integration in the second law ( $N^{2nd}$ ). The proof demonstrates how analogous models can be applied to establish LEC. A special case of  $N^{2nd}$  emerges naturally when the inertial force is zero, signifying balanced action and reaction forces. This leads to two crucial consequences: (1) balanced forces on any boundary interface surface ( $N^{3rd}$ ), and (2) non-accelerated systems ( $N^{1st}$ ). Fundamentally, all three Newton Laws of motion derive from  $N^{2nd}$ , making  $N^{1st}$  and  $N^{3rd}$  special cases when acceleration or mass is zero, respectively.

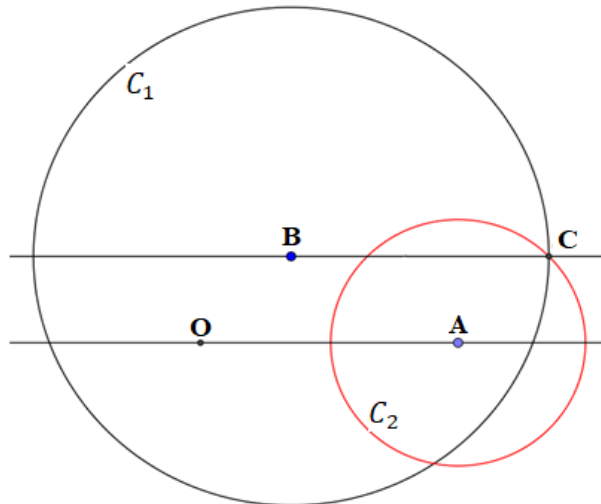
**4.3.1 A geometric model of the Newton's First Law ( $N^{1st}$ )**

The goal of this section is to show that all points of the parallel straight lines constructed from a chosen point  $O(x, y)$  through a distinct point  $A(x_1, y_1)$  in a Euclidean plane where  $O \neq A$ ; are the same.

**Lemma 1 (The empirical identity property for addition).**

For any point A,  $A \oplus O \cong A$ .

Consider two distinct points such that  $B \cong O$  and  $A \cong C$  in naturally constructed geometric configuration. We extend the addition property operation ( $\oplus$ ) via the following straightedge and compass construction.



**Figure 3.** Geometric Identity Property of Addition. (Illustrating a geometric model of Newton's First Law ( $N^{1st}$ ), this figure demonstrates the empirical identity property for addition lemma (1). The construction involves distinct points B and C, with  $B \cong O$  and  $A \cong C$ , and employs the addition operation ( $\oplus$ ) through a stepwise geometric process.)

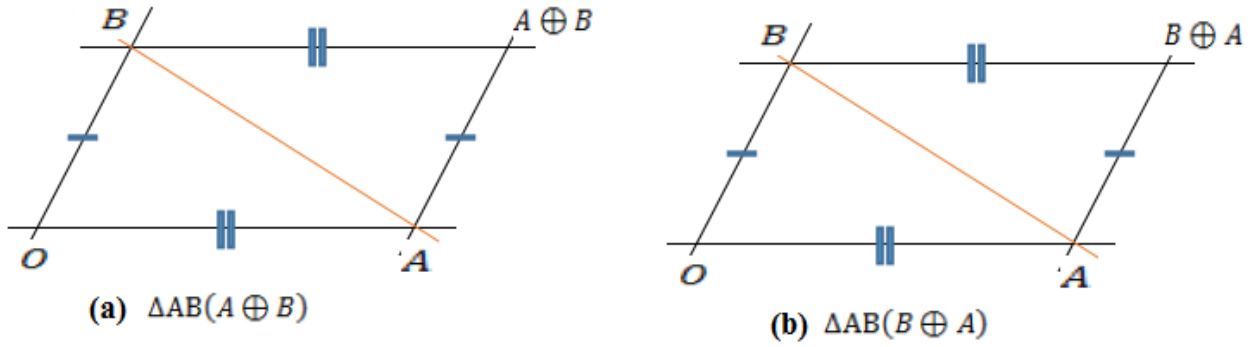


Figure 4. Geometric proof for Lemma 1.

1. If  $A \cong O$ , construct the point  $O$ . Otherwise, proceed through step (2).
2. Construct line  $L_1$  passing the points  $O$  and  $A$ .
3. Construct line  $L_2$  parallel to line  $L_1$  though point  $B$ .
4. Construct circle  $C_1$  of radius  $L_1$  centered at the point  $B$ .
5. Construct a point  $C$ , the intersection of the line  $L_2$  and circle  $C_1$ .
6. Construct circle  $C_2$  of radius  $\overline{OB}$  centered at the point  $A$ .

Figure 3 offers an extended fashion of lemma (1). In the essence of the described construction, it is assumed that both the lines  $L_1$  and  $L_2$  are constructed through the points  $O$  and  $A$ . The figure, therefore, provides a simplified geometric characteristic illustration for showing that when traced on each other, the lines  $L_1$  and  $L_2$  are geometrically equal (the same).

#### Claim 1.

The circle  $C_2$  intersects  $L_2$  through the point  $C$ , implying that the lines  $\overline{OB} \cong \overline{AC}$  and,  $O \cong B$  and  $A \cong C$  when the construction is not stretched.

#### Proof for Claim 1.

We redefine Figure 3 so that the inherently constructed point  $C$  corresponds to the point  $A \oplus B$  in the diagram (a) of Figure 4 and in a distinct view, the point  $C$  correspond to the point  $B \oplus A$  according in the diagram (b) of Figure 4.

Consider a congruent relation deduced from the diagram (a) of Figure 4 and diagram (b) of Figure 4 expressed as  $\Delta AB(A \oplus B) \cong \Delta AB(B \oplus A)$ , respectively. Further, based on Figure 3 we note that since  $\overline{OA} \parallel \overline{BC}$ , then  $\overline{OB} \parallel \overline{AC}$ . This corresponds to the schemes in the diagram (a) of Figure 4,  $\overline{OB} \parallel \overline{A(A \oplus B)}$  and in the diagram (b) of Figure 4,  $\overline{OB} \parallel \overline{A(B \oplus A)}$ .

#### Remark 6.

In Figure 4, the congruent triangles ( $\Delta AB(A \oplus B)$  and  $\Delta AB(B \oplus A)$ ) share points  $A$  and  $B$ , with their third points situated on the side  $\overline{AB}$ . The equality of these third points can be demonstrated through the following deductions.

Starting with  $\Delta AOB$ , we set the angles;

$$\angle OAB = \alpha \text{ and } \angle OBA = \theta \quad (2)$$

It follows that  $\angle AOB = \pi - (\alpha + \theta)$  (Angles sum in a triangle) (3)

We focus on  $\Delta AB(A \oplus B)$ , from the diagram (a) of Figure 4.

The  $\angle BA(A \oplus B) = \theta$ , and the  $\angle AB(A \oplus B) = \alpha$  (alternate angles to  $\angle OBA$  and  $\angle OAB$  respectively). (4)

Therefore,  $\angle A(A \oplus B)B = \pi - (\alpha + \theta)$ , (Angles sum in a triangle) (5)

Similarly, consider  $\Delta AB(B \oplus A)$  in the diagram (b) of Figure 4.

$\angle BA(B \oplus A) = \theta$  and the  $\angle AB(B \oplus A) = \alpha$  (alternate angles to  $\angle OBA$  and  $\angle OAB$  respectively). (6)

Therefore,  $\angle A(B \oplus A)B = \pi - (\alpha + \theta)$ , (Angles sum in a triangle) (7)

Since  $\overline{OB} \parallel \overline{A(A \oplus B)}$  and  $\overline{OB} \parallel \overline{A(B \oplus A)}$ , and,  $\angle A(A \oplus B)B = \angle A(B \oplus A)B$ , then  $\overline{OB} = \overline{A(A \oplus B)}$ . Thus,  $\Delta AB(A \oplus B)$  is similar to  $\Delta AB(B \oplus A)$  by the property; SAS. Equation (5) and Equation (7) show that  $A \oplus B = B \oplus A$ , and this proves lemma (1).

#### Translation of Lemma 1 to it physics equivalence.

Lemma 1, when translated into its physics equivalence, establishes a geometric framework limited to rectilinear forms of motion. This aligns with Descartes' early conceptualization of motion systems; wherein non-rectilinear motions were reduced to rectilinear motions. Descartes proposed that a body's tendency to move instantaneously is rectilinear, as only such motion can be clearly identified. According to Descartes, the conservation of motion occurs except during collisions, where the total motion is conserved but may be redistributed among the colliding bodies. To comprehend motion in a circle or within any other trajectory, it is essential to consider "at least two of its distinct instants, or rather two of its parts that are

distinct and the relations between them” [44,80,94]. Here, we reflect on the idea that a point-particle launched between two points in a Euclidean plane naturally seeks to continue moving in a straight line. This perspective is illustrated in the motion between points  $B$  and  $Z$  in the earlier-established *ETIS*. In Figure 1, it was observed that the causal effect of motion between the point-particles from points  $B$  and  $Z$  ensured that both particles followed a common straight line pathway. We affirm that Definition 4 and Lemma (1) offer reliable geometric frameworks for explaining concepts corresponding to physical situations in physics. The  $N^{1st}$  statement in physics involves rectilinear forms of uniform motions and motions influenced by external forces (non-rectilinear). Applying Descartes’ perspective on motion to a point-particle, this section contends that Descartes’ understanding is adequate to explain any motion executed by a point-particle in the *ETIS*. Reducing circular motion to instantaneous limits of rectilinear motion aligns with geometric principles, given the understanding that a straight line connects any two points in a Euclidean plane [95]. This implies that the  $N^{1st}$  is always rectilinear from a Euclidean geometric viewpoint.

#### 4.3.2 Formulating the $N^{1st}$ from the $N^{2nd}$

As mentioned earlier, the  $N^{1st}$  and  $N^{3rd}$  are pivotal to the  $N^{2nd}$ , being constructible from it. The genetic form of the  $N^{2nd}$ , rooted in the concept of force, is not explicitly known but is experienced in a physical system. This genetic form is characterized by the effect of force in nature, devoid of a tangible sense of the force itself. At elementary levels, the  $N^{2nd}$  can be expressed mathematically as follows.

$$F = ma \quad (8)$$

Equation (8) can be broken down to the  $N^{1st}$  statement as follows.

$$F = m \left( \frac{v-u}{t} \right) \Rightarrow Ft = mv - mu \quad (9)$$

Where;

$v =$  final motion velocity,  
 $u =$  initial motion velocity,  
 $m =$  mass of the point – particle, and the  $Ft$  leads to the experience of a force due to the point-particle, through a time event.

We can construct two perspectives of the  $N^{1st}$  from Equation (9).

- a. When  $F = 0$ , and  $u = 0$ , then  $v = 0$ , implying that an object (the point-particle in this case) will remain at rest unless a force acts on it.
- b. When  $F = 0$ , then  $v = u$ , and this is a statement of a fraction of the  $N^{1st}$  that in the absence of external forces, an object (say the point-particle) will continue moving with the same velocity.

The  $N^{1st}$  is subject to force based on the  $N^{2nd}$ . Comparing both perspectives to the geometric algorithm in Lemma (1), if the basepoints are the same ( $A \cong O$ ), no construction is possible, as at least two distinct basepoints are needed to initiate the construction. This aligns with the understanding that, in reality, a point-particle cannot exist without a Euclidean space, and similarly, it cannot execute motion in a Euclidean plane without energy or a force driving it. Thus, perspective (a) constitutes an element of the construct of rectilinear motion as outlined in Lemma (1). Conversely, when objects are launched from a common point under the rigor of uniform motion and devoid of external forces, they will consistently follow the same path throughout. This idea aligns with the notion established in Lemma (1), indicating that all straight lines constructed through points  $O$  and  $A$  are parallel and identical geometrically. The proof of Lemma (1) offers comprehensive conditions reflecting situations in the  $N^{1st}$  perspective. Perspective (b) becomes clearer when considering a point-particle moving with uniform instantaneous velocities in a thermodynamic system. Here, the geometric consideration is that instantaneous velocities can be defined as geometric magnitudes, equidistant from two distinct basepoints. Furthermore, the scientific and geometric significance, denoting a non-zero driving force ( $F \neq 0$ ) for the point-particle, operating with two distinct instantaneous geometric magnitudes (velocities in this case) is demonstrated by Definition 10.

#### Example (Application of Lemma 1).

Consider a point-particle initially at rest on a frictionless surface. At time  $t = 0$ , a constant force  $F$  is applied to the point-particle in the positive  $x$  – direction. Using the geometric principles outlined in Lemma 1, determine the position of the point-particle at a given time  $t$ .

#### Solution. Establishing $t$ as a geometric property.

In the geometric framework provided by Lemma 1, time  $t$  can be established as a geometric property through a construction involving straightedge and compass operations. Considering the inherent properties of the geometric construction, we can ensure that  $t$  remains invariant throughout the analysis.

#### Physics interpretation.

Newton’s second law states that the force  $F$  acting on an object is equal to its mass times its acceleration ( $F = ma$ ). In this scenario, since the force  $F$  is constant, the acceleration  $a$  will also be constant. Using the kinematic equation  $x = x_0 + v_0t + \frac{1}{2}at^2$ , where  $x_0$  is the initial position,  $v_0$  is the initial velocity, and  $t$  is the time, we can determine the position of the point-particle at any given time  $t$ .

#### Geometric interpretation.

Lemma 1 establishes the empirical identity property for addition of geometric points. This property ensures that for any point  $A$ ,  $A \oplus O$  is equal to  $A$ , where  $O$  is the origin. In this scenario, we can consider  $O$  as the initial position of the

point-particle, and  $A$  as its position after a certain time  $t$ . Therefore, the displacement of the point-particle ( $A \oplus O$ ) is equal to its final position ( $A$ ), which allows us to compute the final position based on the applied force and time elapsed.

Using the kinematic equation  $x = x_0 + v_0t + \frac{1}{2}at^2$ , and given that the initial velocity ( $v_0 = 0$ ) (since the point-particle starts from rest), we can compute the final position  $x$  of the point-particle at time  $t$  as follows.

$$x = x_0 + \frac{1}{2}at^2 \tag{E1.1}$$

Since the force  $F$  is equal to  $ma$ , we have  $a = \frac{F}{m}$ . Therefore, the equation (E1.1) becomes;

$$x = x_0 + \frac{1}{2}\left(\frac{F}{m}\right)t^2 \tag{E1.2}$$

E1.2 gives us the position of the point-particle at time  $t$ , based on the applied force  $F$ , the mass of the particle  $m$ , and the initial position  $x_0$ .

This solution provides an approach to solving a physics problem using the principles established in Lemma 1, integrating both physics and geometric interpretations to arrive at a solution.

#### 4.4 Geometric scheme for $N^{3st}$

The  $N^{3rd}$  can be conceptualized through directionality notation, and its geometric interpretation aligns with the form defined in Definition 6.

#### Definition 6.

Given an arbitrary origin point  $O$  and two distinct points  $A$  and  $B$  in a Euclidean plane, we define the geometric operation  $A \ominus B$  through;  $A \ominus B \equiv A \oplus (-B)$ .

Lemma (2) shows that the geometric operation  $\ominus$  has the following cancellation property.

#### Lemma 2.

Given a point  $A$ , the geometric operation  $A \ominus B \cong O$  constructs the inverse of the point  $A$  with respect to the geometric operation  $\oplus$ .

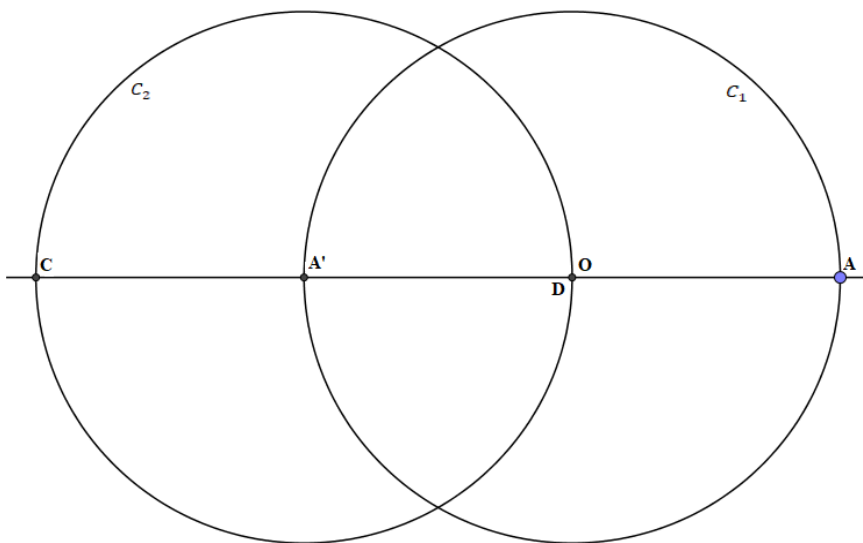
1. If  $A \cong O$ , construct the point  $O$ . Otherwise, proceed through step (2).
2. Construct line  $L_1$  passing the points  $O$  and  $A$ .
3. Construct circle  $C_1$  of radius  $L_1$  centered at the point  $O$ .
4. Construct a point  $A'$ , the intersection of the line  $L_1$  and circle  $C_1$ .
5. Construct circle  $C_2$  of radius  $L_1$  centered at the point  $A'$ .
6. Construct points  $C$  and  $D$ , the intersections of the line  $L_1$  and circle  $C_2$  according to Figure 5.

#### Proof for Lemma (2).

Utilizing the given construction algorithm, we assert the congruence  $\overline{OA} \cong \overline{OA'} \cong \overline{A'D} \cong \overline{A'C} \cong L_1$ . Consequently, by definition, the point  $O$  is geometrically equivalent to the point,  $D$ . Furthermore, circles  $C_1$  and  $C_2$  are congruent, implying that the straight line formed through points  $C$  and  $A'$  passes evenly through points  $O$ ,  $D$ , and,  $A$ . Employing vector notation, the relationship  $A = -A'$  holds, a consequence of the cancellation property. This property, interpretable geometrically as the equality in magnitude between  $OA$  and  $OA'$  (implying the geometric subtraction of the magnitude  $OA$  from itself), definitively establishes the cancellation property in an  $ETIS$ , thereby proving the law.

#### Remark 7.

In Euclidean geometry, the cancellation property applies exclusively to equal magnitudes of similar kinds.



**Figure 5.** Geometric illustration of a cancellation property in a Euclidean Plane. (The figure illustrates the cancellation property in a Euclidean plane based on Lemma (2). Starting with a point  $A$ , the construction proceeds through steps (1) to (5) to create points  $C$  and  $D$ , highlighting the geometric operation  $\ominus$ , which constructs the inverse of the point  $A$  with respect to the geometric operation  $\oplus$ ).

#### 4.4.1 Translation of Lemma (2) to its physics equivalence

The physics concept of cancellation, rooted in equality between similar physical quantities, is applied in dimensions, dimensional analysis, forces, Newton's third law, and various other contexts. Although Euclidean geometry lacks a precise definition of equality, its contextual use aligns exactly with the concept of equality in physics. In the physical perspective, Newton's third law exhibits a cancellation feature expressed as  $q_{1,2} = -q_{2,1}$  (Equation (12)). Thus, Lemma (2), besides being deductive, introduces a distinct aspect of cancellation, allowing the modeling of interactions between point-particles.

#### 4.4.2 Deriving the $N^{3rd}$ from the $N^{2nd}$

Consider two point-particles in a *ETIS* interacting without the influence of external forces. We set the two point-particles  $q_1$  and  $q_2$  interacting in *ETIS*, with enough energy such that  $q_1$  impacts  $q_2$  by a force designated by  $q_{1,2}$ , and  $q_2$  has a responsive equivalent force expressed as  $q_{2,1}$  that acts on  $q_1$ . The rate of change of momentum of  $q_1 = \frac{dp_1}{dt}$  and the rate of change of momentum of  $q_2 = \frac{dp_2}{dt}$ .

Thus, according to  $N^{2nd}$ ,

$$q_{1,2} = \frac{dp_2}{dt} \text{ and } q_{2,1} = \frac{dp_1}{dt} \quad (10)$$

Adding the two in Equations (10) we obtain;

$$q_{1,2} + q_{2,1} = \left( \frac{dp_2}{dt} + \frac{dp_1}{dt} \right) = \frac{d(p_2+p_1)}{dt} \quad (11)$$

In the absence of external forces, interactions between point-particles with charges  $q_1$  and  $q_2$  result in uniform motion, yielding zero change in momentum.

It turns out from Equation (11) that  $\frac{d(p_2+p_1)}{dt} = 0$ , implying that  $q_{1,2} + q_{2,1} = 0$ .

Thus,

$$q_{1,2} = -q_{2,1} \quad (12)$$

Equation (12) is derived  $N^{3rd}$  from  $N^{2nd}$ .

Examining the impact of force on a body, Equation (12) takes on geometric significance in connection with point-particles, particularly within a force field or the *ETIS*. When considering the quantities  $q_{1,2}$  and  $q_{2,1}$  for point-particles in a Euclidean plane, their geometric equivalence points to relations among the points ;  $O$ ,  $D$ ,  $A$  and  $A'$ . This indicates that Equation (12) serves as a physical translation of Lemma (2). Consequently,  $N^{3rd}$  emerges as a fundamentally mathematical concept, supported by a robust geometric proof affirming the inherent validity of the law, even in the absence of experiments.

#### Remark 8.

Mathematical proofs in physics typically rely on assumptions within a physical system. However, the demonstration of the  $N^{1st}$  and the  $N^{3rd}$  reveals that proofs in physics need not always stem from assumptions within a physical setup. Instead, it has been established that proofs in physics can be inherently natural, where assumptions, whether from within or outside a described physical system, hold true regardless of experimental observations. The Euclidean geometric system provides a broad framework for constructing physics proofs by leveraging factual axioms inherent to the system.

#### Example (Application of Lemma 2).

Consider two point-particles,  $q_1$  and  $q_2$ , with charges of  $+2C$  and  $-2C$  respectively, interacting in an isolated system. Use Lemma 2 to determine the magnitude and direction of the force exerted by  $q_1$  on  $q_2$  and vice versa.

#### Solution.

Lemma 2 demonstrates the cancellation property of the geometric operation  $\ominus$ , which constructs the inverse of a point with respect to another point. In this scenario,  $A \ominus B$  constructs the inverse of point  $A$  with respect to the geometric operation  $\oplus$ .

#### Given data

- Charge of  $q_1 = +2C$
- Charge of  $q_2 = -2C$

#### The cancellation property (A geometric scheme).

Lemma 2 establishes that  $A \ominus B$  constructs the inverse of point  $A$  with respect to the operation  $\oplus$ . This property applies to the interaction between point-particles in a Euclidean plane.

#### Contextual proof for Lemma 2.

Utilizing the construction algorithm outlined in Lemma 2, we can demonstrate the cancellation property geometrically. By following the steps outlined in the lemma, we can construct points  $C$  and  $D$ , showcasing the cancellation property of the geometric operation  $\ominus$ .

#### Physics equivalence.

In the physics context, the cancellation property of Lemma 2 applies to the equal and opposite nature of forces between interacting point-particles. The force exerted by  $q_1$  on  $q_2$  ( $F_{1 \rightarrow 2}$ ) is equal in magnitude and opposite in direction to the force exerted by  $q_2$  on  $q_1$  ( $F_{2 \rightarrow 1}$ ).

#### Magnitude of force.

By applying Lemma 2, the force exerted by  $q_1$  on  $q_2$  ( $F_{1 \rightarrow 2}$ ) is equal in magnitude to the force exerted by  $q_2$  on  $q_1$  ( $F_{2 \rightarrow 1}$ ). Thus, the magnitude of ( $F_{1 \rightarrow 2}$ ) is equal to the magnitude of ( $F_{2 \rightarrow 1}$ ).



### Direction of force.

Since  $q_1$  has a positive charge and  $q_2$  has a negative charge, the force exerted by  $q_1$  on  $q_2$  is attractive, directed towards  $q_2$ . Similarly, the force exerted by  $q_2$  on  $q_1$  is attractive, directed towards  $q_1$ .

Using *Lemma 2*, this example has determined that the forces exerted by  $q_1$  and  $q_2$  on each other are equal in magnitude and opposite in direction, consistent with the principles of Newton's third law. Further, the example illustrates how geometric principles can be applied to understand the interactions between point-particles in a physics context.

## 5 The main result-proving the law of energy conservation

This section provides a methodical proof of the Law of Energy Conservation (LEC) through two approaches; classical version and its geometric equivalent.

### 5.1 Proof of the Work-Energy theorem (A classical perspective on the LEC)

This section dives into the Work-Energy Theorem, offering a physical perspective on the Law of Energy Conservation (LEC). It acknowledges the complexity of energy, recognizing both directional and chaotic forms [96]. Examples include organized kinetic energies like mechanical motion and electrical current, contrasted with the chaotic thermal energy of atomic and molecular motion [96]. The paper emphasizes that system energy can be defined based on position within various force fields, such as elastic potential energy, gravitational potential energy, or electromagnetic field energy. It highlights the vast spectrum of energy forms, suggesting even more might be discovered. Here, the focus is not on absolute energy levels but rather on energy changes during a process, from an initial state ( $i$ ) to a final state ( $f$ ). Therefore, zero-point references for different energy forms are irrelevant and often chosen arbitrarily for convenience. The section then provides basic correlations for energy changes in common forms including: kinetic energy  $E_k = KE$  as function of system velocity ( $v$ ); spring elastic potential energy  $E_{ps}$  as function of spring deformation displacement ( $x$ ); gravitational potential energy  $E_{pg} = PE_g$  as function of gravitational elevation ( $z$ ); and sensible thermal energy  $E_u = U$  as function of system temperature ( $T$ ). According to the *LEC*, the different forms of energy can be transformed from one form to the other. This energy transformation hypothesis due to the *LEC* is briefly addressed in a later section of the proof.

#### 5.1.1 Classical formulation of the LEC

Typically, all matter is energy-driven (energy is a characteristic property of matter) [97,98]. Thus going back to the earlier formulation, we adopt the notion of matter for energy by considering an acting system ( $A$ ) that accelerates a responding system ( $R$ ) with average force  $F_A$  along displacement  $d_{AR}$  during mater interaction.

We set,

$$W_{FA} = \int_0^{d_{AR}} F_A ds = \int_0^{d_{AR}} \left( m \frac{dv_R}{dt} \right) ds = \int_0^{d_{AR}} \left\{ m \frac{dv_R}{ds} \left( \frac{ds}{dt} \right) \right\} ds = \int_{V_{R_1}}^{V_{R_2}} m v_R dv_R. \quad \text{This leads to Equation (13).}$$

$$W_{FA} = \frac{1}{2} m \{ V_{R_2}^2 - V_{R_1}^2 \} \quad (13)$$

If we let the quantities  $\frac{1}{2} m V_{R_2}^2$  and  $\frac{1}{2} m V_{R_1}^2$  be the system kinetic energies expressed as  $\frac{1}{2} m V_{R_2}^2 = E_{R_2}$  and  $\frac{1}{2} m V_{R_1}^2 = E_{R_1}$  respectively, then Equation (13) is expressible as:

$$W_{FA} = E_{R_2} - E_{R_1} = \Delta E_R \quad (14)$$

Equation (14) proves the work-energy theorem.

At the same time, the acting system ( $A$ ) will decelerate under the equilibrium reaction force of system ( $R$ ),  $F_R = -F_A$ , along the same displacement,  $d_{AR}$ . Therefore we set;

$$W_{FR} = \int_0^{d_{AR}} F_R ds = \int_0^{d_{AR}} \left( m \frac{dv_A}{dt} \right) ds = \int_0^{d_{AR}} \left\{ m \frac{dv_A}{ds} \left( \frac{ds}{dt} \right) \right\} ds = \int_{V_{A_1}}^{V_{A_2}} m v_A dv_A, \quad \text{leading to Equation (15).}$$

$$W_{FR} = \frac{1}{2} m \{ V_{A_2}^2 - V_{A_1}^2 \} \quad (15)$$

If we let the quantities  $\frac{1}{2} m V_{A_2}^2$  and  $\frac{1}{2} m V_{A_1}^2$  be the system kinetic energies expressed as  $\frac{1}{2} m V_{A_2}^2 = E_{A_2}$  and  $\frac{1}{2} m V_{A_1}^2 = E_{A_1}$  respectively, then Equation (15) is expressible as:

$$W_{FR} = E_{A_2} - E_{A_1} = \Delta E_A \quad (16)$$

$$\int_0^{d_{AR}} (F_R) ds = \int_0^{d_{AR}} (-F_A) ds = -\Delta E_R \quad (17)$$

In classical physics, the above correlation is known as the "work-energy principle" [99]. We extend the work-energy principle to include work of gravitational force and gravitational potential energy as well as elastic spring force and potential elastic spring energy.

$$W_{FA} = \int_0^{d_{AR}} (F_A) ds = \int_{s_1}^{s_2} (Ks) ds = (PE_{R_2} - PE_{R_1}) = (E_{R_2} - E_{R_1}) = \Delta E_R, \quad \text{leading to Equation (18).}$$

$$W_{FA} = \int_0^{d_{AR}} (-F_R) ds = (KE_{A_2} - KE_{A_1}) = (E_{A_2} - E_{A_1}) = -\Delta E_A \quad (18)$$

Therefore, during an interaction between two material particles or systems, the acting system energy will be reduced and transferred in the same amount to the resisting system so that the totality of energy of the two interacting systems is unchanged. It then follows that;

$$\Delta E_A = -\Delta E_R, \quad \text{implying Equation (19).}$$

$$E_{A2} - E_{A1} = -(E_{R2} - E_{R1}) \Rightarrow (E_{A2} + E_{R2}) = (E_{R1} + E_{A1}) = \text{Constant}. \quad (19)$$

Relation (19) is expressible in the form of Equation (20) which puts together; potential energy (being converted to kinetic energy of the falling body), and the total mechanical energy (sum of kinetic and potential mechanical energies) in a free fall configuration. Similarly, the mechanical energy is also conserved if a mass freely vibrates on an ideally elastic spring (generally, in simple harmonic trajectories) in the absence of dissipative effects. In general, for work of conservative forces only, the mechanical energy,  $E_{mech}$ , for  $N$  isolated systems, is conserved since there is no dissipative conversion in thermal energy and thus no heat transfer.

$$E_{mech} = E_K + E_{Pg} + E_{Ps} = \sum_{i=1}^N \left( \frac{1}{2}mv^2 + mgz + kx \right)_i = \text{constant}. \quad (20)$$

Equation (20) offers a generic algebraic expression for interpreting empirical observations due to the energy conservation principle. In regard to Definition 3 and Definition 5, Equation (20) projects a misconception of what an isolated thermodynamics system is. It projects a thermodynamics isolated system as that which corresponds to Definition 1 thus contradicting proposition (1). For consistency throughout the workflow, we restate in the summation operator index ( $N$ );  $\left( \sum_{i=1}^N \left( \frac{1}{2}mv^2 \oplus mgz \oplus kx \right)_i \right)$  such that  $N$  corresponds to the number of point-particles considered from a system of interacting point-particles in an  $TIS$ , rather than having  $TISs$  interacting with each other. This view is based on the consideration that the existence of multiple  $TIS$  suggests the existence of distinct multiple universes, contradicting the earlier clarified geometric characteristic  $ETIS$  (Definition 3).

## 5.2 Establishing geometric principles of the LEC

While there's no single, universally accepted genetic proof for the Law of Energy Conservation (LEC), existing mathematical expressions rely on the general theory of motion for various energy forms [1,99,100]. This section offers a different approach; a natural, observation-independent proof based on geometric principles. The proof translates physical relationships derived from the theory of object motion under applied forces into a geometric framework. It leverages established Euclidean geometric proofs and translates them into Cartesian geometric operations that align with our understanding of object geometries in physics. This approach draws upon René Descartes' work (La Géométrie, 1637) [36], which laid the foundation for Cartesian geometry with its practical applications. Descartes' method demonstrates how arithmetic operations can be constructed geometrically using basic tools like a straightedge and compass. Notably, his work not only solves abstract algebraic equations but also geometric problems translated into algebraic form. The geometric-arithmetic operations of  $G_m$  and  $G_d$  are well founded in the Descartes' scheme. For instance, the  $G_m$  of

two magnitudes can have two characteristic similar operations; a) taking the two magnitudes as straight-line segments ( $l_1$  and  $l_2$ ), the operation  $l_1 G_m l_2$  corresponds to constructing the  $l_1$  at  $l_2$  times. b) Taking  $l_1$  and  $l_2$  as side lengths of a quadrilateral (say rectangle) then the geometric operation  $l_1 G_m l_2$  corresponds to constructing a region bound between the two straight lines. On the other hand, the  $G_d$  operation involves practices such as the geometric bisection of a geometric magnitude, or the  $n$  – sectioning of a given magnitude (very often  $G_d$  operates as the inverse of  $G_m$ ). The succeeding sections concerns operations based on the  $G_m$  of geometric magnitudes, as the  $G_d$  is considered a straightforward exercise whenever desired (to the focus of this paper).

### 5.2.1 Scaling points in the Euclidean plane

We start by defining a way of scaling points in the Euclidean plane with respect to a basepoint,  $O$ , by whole number multiples.

#### Definition 7 (Scaling a point by a whole number multiple with respect to a basepoint).

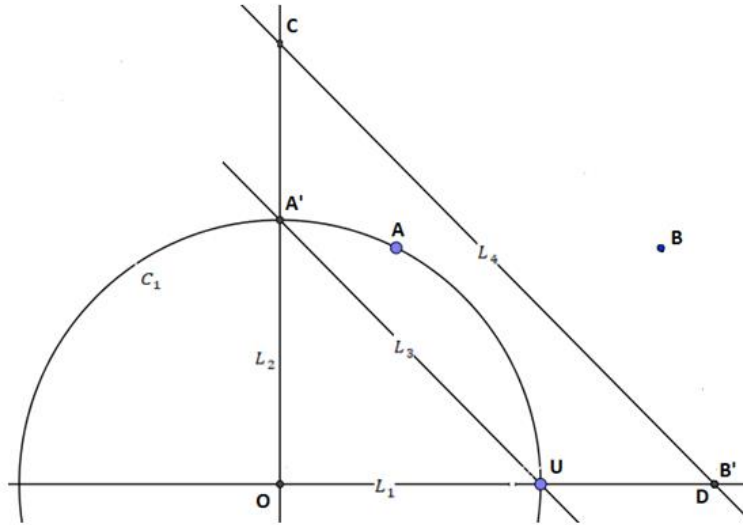
Given a basepoint  $O$ ,  $n \in \mathbb{N}$ , and a point  $A$ , we define the  $n_{th}$  multiple of  $A$  with respect to  $O$ , denoted  $n \odot A$ , inductively by;

- i.  $n \odot A \equiv O$ .
- ii. For  $n > 0$ ,  $n \odot A \equiv ((n - 1) \odot A) \oplus A$ .

Within the Euclidean system, the base operation (i) implies that the basepoint  $O$  and the point  $A$  are exactly the same in a Euclidean plane, and thus, no motion can be experienced. Similarly, the arithmetic operation shows that a sequence of construction cannot be started, as every Euclidean geometric construction stems from two distinct points basepoints. Recursive operation (ii) offers a valid Euclidean geometric statement in that it strictly considers only the positive integers as the rational multiples. Combining these operations conceives a geometric practical extension of the  $\odot$  operation to rational numbers. Genetically, the operations provide a piece of significant geometric machinery for interpreting Equation (20).

#### Definition 8 (Geometric multiplication of a pair of equidistant points $A$ and $B$ relative to a pair of equidistant distinct basepoints $O$ and $U$ ).

We define the geometric multiplication of a pair of equidistant points  $A$  and  $B$  with respect to a pair of equidistant distinct basepoints  $\{O, U\}$ , denoted as  $A \otimes B$  via the following construction beginning from  $\{O, U, A, B\}$ .



**Figure 6.** Geometric multiplication of similar points in a Euclidean plane

1. If  $U \cong O$ , construct the point  $O$ . Otherwise, proceed to step (2).
2. Construct line  $L_1$  through the points  $O$  and  $U$ .
3. Construct line  $L_2$  perpendicular to  $L_1$  through point  $O$ .
4. Construct circle  $C_1$  centered at  $O$  though point  $A$ .
5. Let  $A'$  denote the intersection of  $C_1$  and  $L_2$ .
6. Construct line  $L_3$  passing through the points  $A'$  and  $U$ .
7. Construct the point  $B'$ , a geometric rotation of the point  $B$  onto  $\overline{OU}$  (see appendix 2).
8. Construct line  $L_4$  parallel to line  $L_3$ , through the point  $B'$ .
9. Construct the point  $C$ , the intersection of  $L_2$  and  $L_4$ .
10. Construct the point  $D$ , a geometric rotation of the point  $C$  onto  $\overline{OU}$  (see appendix 2).

**Proof.**

Definition 8 provides a geometric configuration corresponding to the scheme;  $\overline{OA} \cong \overline{UB} \cong \overline{OU} \cong \overline{AB}$ , since the point,  $D$  is a geometric rotation of the point  $C$  (see appendix 2). This is quite a unique feature that can be directly interpreted from algebra as characterizing any quadrilateral. We can deduce from Figure 6 that the point  $D$  is the geometric “product point” and the magnitude  $\overline{OD}$  is the geometric “product”. To complete the proof, we set through the construction; that the point  $A = A'$  implying that  $D = U = B'$ . Since  $U \not\cong O$ , the focus is to show that  $D = U = B'$ . By definition,  $L_4 \parallel L_3$  and following claim 1 (which proves lemma (1)) it has been shown that for two similar and equal-parallel lines through two distinct points in a Euclidean

plane, all their points defining the two parallel lines are geometrically the same.

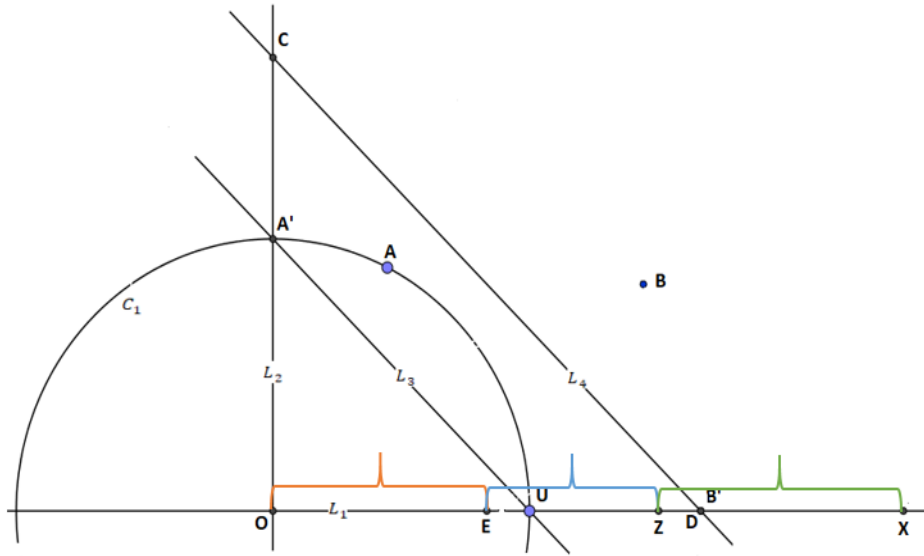
**Translation and the physical interpretation of Definition 8.**

Proceeding from Equation (20), this section asserts and shows that Definition 8 has an important physical relation in physics. We consider the  $i^{th}$  point-particle given a system of point-particles in the ETIS. We let the  $i^{th}$  point-particle be energy driven such that it executes motion useful in describing the energy terms of the form projected in Equation (21). Therefore, characteristically, the  $i^{th}$  point-particle possess kinetic energy expressible as  $\frac{1}{2}mv^2$ , gravitational potential energy expressed by  $mgz$ , and, in a spring system, the  $i^{th}$  point-particle becomes an element of the spring experiencing motion leading to the energy term  $kx$ .

$$E_{mech} = \sum_{i=1}^N \left( \frac{1}{2}mv^2 + mgz + kx \right)_i = constant \quad (21)$$

To reduce Equation (21), we make two assumptions; a) in distinct field settings, the mass of the  $i^{th}$  point-particle remains constant, and so we set  $m$ ,  $g$ , and  $k$  as non-geometric constants (scalars). b) The three constants  $m$ ,  $g$ , and  $k$  only correspond to positive real number integers (let these constants be the scaling multiples for the inherent geometric operations). The deduction reduces Equation (21) for the  $i^{th}$  point-particle, to its geometric equivalence in Equation (22).

$$E_{mech} = \sum_{i=1}^N \left( \frac{1}{2}v^2 \oplus z \oplus x \right)_i = constant \quad (22)$$



**Figure 7.** Geometric proof of the *LEC* in a *ETIS* for the  $i^{th}$  point-particle

The quantities  $v^2$ ,  $z$ , and  $x$  have a significant geometric essence. Considerably, the quantity  $v^2$  corresponds to a  $G_m$  operation on two equal and similar magnitudes expressible as  $v \otimes v$ . In regard to the aim of this proof, we will consider the quantity  $v$  for a straight line segment between two distinct points, in a Euclidean plane. Following this perspective, we apply the  $G_d$  operation (corresponding to straightedge and compass sectioning of a straight line) to scale down the geometric operation ( $v \otimes v$ ) to  $\frac{1}{2}(v \otimes v)$ . We then consider the quantities  $z$  and  $k$  as straight line segments geometrically put together with the magnitude  $\frac{1}{2}(v \otimes v)$  through the following straightedge and compass algorithm.

1. If  $U \cong O$ , construct the point  $O$ . Otherwise, proceed to step (2).
2. Construct line  $L_1$  through the points  $O$  and  $U$ .
3. Construct line  $L_2$  perpendicular to  $L_1$  through point  $O$ .
4. Construct circle  $C_1$  centered at the point  $O$  though point  $A$ .
5. Let the point  $A'$  denote the intersection of  $C_1$  and  $L_2$ .
6. Construct line  $L_3$  passing through the points  $A'$  and  $U$ .
7. Construct the point  $B'$ , a geometric rotation of the point  $B$  onto  $\overline{OU}$  (see appendix 2).
8. Construct line  $L_4$  parallel to line  $L_3$ , through the point  $B'$ .
9. Construct the point  $C$ , the intersection of  $L_2$  and  $L_4$ .

10. Construct the point  $D$ , a geometric rotation of the point  $C$  onto  $\overline{OU}$  (see appendix 2).
11. Construct the point  $E$ , the bisection pint of  $\overline{OD}$ .
12. Construct the circle  $C_2$  centered at the point  $E$  and radius  $\overline{OZ}$ , to the side of point  $E$ .
13. Let the point  $Z$  denote the intersection of  $C_2$  and  $L_1$ .
14. Construct the circle  $C_3$  centered at the point  $Z$  and radius  $\overline{OX}$ , to the side of point  $Z$ .
15. Let the point  $X$  denote the intersection of  $C_3$  and  $L_1$ .

The circles  $C_2$  and  $C_3$  can be stifled after obtaining the magnitudes  $\overline{EZ}$  and  $\overline{ZX}$ , according to Figure 7.

**Proof.** Following Definition 8,  $\overline{OD} = (v \otimes v)$  (proven). Therefore by definition,  $\overline{OE} = \frac{1}{2}(v \otimes v)$ . Further, given a Euclidean plane, a straight line segment can always be extended using straightedge-compass constructions [43]. Thus, it is geometrically possible to put together the three magnitudes  $\overline{OE}$ ,  $\overline{EZ}$  and  $\overline{ZX}$  such that;

$$(\overline{OE} \oplus \overline{EZ} \oplus \overline{ZX}) \cong \overline{OX}. \text{ Therefore, the } LEC \text{ (Equations (20, 21, and 22)) is proven.} \quad (23)$$

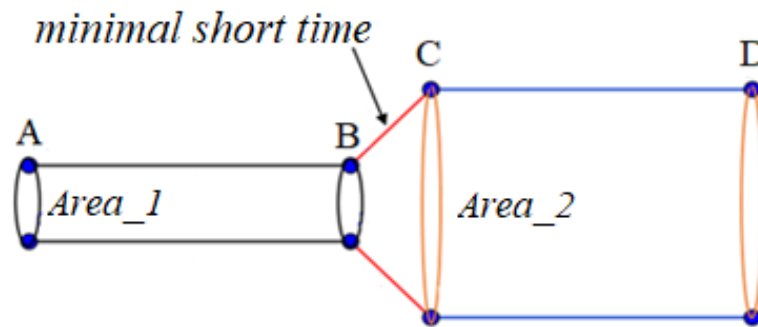
Equation (23) is inherently geometric, and its evaluation reflects the fundamental principles of Euclidean constructions. Throughout the paper, we have assumed that every Euclidean operation requires two distinct points. If points coincide, the operation becomes undefined. This concept translates directly to the energy equation's segments, which represent geometric magnitudes. The magnitude  $\overline{OE}$  is the kinetic energy term which implies that the  $i^{th}$  point-particle must execute motion between two distinct points in

a Euclidean space. Otherwise, the kinetic energy term does not exist. The magnitude  $\overline{E\bar{Z}}$  defines the gravitational potential energy due to the motion of the  $i^{th}$  point-particle from some height above the Euclidean plane (virtually in reference to the earth's surface). So similarly, the magnitude  $\overline{E\bar{Z}}$  is only constructible between two distinct points. Lastly, the magnitude  $\overline{Z\bar{X}}$  corresponds to the energy possessed by an element of a spring (the  $i^{th}$  point-particle) in motion due to a spring extended between two distinct points. Practically (this is not part of the proof but an illustration), taking  $U \cong 0$  results to  $\overline{O\bar{E}} \cong 0$ , hence validating the assumption that for a valid geometric construction corresponding to a physical relationship in a Euclidean space,  $U \neq 0$ . This proof demonstrates that the LEC can be derived logically from self-evident geometric principles within the Euclidean system, independent of experimental observations. The paper argues that considering the LEC "unprovable" is an oversight. Rather, it reflects a lack of exploration at the intersection of physics and geometry, where both inductive and deductive reasoning can be applied.

### 5.3 Exploring the possibility of breaking the law of energy conservation

This section introduces an unconventional perspective on the potential violation of the Law of Energy Conservation (LEC), focusing on phenomena within classical systems rather than the conventional development of a Perpetual Motion Machine (PMM). The approach theorizes a specific, practical model of an electrical short circuit as an example of an anomalous event capable of challenging traditional interpretations of energy conservation. Unlike models grounded in abstract notions or "nothingness", the proposed framework relies on physical quantities conceptualized as point particles. The primary objective is to illustrate how a transient event, such as a short circuit, can evolve into a steady-state system while maintaining coherence with geometric principles. The analysis redefines the perception of short circuits, which are traditionally considered transient

phenomena characterized by significant energy dissipation as heat and governed by internal resistances and potential differences. Instead, this framework establishes a steady-state model for short circuits, using unconventional circuit representations. These models highlight the possibility of higher current magnitudes arising in steady-state conditions without adhering strictly to anomaly-free interpretations. The aim is to shift the discussion toward a structured and investigable domain where short circuits serve as critical cases for re-evaluating the scope of the LEC. Experimental validation of such steady-state behaviors is acknowledged as a significant challenge, requiring tools and methodologies that extend beyond the current scope of physics. While this paper limits itself to theoretical proofs and geometric modeling, ongoing research aims to develop experimental setups capable of measuring, analyzing, and applying electrical quantities such as current, voltage, and resistance during short circuit events. These efforts will be presented in separate publications to complement the theoretical framework outlined here. Section 2 identified the limitations of modern physics in addressing chaotic systems like short circuits, particularly in defining energy conservation under such conditions. The inability to provide absolute clarity on the LEC in these scenarios raises questions about whether the principle is universally applicable. This section explores those questions by examining the theoretical feasibility and underlying motivations for potential violations of the LEC. The discussion also aims to clarify misconceptions about the principle, often fueled by growing energy demands and a limited understanding of its boundaries. The notion of introducing a new element termed the "Chaotic Magnitude" into the governing equations of energy conservation (Equations 21 and 22) is proposed as a way to address these challenges. While not formally proven, this element is supported by physical principles and geometric axioms, offering a conceptual extension of the LEC. Figure 8 demonstrates the application of this concept in an electrical short circuit, emphasizing its potential to refine our understanding of energy conservation.



**Figure 8.** Geometric Interpretation of Electrical Short Circuit in Ordered and Chaotic States. (This figure illustrates the electric current flow within a conductor  $\overline{AD}$  in two distinct states: ordered and chaotic. The ordered flow is represented in section  $\overline{AB}$ , while the chaotic short circuit is depicted in section  $\overline{CD}$ . The region  $\overline{BC}$  marks the critical transition from ordered to chaotic current flow, identified as the "minimal short time", an interval during which the system undergoes a shift. The figure encapsulates the steady-state mode of the short circuit, challenging conventional models that assume zero resistance or voltage during such events. The diagram serves as a basis for understanding the short circuit as a dynamic phenomenon that can be explored for its potential in energy generation).

Figure 8 presents a detailed model of the electric current flow in two distinct scenarios within a conductor labeled  $\overline{AD}$ . The section  $\overline{AB}$  of the conductor represents an ordered, regular flow of current, while the section  $\overline{CD}$  corresponds to the chaotic state induced by the occurrence of a short circuit. The region  $\overline{BC}$ , positioned between  $\overline{AD}$  and  $\overline{CD}$ , represents the transition from the ordered state to the chaotic flow. This region marks a critical point in the evolution of the short circuit and is referred to as the “minimal short time”, an interval during which the system undergoes a shift from ordered to chaotic current flow. The conductor’s stability is assumed to support both energy flows and a constant energy source, ensuring that no additional external power input interferences disrupt the constant chaotic flow through  $\overline{CD}$ . Short circuits, whether intentional or unintentional, are integral to various applications, including power protection system design and the determination of protective device capacities [101-104]. Unintentional short circuits frequently arise in power circuits, highlighting the practical relevance of understanding their dynamics. The transition from ordered to chaotic current flow, represented by  $\overline{BC}$ , is thus defined by the elemental magnitude of the “minimal short time”, a key parameter for studying the phenomenon. Traditional models assume that the “minimal short time” is associated with negligible conductor resistance, often treated as zero in theoretical models. However, this assumption is rigorously challenged in this paper. Contrary to the assumption of zero resistance, the argument here is that electrical resistance cannot be zero during a short circuit. This insight is expanded upon in separate work that addresses experimental models for the “minimal short time” and explores the behavior of quantities such as current, voltage, and resistance during electrical short circuits. To derive a basic formulation for an electrical short circuit, the current expression from Ohm’s Law is employed. Previous sections established that motion-energy processes occur strictly between distinct spatial points, prompting an inquiry into the practical and theoretical validity of applying Ohm’s law in this context. Specifically, this exploration critically examines the claim that electrical resistance, denoted as  $R$ , can be zero for a given conductor. Through this investigation, the paper aims to demonstrate the potential benefits of utilizing electrical short circuits not merely as hazardous occurrences, but as mechanisms for energy generation, offering new insights into their practical applications. The electrical current formulation derived from Ohm’s law is presented in Equation (24), providing the foundation for the subsequent analysis.

$$I = \frac{V}{R} \quad (24)$$

In the ideal form, Equation (24) implies that;

$$I = \frac{V}{0} = \infty \quad (25)$$

Equation (25) suggests the possibility of obtaining an infinite quantity from a finite physical relation(s). The subsequent discussion concerns objecting to this view. It also

establishes an intelligible objection to the possibility of the mathematical relation for electrical resistance in a conductor as,  $R = 0$ .

The genetic definition of electrical resistance is presented in Equation (26):

$$R = \rho \frac{L}{A} \quad (26)$$

where  $\rho$  denotes the material resistivity,  $L$  represents the conductor length, and  $A$  is the cross-sectional area.

To critically examine the notion  $R = 0$ , two hypothetical experiential instances are proposed for analysis.

**Premise 1 (When  $L = 0 \Rightarrow A = 0$ ).**

We start by opening up the expression for  $A$ ;  $A = \pi r^2$ .  $A$  has a geometrical property of the conductor and so we can relate  $L$  to  $r$  such that; when  $L = 0$ ,  $r = 0$  implying the existence of electrical conductors without cross-sectional areas in their geometries. This results to a typical mathematical string that gives the quite strange observation projected in Equation (27).

$$R = \rho \frac{0}{0} = \infty \quad (27)$$

Equation (27) illustrates that if the relations  $L = r = 0$  possibly existed, then the conductor’s electrical resistance would be infinitely ever large, and not zero. This is obscure enough since we cannot have infinitely large electrical resistance without the electrical conductor. However, the equation could have a simplified reinterpretation as; in the case of an open circuit, resistance tends to  $\infty$  as it is assumed in the studies on electrical voltage and current using Norton-Thevenin relations [105,106]. Note that genetically, Equation (27) rightfully implies that the geometries of the conductor influence its electrical resistance, and this paper completely subscribes to this view.

**Premise 2 (When either  $\rho = 0$ ).**

Setting  $\rho = 0$  in Equation (26) we end up with  $R = 0$ . This seems scientifically sensible. However, this paper asserts that the expression  $R = 0$  offers quite an ambiguous physical relation and a highly refutable observation since  $\rho$  is a genetic property of the electrical conductor. Therefore, the  $\rho = 0$  denotes an electrical conductor free of resistivity property or the material, and it is known that such a material cannot practically exist. Ensuing these deductions, it is judicious to opine conclusively that material resistance equals zero only when there is no conducting material or in the absence of voltage and current source (reasonably, because any power source will have some resistance as studied in the Norton-Thevenin concepts [106]).

Premises (1 and 2) categorically reject the possibility of the relation  $R = 0$ , both theoretically and practically. Therefore, asserting  $R = 0$  reflects a fundamental misunderstanding of the nature of an electrical short circuit. Equations (24-27) demonstrate that Ohm’s law imparts understandable geometrical properties to electrical

conductors, precluding the possibility of  $R = 0$ . In the following section, we will explore a condition of very low electrical resistance in a conductor, using this concept to illustrate the perpetual breach of the *LEC* in both physical and theoretical contexts.

#### 5.4 A geometric projection to breaking the *LEC*

This section aims to establish a geometric perspective defining theoretical and physical models targeting the violation of the *LEC*. Within a population of point-particles, denoted as  $i^{th}$ , exemplified by the transition of electric charges from an ordered to chaotic state through a conductor, we designate two instantaneous velocities:  $v_o$  for ordered current flow and  $v_c$  for chaotic current flow. Throughout, we assume that during ordered current flow, point-particles move uniformly at an instantaneous velocity magnitude,  $v_o$ . Conversely, in the case of a short circuit (maintaining constant conductor geometries), we assume an increase in electric field strength between interacting point-particles, intensifying force interactions due to uniformly charged particles, resulting in stronger repulsive forces. We assume that an increase in repulsive force strengths corresponds to an increase in the strengths of electric fields, leading to an enhanced flow of the respective electric fields through the conductor. The velocity,  $v_c$ , of interacting point-particles increases with higher speeds of the interacting fields. The geometric projection of this phenomenon necessitates the use of instantaneous velocity magnitudes between the ordered and chaotic sections of the current flow process. We proceed by considering the velocity magnitudes for both  $v_o$  and  $v_c$  for the  $i^{th}$  point-particle through the ordered and chaotic sections of the flow, denoting them as geometric relations  $\overline{OA}_o \cong v_o$  for the ordered velocity magnitude and  $\overline{OB}_c \cong v_c$  for the chaotic velocity magnitude, both taken from a fixed point  $O$ . Once explicitly defined, the sub-scripts  $o$  and  $c$  on the magnitudes  $\overline{OA}_o$  and  $\overline{OB}_c$  will be omitted throughout the workflow. The geometric solutions will involve two schemes concerning the basepoints  $O$  and  $U$  in a Euclidean plane, as per [Definition 10](#).

#### Definition 9 (Chaotic Magnitude).

Here, a Chaotic Magnitude is defined as a physical quantity that cannot be discerned using standard scales of physics. These magnitudes arise in anomalous processes and may encompass velocities, forces, or energies experienced by charged particles, such as those in an electrical short circuit.

#### Remark 9.

The defined chaotic velocity  $v_c$  serves as a illustrative instance of the mentioned chaotic magnitude.

#### Chaotic kinetic energy.

[Definition 8](#) demonstrates the geometric squaring of ordered instantaneous velocities, denoted as  $v_o$ . In this section, the aim is to expand [Equations \(21\) and \(22\)](#) by introducing a corresponding instantaneous velocity,  $v_c$ , for chaotic flow. The quantities  $v_o$  and  $v_c$  will then be combined geometrically, employing operations bridging classical

physics and relativity. Despite limited knowledge of chaos in classical physics, studies indicate its prevalence [\[96,107,108\]](#). To establish chaotic kinetic energy on a Newtonian scale, this section initiates by illustrating that chaotic flows can occur within the framework of classical physics, dependent on the velocities of the moving bodies. Although the velocities driving chaotic bodies are not fully understood, we assume that the considered point-particles in chaotic flows move at speeds less than the speed of light.

#### Remark 10.

Significantly, for a body moving at a fraction of the speed of light, employing relativistic mechanics is sensible for calculating its kinetic energy. This enhanced kinetic energy, termed chaotic kinetic energy in this paper, results from such speeds. In the context of special relativity theory, modifications to the expression for linear momentum are introduced, with  $m$  representing the object's rest mass,  $v$  denoting its velocity, and  $c$  indicating the speed of light in a vacuum.

We then apply the expression for linear momentum;

$$p = m\gamma v \tag{28}$$

$$\text{where the quantity } \gamma = \frac{1}{\sqrt{1-\frac{v^2}{c^2}}}$$

Applying the integration by parts we obtain;

$$E_k = \int v \cdot dp = \int v \cdot d(m\gamma v) = m\gamma v \cdot v - \int m\gamma v \cdot dv = m\gamma v^2 - \frac{m}{2} \int \gamma d(v^2) \tag{29}$$

$$\text{Having previously defined the quantity } \gamma = \frac{1}{\sqrt{1-\frac{v^2}{c^2}}}$$

$$E_k = m\gamma v^2 - \frac{-mc^2}{2} \int \gamma d\left(1 - \frac{v^2}{c^2}\right)$$

$$E_k = m\gamma v^2 + mc^2 \left(1 - \frac{v^2}{c^2}\right)^{1/2} - E_0 \tag{30}$$

And  $E_0$  is a constant of integration for the indefinite integral.

Simplifying the expression [Equation \(30\)](#) reduces to;

$$E_k = m\gamma \left( v^2 + c^2 \left(1 - \frac{v^2}{c^2}\right) \right) - E_0$$

$$E_k = m\gamma(v^2 + c^2 - v^2) - E_0$$

$$E_k = m\gamma c^2 - E_0 \tag{31}$$

Where  $E_0$  is found to obey  $v = 0$ ,  $\gamma = 1$ ,  $E_k = 0$ , resulting to;

$$E_0 = mc^2 \tag{32}$$

Proceeding from Equation (32), following this relation we have;

$$E_k = \gamma mc^2 - mc^2 = \frac{mc^2}{\sqrt{1-\frac{v^2}{c^2}}} - mc^2 = (\gamma - 1)mc^2 \quad (33)$$

Equation (33) illustrates that as speed approaches the speed of light, the work needed to accelerate an object from rest approaches infinity. The implication, discussed in detail in a separate article, leads us to assume that no object can exceed the speed of light limits. This computation results in the mass-energy equivalence formula, asserting that a body at rest must possess energy content.

$$E_{rest} = E_0 = mc^2 \quad (34)$$

From a Newtonian perspective, the classical kinetic energy actually approximates the relativistic kinetic energy at low speeds ( $v \ll c$ ). Therefore, we assume that this condition is observed in this intuitionistic-contextual deduction. We then employ use of the Taylor expansion on the first two terms or a binomial approximation to get the reciprocal square root, as follows;

$$E_k \approx mc^2 \left(1 - \frac{1}{2} \frac{v^2}{c^2}\right)^{\frac{1}{2}} - mc^2 = \frac{1}{2}mv^2 \quad (35)$$

Equation (35) shows that the total energy  $E_k$  can be partitioned into the rest mass energy plus the Newtonian kinetic energy at low speeds. The energy expression  $\frac{1}{2}mv^2$  resulting from the computation will be considered the chaotic kinetic energy expressed as  $\frac{1}{2}mv_c^2$  through the proof.

### Relationship between ordered and chaotic kinetic energies.

Here, we establish an abstract relationship between the stated chaotic velocity and the ordered velocity based on simple kinetic energy formulation. Kinetic energy is the energy of motion of a mass (so it is not always that a motion starts from a rest state). From physics understanding, velocity is the displacement covered by the body in motion, scaled by the time required to cover the displacement. Denoting the change in displacement as  $\Delta d$  and a change in time through the displacement as  $\Delta t$ , we can define average velocity according to Equation (36).

$$v_{av} = \frac{\Delta d}{\Delta t} \quad (36)$$

From Equation (36) we can then define average acceleration as follows;

$$a_{av} = \frac{\Delta v}{\Delta t} \quad (37)$$

We redefine Equation (8) to average force using Equation (37).

$$F_{av} = ma_{av} = m \left(\frac{\Delta v}{\Delta t}\right) \quad (38)$$

Thus in the time  $\Delta t$  the object is displaced some magnitude  $\Delta d$ . We recall the assumption that the motions throughout the paper are free of external forces, and consider the sort of motion in which the mass  $m$  moves in the direction of the force.

We then compute the work done in this situation as follows;

$$W = F_{av}\Delta d = m \left(\frac{\Delta v}{\Delta t}\right) \Delta d \quad (39)$$

We consider a motion situation that starts with some velocity  $v_b$  and ends with velocity  $v_a$ .

It then follows from Equation (39) that;

$$W = F_{av}\Delta d = m \left(\frac{v_a - v_b}{\Delta t}\right) \Delta d \quad (40)$$

By definition,

$$\Delta d = (v_{av} \times \Delta t) \Rightarrow \Delta d = \frac{1}{2}(v_a + v_b)\Delta t \quad (41)$$

Using Equation (41) in Equation (40) we obtain;

$$W = F_{av}\Delta d = m \left(\frac{v_a - v_b}{\Delta t}\right) \left(\frac{1}{2}(v_a + v_b)\Delta t\right) \Rightarrow W = \frac{1}{2}m(v_a - v_b)(v_a + v_b) \quad (42)$$

$$W = \frac{1}{2}m(v_a^2 - v_b^2) \quad (43)$$

Equation (43) is a consequence of motion due to a body with sort of mass  $m$  that is moving at two distinct velocities.

Ordinarily, the quantity  $v_b$  is assumed to be zero ( $v_b = 0$ ) and thus Equation (43) is reducible to the kinetic energy Equation in (44).

$$K_E = W = \frac{1}{2}mv_a^2 \Rightarrow K_E = \frac{1}{2}mv_a^2 \quad (44)$$

However, following Figure 8, Equation (43) holds as ( $v_b \neq 0$ ). So reasonably, Equation (43) can be related to the chaotic kinetic energy and rewritten to Equation (45).

$$E_k = \frac{1}{2}m(v_c^2 - v_0^2) \quad (45)$$

Equation (45) puts together both the ordered and the chaotic velocities and the corresponding kinetic energies. The equation is geometrically established following proposition 2.

### Proposition 2.

In a classical system involving both ordered and chaotic kinetic energy flows, the Law of Energy Conservation is violated when the chaotic kinetic energy exceeds the ordered kinetic energy according to the geometric formulation of chaotic and ordered velocities and their corresponding



kinetic energies. Specifically, when the geometric difference between the squares of chaotic and ordered velocity magnitudes is non-zero, energy is not conserved.

Proposition (2) will be proven following Definition 10.

**Definition 10 (Geometric difference between the squares of chaotic and ordered magnitudes with respect to distinct basepoints  $O$  and  $U$ ).**

Consider the geometric product of a pair of distinct equidistant points  $A$  and  $B$  with respect to a pair of distinct basepoints  $\{O, U\}$ , and, a geometric product of a pair of distinct points  $E$  and  $F$  equidistant from and with respect the pair of distinct basepoints  $\{O, U\}$ , defined via the following construction algorithm beginning from  $\{O, U, A, B\} \subseteq \{O, U, E, F\}$ .

1. If  $U \cong O$ , construct the point  $O$ . Otherwise, proceed to step (2).
2. Construct line  $L_1$  through the points  $O$  and  $U$ .
3. Construct line  $L_2$  perpendicular to  $L_1$  through the point  $O$ .
4. Construct circle  $C_1$  centered at the point  $O$  though point  $A$ .
5. Let the point  $A'$  denote the intersection of  $C_1$  and  $L_2$ .
6. Let the point  $N$  denote the intersection of  $C_1$  and  $L_1$ .
7. Construct line  $L_3$  passing through the points  $A'$  and  $U$ .
8. Construct the point  $B'$ , a geometric rotation of the point  $B$  onto  $\overline{OU}$  (see appendix 2).
9. Construct line  $L_4$  parallel to line  $L_3$ , through point  $B'$ .
10. Construct the point  $C$ , at the intersection of  $L_2$  and  $L_4$ .
11. Construct the point  $D$ , a geometric rotation of the point  $C$  onto  $\overline{OU}$  (following appendix 2, let  $C_2$  denote the rotation configuration).
12. Construct circle  $C_3$  centered at the point  $U$  of radius  $\overline{ND}$ .
13. Let the point  $N'$  denote the intersection of  $C_3$  and  $L_4$ , from the point  $C$ .
14. Construct circle  $C_4$  centered at the point  $O$  though point  $E$ .
15. Construct the point  $E'$ , the intersection of  $C_4$  and  $L_2$ .
16. Construct line  $L_5$  passing through the points  $E'$  and  $U$ .
17. Construct the point  $F'$ , a geometric rotation of the point  $F$  onto  $\overline{OU}$  on the side of point  $U$  (see appendix 2).
18. Construct line  $L_6$  parallel to line  $L_5$ , through the point  $F'$ .
19. Construct the point  $G$ , the intersection of  $L_2$  and  $L_6$ .
20. Construct the point  $H$ , a geometric rotation of the point  $G$  onto  $\overline{OU}$  on the side of point  $U$  (following appendix 2, let the circle circumference  $C_5$  denote the rotation configuration).
21. Construct circle  $C_6$  centered at the point  $U$  of radius  $\overline{E'G}$ .
22. Let the point  $P'$  denote the intersection of  $C_6$  and  $L_6$ , from the point  $G$ .

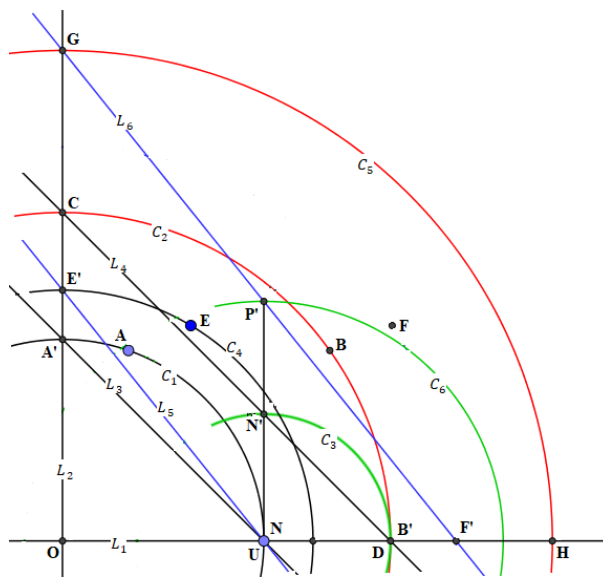


Figure 9. The Energy Conservation Revision Scheme

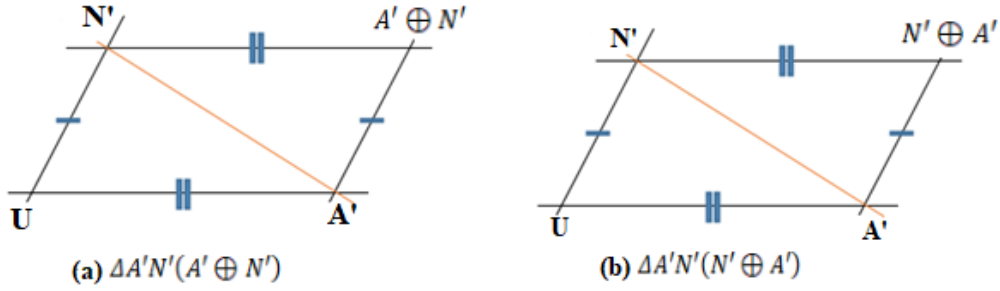


Figure 10. Geometric proof for Claim 2

**Claim 2.**

The circle  $C_3$  intersects  $L_4$  through point  $N'$ , implying that the lines  $\overline{UN'} \cong \overline{A'C}$  and,  $\overline{UA'} \cong \overline{N'C}$ .

**Proof.**

Considering the quadrilateral  $UN'CA'U$  in Figure 9 we can extract Figure 10 according following deductions.

We set the point  $C$  corresponding to the point  $N' \oplus A'$  in the diagram (a), Figure 10 and in a distinct view, we let the point  $C$  correspond to  $A' \oplus N'$  according to diagram (b), Figure 10.

Starting with Figure 9, since  $\overline{ND} \cong \overline{A'C}$  (corresponding to  $\overline{UN'} \cong \overline{A'(A' \oplus N')}$  in the diagram (a) and  $\overline{UN'} \cong \overline{A'(N' \oplus A')}$  in the diagram (b) of Figure 10), we deduce from Figure 10 that  $\overline{UN'} \parallel \overline{A'(A' \oplus N')}$ ,  $\overline{UA'} \parallel \overline{N'(A' \oplus N')}$  for diagram (a). Similarly,  $\overline{UN'} \parallel \overline{A'(N' \oplus A')}$ ,  $\overline{UA'} \parallel \overline{N'(N' \oplus A')}$  for diagram (b). The geometric consequence of these deductions is congruence expressed as  $\Delta A'N'(A' \oplus N') \cong \Delta A'N'(N' \oplus A')$ . The two congruent triangles  $\Delta A'N'(A' \oplus N')$  and  $\Delta A'N'(N' \oplus A')$  share two points ( $A'$  and  $N'$ ) such that the third points lie on the side of  $\overline{A'N'}$ . It can be shown through the following deductions that the thirds points are equidistance from  $\overline{A'N'}$ .

Starting with  $\Delta A'UN'$ , we set the angles;

$$\angle UA'N' = \alpha \text{ and } \angle UN'A' = \theta \tag{46}$$

It then follows that

$$\angle A'UN' = \pi - (\alpha + \theta) \tag{47}$$

(Angles sum in a triangle)

We now focus on  $\Delta A'N'(A' \oplus N')$ , in the diagram (a) of Figure 10.

$$\angle N'A'(A' \oplus N') = \theta, \text{ and the } \angle A'N'(A' \oplus N') = \alpha \tag{48}$$

(alternate angles to  $\angle UN'A'$  and  $\angle UA'N'$  respectively).

Therefore,

$$\angle A'(A' \oplus N')N' = \pi - (\alpha + \theta), \tag{49}$$

(Angles sum in a triangle)

Next, we consider  $\Delta A'N'(N' \oplus A')$  in diagram (b) of Figure 10.

$$\angle N'A'(N' \oplus A') = \theta \text{ and the } \angle A'N'(N' \oplus A') = \alpha \tag{50}$$

(alternate angles to  $\angle OBA$  and  $\angle OAB$  respectively).

Therefore,

$$\angle A'(N' \oplus A')N' = \pi - (\alpha + \theta), \tag{51}$$

(Angles sum in a triangle)

Since,

$$\angle A'(A' \oplus N')N' = \angle A'(N' \oplus A')N', \quad \overline{UN'} \parallel \overline{A'(A' \oplus N')}$$

and  $\overline{UN'} \parallel \overline{A'(N' \oplus A')}$ , implying that;

$$\overline{UN'} = \overline{A'(A' \oplus N')}. \tag{52}$$

A very significant consequence of statement (52) is that; in allusion to Figure 9, the equation leads to a rigorous Euclidean geometric fact based on the theory of similar triangles. Comparing  $\Delta COB'$  and  $\Delta N'UB'$ , it is geometrically reasonable to assert that  $\frac{OC}{UN'} \cong \frac{OB'}{UB'}$ , implying that  $\Delta COB' \cong \Delta N'UB'$  (due to a similarity property on SAS). Similarly, by the provided construction, the proof for claim 2 is inductively equally deducible for the quadrilateral  $GE'UP'G$ . Hence Definition 10 is proven. The analytical benefits of Definition 10 are elaborated in the following section.

**6 Discussion**

The proof for Definition 10 concludes the intended perspective on the LEC within the paper's scope. However, the bisection of product lines  $\overline{OD}$  and  $\overline{OH}$  is not explicitly addressed in the proof. The primary objective was to demonstrate the derivation of the difference between the squares of the magnitudes  $v_c$  and  $v_o$ . It is asserted inductively that bisecting the product lines  $\overline{OD}$  and  $\overline{OH}$  yields bisection points that exhibit behavior analogous to points  $D$  and  $H$  in the experimental framework for both  $v_c$  and  $v_o$ , given that  $\overline{OD} \subseteq \overline{OH}$ . There is no inconsistency in performing these bisection operations to establish a relationship akin to the projection in Equation (23). Consequently, Equation (23) can be reformulated as follows: Let  $E$  denote the bisection point of the product  $\overline{OD}$ , and let  $J$  represent the bisection point of the product  $\overline{OH}$ . This allows rewriting Equation (23),

$(\overline{OE} \oplus \overline{EZ} \oplus \overline{ZX}) \cong \overline{OX}$ ) as;  $([\overline{OJ} - \overline{OE}] \oplus \overline{EZ} \oplus \overline{ZX}) \cong \overline{OX}$ ). In the context of the electrical short circuit example applied to electrical energy models, the difference  $([\overline{OJ} - \overline{OE}])$  is anticipated to consistently result in a positive magnitude. The methodology for measuring electrical short circuit current based on a given circuit power input is addressed in a separate article that focuses on experimental investigations. **Definition 10** provides both natural and experimental geometric interpretations of the relationship between the magnitudes  $(v_c^2 - v_o^2)$  in **Equation (45)**, as outlined in Claim 2. This section focuses on expanding the established proofs for the Law of Energy Conservation (LEC) from two perspectives: the validity and limitations of the LEC statement and the potential for its practical violation. The geometric proof associated with **Equation (45)** suggests that energy-driven systems do not always initiate motion from rest or zero-velocity conditions. **Equation (45)** finds practical application in scenarios such as electrical short circuits, as illustrated in **Figure 8**, where the point particles under consideration exhibit distinct instantaneous velocities. The first phase of the proof for **Definition 10** concerns the geometric multiplication of two distinct points ( $A$  and  $B$ ), equidistant from given two distinct basepoints ( $O$  and  $U$ ), to  $\overline{OU}$ . These operations can be translated to the geometric multiplication of two equal magnitudes so that we have the relations  $\overline{OA} \cong v_o$  and  $\overline{OB} \cong v_o$  geometrically put together such that  $(\overline{OA} \otimes \overline{OB}) \cong v_o^2$  when the point-particle is executing discernible kind of motion (we name this kind of discernible motion the ordered motion and the associated quantities, ordered quantities (magnitudes) as mentioned earlier, for  $v_o$ ). In this configuration,  $\overline{OA} \cong \overline{AB} \cong \overline{BU} \cong \overline{OU}$ . The second segment in the proof for **Definition 10** involves the geometric multiplication of two distinct points ( $E$  and  $F$ ) taken equidistant from the two distinct basepoints ( $O$  and  $U$ ) such that  $\overline{OH} \cong \overline{UF} \not\cong \overline{OU}$ , with no restrictions to the basepoints condition, provided  $(\overline{OA} \cong \overline{AB} \cong \overline{BU} \cong \overline{OU}) \not\cong (\overline{OH} \cong \overline{UF})$ . Likewise, we translate the geometric relations  $\overline{OH} \cong v_c$  and  $\overline{OF} \cong v_c$  geometrically put together such that  $(\overline{OH} \otimes \overline{OF}) \cong v_c^2$  when the point-particle is executing chaotic kind of motion (we name this kind of indiscernible motion the chaotic motion and the associated quantities, chaotic quantities as established, for  $v_c$ ).

### 6.1 Geometric modification of Equation 21

**Equation (21)** necessitates the incorporation of a geometrically squared magnitude to account for the chaotic velocity of an electric charge. To explore how energy can be generated, a shift in the physical perspective of **Equation (21)** is required. Following the assumptions underlying **Equation (22)**, the equation can be reduced to its geometric counterpart. Given the previously established geometric definitive condition, where  $(\overline{OA} \cong \overline{AB} \cong \overline{BU} \cong \overline{OU}) \not\cong (\overline{OH} \cong \overline{UF})$ , the mechanical energy expression becomes:

$$E_{mech} = \sum_{i=1}^N \left( \left[ \frac{1}{2} m v_c^2 - \frac{1}{2} m v_o^2 \right] + mgz + kx \right)_i \neq \text{constant} \quad (53)$$

Further refinements lead to the following geometric formulation:

$$E_{mech} = \sum_{i=1}^N \left( \left[ \frac{1}{2} v_c^2 \ominus \frac{1}{2} v_o^2 \right] \oplus z \oplus x \right)_i \neq \text{constant} \quad (54)$$

**Equations (53)** and **(54)** indicate that under classical limits, the Law of Energy Conservation (LEC) has consistently been violated. Under the specified set construction condition  $(\overline{OA} \cong \overline{AB} \cong \overline{BU} \cong \overline{OU}) \not\cong (\overline{OH} \cong \overline{UF})$ , it becomes evident that  $v_c^2 > v_o^2$ . This inequality suggests that a geometric subtraction in **Equations (54)** demonstrates that a system comprising both chaotic and ordered motions inherently results in an excess of a measurable quantity. To address this paradox, attention is directed to adjusting the position of point  $U$  in **Figure 10** towards point  $O$ . Observations reveal that as point  $U$  approaches point  $O$ , the magnitude  $(v_o^2)$  diminishes while  $(v_c^2)$  increases significantly. Through **Definitions (8)** and **(10)**, the geometric multiplication of distinct points, given two distinct base points on a plane, translates into the geometric multiplication of distinct magnitudes relative to a specific base point. Consequently, the geometric difference between the terms in the square brackets in **Equations (53)** and **(54)** corresponds to the geometric difference between two distinct product magnitudes, obtained as the geometric squares of two unique straight-line segments. Each magnitude's geometric square is definable as:  $OA \otimes OB: OU \cong (OA/OU) \otimes (OB/OU)$ . This result adheres to the principles of René Descartes' operation, as illustrated in Appendix 1. Throughout the paper, significant advancements have been achieved. The complete establishment of the LEC for a thermodynamics isolated system configuration in physics prompted an investigation into the meaning of a thermodynamics isolated system. The deductions revealed that the current understanding of a thermodynamics isolated system is scientifically flawed and vague. The notion of multiple isolated systems in the entire universe was identified as a serious scientific and mathematical misinterpretation. The paper proposed an alternative and definitive perspective on the thermodynamics isolated system, referred to as *TIS* (**Definition 5**), within a Euclidean plane. Geometrically, the established workflow operates within an interface named *ETIS*. Building on the *TIS* definition, the review refuted the false hypothesized multiverse concepts [109], particularly when considering the universe as a practical example of a *TIS*. It has been established that the Law of Energy Conservation (LEC) operates within defined classical bounds and has been consistently challenged in classical systems. The electrical short circuit, serving as an exemplary model transitioning from ordered to chaotic modes, provided a foundation for completing this proof. This was achieved through the introduction of chaotic magnitudes within the proposed steady-state mode in a classical system. However, it is important to emphasize that the short circuit concept was employed illustratively, as depicted in **Figure 8**. The exploration of short circuits as a potential means of energy generation remains a topic for a separate study. **Equation**

(54) fundamentally reinterprets Equation (22), indicating that the difference between the terms within the square brackets will always exceed the initial state of the system. Geometrically, when the construction is completed as mentioned previously, Equation (54) corresponds to the operation  $([\overline{OJ} - \overline{OE}] \oplus \overline{EZ} \oplus \overline{ZX}) \cong \overline{OX}$ , where the magnitude  $\overline{OX}$  is large enough, in proportions to the difference due to the terms in the square braces. Thus, as it was desired, it is proven that the LEC can be broken in the ordinary physical settings. Considerably, processes go through in a particular direction and not the opposite. In the exposed workflow, directionality was observed following the rigor of Euclidean geometric constructions. This was in caution though, as direction is not constrained by the LEC. In thermodynamics, adherence to the first law (LEC) and second law is crucial for a process to occur [86,110]. Notably, this principle remains consistent across the established proofs. The presented proof for the Law of Energy Conservation (LEC) proposes a novel approach, challenging the traditional reliance on the impossibility of perpetual motion. Instead, it asserts that the LEC can be derived from the fundamental principle that 'something cannot originate from nothing', particularly when the two entities are inherently similar. This paper paves the way for a more philosophical exploration of the LEC, moving beyond purely physical considerations.

**Remark 11 (energy generation perspective).**

In the context of this paper, we consider “creating energy” as establishing a scheme that defines a higher energy output given some energy input to a system, without external interferences to the specific processes. Consider Theorem 2.

**Theorem 2 (Violation of the law of energy conservation in chaotic-ordered systems).**

Let  $v_o$  represent the ordered velocity magnitude and  $v_c$  represent the chaotic velocity magnitude of point-particles in a classical system. If the chaotic velocity exceeds the ordered velocity, i.e.,  $v_c > v_o$ , then the system breaks the Law of Energy Conservation according to Equation (45).

**Geometric setup (Elaborated proof).**

Consider the instantaneous velocity magnitudes  $v_o$  for ordered flow and  $v_c$  for chaotic flow in a classical system. Let  $O$  and  $U$  be distinct basepoints from which we measure these velocities geometrically.

- Let the ordered velocity be represented geometrically by the line segment  $OA_o$ .
- Let the chaotic velocity be represented geometrically by the line segment  $OB_c$ .

**Energy Relationship.**

The kinetic energy corresponding to each flow state (ordered and chaotic) is given in Equation (45) can be broken as follows:

$$\text{Ordered kinetic energy. } KE_E^{(o)} = \frac{1}{2}mv_o^2$$

$$\text{Chaotic kinetic energy. } KE_E^{(c)} = \frac{1}{2}mv_c^2$$

**Conditions for energy violation.**

The Law of Energy Conservation is broken under the following conditions.

- In a conserved energy system, the kinetic energy cannot simultaneously exist in both chaotic and ordered states.
- Velocity Condition. Violation of the Law of Energy Conservation occurs if  $v_c \neq v_o$ . Implying that the geometric difference between the squared chaotic and ordered velocities must be positive.
- Geometric Difference and Kinetic Energy Imbalance. In particular, if  $v_c > v_o$ , the chaotic kinetic energy  $KE_E^{(c)}$  exceeds the ordered kinetic energy  $KE_E^{(o)}$  implying that  $E_k = \frac{1}{2}m(v_c^2 - v_o^2) > 0$ .
- Absence of External Input. No external energy is introduced to account for the increase in chaotic kinetic energy.

**Geometric justification.**

According to Definition 10, the geometric difference between chaotic and ordered magnitudes with respect to basepoints  $O$  and  $U$  is non-zero when  $v_c \neq v_o$ . This geometric non-equivalence directly translates to an energetic non-equivalence.

**Implication for energy conservation.**

If  $v_c > v_o$ , the difference  $v_c^2 - v_o^2$  is positive, and thus the chaotic kinetic energy exceeds the ordered kinetic energy. In classical physics, this extra kinetic energy does not originate from any discernible source, thus implying a violation of the Law of Energy Conservation. The system has more energy in the chaotic state than it had in the ordered state, with no external input.

Therefore, under the assumption that  $v_c > v_o$ , the system violates the Law of Energy Conservation, according to Definition 10. The difference in kinetic energies breaks the standard conservation rule, thus establishing the theorem.

6.2 A significance of the provable review

This paper fundamentally redefines the geometric framework underpinning the Law of Energy Conservation (LEC) by introducing and rigorously establishing chaotic magnitudes within a Euclidean plane. Central to this exploration is the geometric proof tied to Equation (45), which conclusively demonstrates that energy systems can deviate from traditional assumptions of initiation from rest or zero velocity. This insight highlights the innovative realization that classical physical settings can indeed exhibit violations of the LEC under specific configurations. The geometric proofs presented herein emphasize the critical relationship between chaotic and ordered motions, offering a novel lens for understanding energy interactions in both theoretical and practical domains. The established chaotic magnitude plays a pivotal role in extending the expressibility of the LEC. Firstly, it provides a robust framework for addressing discrepancies between traditional and modern interpretations of mechanical energy. Secondly, it

establishes a geometric foundation for analyzing transitions between ordered and chaotic systems, particularly in scenarios like electrical short circuits. Finally, it enables the formulation of new mathematical constructs to describe energy interactions beyond classical constraints, offering insights into phenomena that were previously deemed impossible within the established confines of energy conservation.

### 6.3 Implications of the study

This paper introduces a paradigm shift in understanding the LEC by exploring its aspects under chaotic and complex phenomena, specifically within steady-state modes of electrical short circuits. This approach challenges the conventional transient-focused perspective, offering a deeper understanding of energy systems when transitioning between ordered and chaotic modes. Such insights provide corrections to long-standing misconceptions regarding the universality of the LEC, presenting opportunities for novel interpretations and applications. The implications of this paper extend to practical domains, including the global energy crisis. By proposing a framework where energy generation aligns with the explored steady-state models, the study highlights potential pathways to reduce dependence on finite energy resources. This aligns with the pursuit of green and clean energy systems, where the proposed constructs could minimize noise and air pollution, paving the way for sustainable innovations. Moreover, this paper fosters advancements in understanding energy conservation under extreme conditions, suggesting broader applications in high-efficiency technologies. These include minimizing energy losses in power transmission and enabling breakthroughs in energy storage systems. Finally, the presented proofs contribute to the broader scientific discourse, providing a solid mathematical foundation for future explorations of energy phenomena in complex physical systems.

## 7 Conclusion

The paper has provided a detailed exploration of the Law of Energy Conservation (LEC) from both scientific and mathematical perspectives. A two-pronged approach was utilized to assess the validity of the LEC. A novel geometric proof, independent of experimental validation, was developed, revealing a remarkable implication: the LEC might be systematically violated in certain classical systems. Such a violation could arise from the non-universality of energy creation or destruction or by challenging the conventional understanding of energy transformation in specific contexts. The electrical short circuit model, characterized by excessive flow or accumulation of electric charges at a specific point within a conductor—viewed as point particles in a chaotic system—illustrated a plausible scenario for such a violation in classical frameworks. This study underscores the potential limitations of scientific understanding when it relies exclusively on inductive, observation-based methodologies. The necessity of rigorous, deductive proofs, developed independently of experimental constraints, is emphasized as critical for constructing a more robust and comprehensive scientific framework. The analysis suggests that technological advancements can

facilitate the establishment of demonstrable proofs for fundamental natural phenomena, even in scenarios where traditional experimental validation is impractical. The presented findings reveal potential gaps in the current understanding of physics, which may arise from inadequacies in the philosophical and mathematical frameworks employed to study natural systems. The investigation further proposes that violations of the Law of Energy Conservation (LEC) could occur in classical systems, such as electrical short circuits (when considered as an example model of a chaotic system), particularly when analyzed within a steady-state framework. However, validating or invalidating this requires a new approach. Developing a comprehensive scheme applicable across dimensions, ensuring consistency beyond mathematical formalization, is essential. This would enable the design of experiments or proofs that definitively demonstrate LEC violation. Furthermore, improved formulations for calculating short-circuit currents, incorporating the concepts introduced in this paper, are necessary for a more complete understanding of this phenomenon. Further validation of the geometric proof and the concept of “*Chaotic Magnitude*” is crucial. This validation could involve applying these ideas to other physical systems and comparing the results with established physical laws. Additionally, exploring the philosophical and mathematical implications of the proposed framework for studying the LEC could lead to significant advancements in our understanding of energy and its behavior. The paper argues that perpetual motion machines are not a valid method for proving the LEC. The reasons for this include potential violations occurring within the system itself, masked by our current understanding. Hence, this paper presented a novel approach to the LEC, employing geometric proofs and highlighting the limitations of purely experimental methods. The potential violation of the LEC in classical systems, particularly during electrical short circuits (as the examples assert the generation of higher electrical current than the systems input current), highlights the need for a more comprehensive scientific framework. Future research should focus on developing a cross-dimensional validation scheme, improving short-circuit current calculations, and further validating the geometric proof and the concept of “*Chaotic Magnitude*”. These advancements can lead to a deeper understanding of the LEC and its role in the physical world.

### Conflict of interest

The author declares that there is no conflict of interest.

### Similarity rate (Drillbit): 6%

### References

- [1] H. Goldstein, C. P. Poole, and J. L. Safko, *Classical mechanics*, 3. ed., [Nachdr.]. San Francisco Munich: Addison Wesley, 2008.
- [2] G. Kalies and D. D. Do, “Momentum work and the energetic foundations of physics. I. Newton’s laws of motion tailored to processes,” *AIP Adv.*, vol. 13, no. 6, p. 065121, Jun. 2023, <https://doi.org/10.1063/5.0147910>.

- [3] F. Verhulst, "Henri Poincaré (1854–1912) Engineer, Mathematician, Physicist and Philosopher," in IUTAM Symposium on Exploiting Nonlinear Dynamics for Engineering Systems, vol. 37, I. Kovacic and S. Lenci, Eds., in IUTAM Bookseries, vol. 37, Cham: Springer International Publishing, 2020, pp. 15–26. [https://doi.org/10.1007/978-3-030-23692-2\\_2](https://doi.org/10.1007/978-3-030-23692-2_2).
- [4] "Poincaré, Jules Henri | Internet Encyclopedia of Philosophy." Accessed: Jan. 10, 2025. [Online]. Available: <https://iep.utm.edu/poincare/>.
- [5] M. Silberstein, W. M. Stuckey, and T. McDevitt, "Beyond Causal Explanation: Einstein's Principle Not Reichenbach's," *Entropy*, vol. 23, no. 1, p. 114, Jan. 2021, <https://doi.org/10.3390/e23010114>.
- [6] L. Guzzardi, "Energy, Metaphysics, and Space: Ernst Mach's Interpretation of Energy Conservation as the Principle of Causality," *Sci. Educ.*, vol. 23, no. 6, pp. 1269–1291, Jun. 2014, <https://doi.org/10.1007/s11191-012-9542-9>.
- [7] J. B. Pitts, "Conservation of Energy: Missing Features in Its Nature and Justification and Why They Matter," *Found. Sci.*, vol. 26, no. 3, pp. 559–584, Sep. 2021, <https://doi.org/10.1007/s10699-020-09657-1>.
- [8] N. Banerjee and S. Sen, "Einstein pseudotensor and total energy of the universe," *Pramana*, vol. 49, no. 6, pp. 609–615, Dec. 1997, <https://doi.org/10.1007/BF02848334>.
- [9] L. Patton, "Experiment and theory building," *Synthese*, vol. 184, no. 3, pp. 235–246, Feb. 2012, <https://doi.org/10.1007/s11229-010-9772-9>.
- [10] "Chapter 1: The Nature of Science." Accessed: Jan. 10, 2025. [Online]. Available: <https://www.project2061.org/publications/sfaa/online/chap1.htm>?
- [11] P. Fara, "What Is Science? A Historian's Perplexities," *Métode Rev. Difus. Investig.*, vol. 0, no. 5, Apr. 2015, <https://doi.org/10.7203/metode.84.3915>.
- [12] R. V. Blystone and K. Blodgett, "WWW: The Scientific Method," *CBE—Life Sci. Educ.*, vol. 5, no. 1, pp. 7–11, Mar. 2006, <https://doi.org/10.1187/cbe.05-12-0134>.
- [13] K. Morsanyi, T. McCormack, and E. O'Mahony, "The link between deductive reasoning and mathematics," *Think. Reason.*, vol. 24, no. 2, pp. 234–257, Apr. 2018, <https://doi.org/10.1080/13546783.2017.1384760>.
- [14] Liaqat Khan, "What is Mathematics - an Overview," 2015, Unpublished. <https://doi.org/10.13140/RG.2.1.3626.8967>.
- [15] Jaydip Datta, "MATHEMATICS: An Inductive & Deductive Review," 2022, <https://doi.org/10.13140/RG.2.2.25473.99683/9>.
- [16] B. Shea, "Karl Popper: Philosophy of Science," 2016.
- [17] S. El-Badawy, "The Importance of Inductive Reasoning in Science: A Critical Analysis," 2022, <https://doi.org/10.13140/RG.2.2.18728.14087>.
- [18] B. Hepburn and H. Andersen, "Scientific Method," in *The Stanford Encyclopedia of Philosophy*, Summer 2021., E. N. Zalta, Ed., Metaphysics Research Lab, Stanford University, 2021. Accessed: Jan. 10, 2025. [Online]. Available: <https://plato.stanford.edu/archives/sum2021/entries/scientific-method/>.
- [19] R. Meer, "Immanuel Kant's Theory of Objects and Its Inherent Link to Natural Science," *Open Philos.*, vol. 1, no. 1, pp. 342–359, Nov. 2018, <https://doi.org/10.1515/opphil-2018-0025>.
- [20] A. Botica, "Intended' and 'Experienced' Meaning: Reevaluating the Reader-Response Theory," *J. Educ. Soc. Res.*, Oct. 2013, <https://doi.org/10.5901/jesr.2013.v3n7p519>.
- [21] H. Meyer-Ortmann and T. Reisz, Principles of Phase Structures in Particle Physics, vol. 77. in *World Scientific Lecture Notes in Physics*, vol. 77. WORLD SCIENTIFIC, 2006. <https://doi.org/10.1142/3763>.
- [22] A. Szeglet and F. Márkus, "Dissipation in Lagrangian Formalism," *Entropy*, vol. 22, no. 9, p. 930, Aug. 2020, <https://doi.org/10.3390/e22090930>.
- [23] D. Mušicki, "Extended Lagrangian formalism and the corresponding energy relations," *Eur. J. Mech. - ASolids*, vol. 23, no. 6, pp. 975–991, Nov. 2004, <https://doi.org/10.1016/j.euromechsol.2004.01.010>.
- [24] R. M. Marinho, "Noether's theorem in classical mechanics revisited," *Eur. J. Phys.*, vol. 28, no. 1, pp. 37–43, Jan. 2007, <https://doi.org/10.1088/0143-0807/28/1/004>.
- [25] K. Brading and E. Castellani, "SYMMETRIES AND INVARIANCES IN CLASSICAL PHYSICS," in *Philosophy of Physics*, Elsevier, 2007, pp. 1331–1367. <https://doi.org/10.1016/B978-044451560-5/50016-6>.
- [26] S. Bilbao, M. Ducceschi, and F. Zama, "Explicit exactly energy-conserving methods for Hamiltonian systems," *J. Comput. Phys.*, vol. 472, p. 111697, Jan. 2023, <https://doi.org/10.1016/j.jcp.2022.111697>.
- [27] G. Kalies and D. D. Do, "Momentum work and the energetic foundations of physics. III. The unification of mechanics and electrodynamics," *AIP Adv.*, vol. 13, no. 9, p. 095322, Sep. 2023, <https://doi.org/10.1063/5.0166847>.
- [28] H. Liu, X. Cai, Y. Cao, and G. Lapenta, "An efficient energy conserving semi-Lagrangian kinetic scheme for the Vlasov-Ampère system," *J. Comput. Phys.*, vol. 492, p. 112412, Nov. 2023, <https://doi.org/10.1016/j.jcp.2023.112412>.
- [29] D. E. Chang, A. M. Bloch, N. E. Leonard, J. E. Marsden, and C. A. Woolsey, "The Equivalence of Controlled Lagrangian and Controlled Hamiltonian Systems," *ESAIM Control Optim. Calc. Var.*, vol. 8, pp. 393–422, 2002, <https://doi.org/10.1051/cocv:2002045>.
- [30] C. Woolsey, C. K. Reddy, A. M. Bloch, D. E. Chang, N. E. Leonard, and J. E. Marsden, "Controlled Lagrangian Systems with Gyroscopic Forcing and Dissipation," *Eur. J. Control*, vol. 10, no. 5, pp. 478–

- 496, Jan. 2004, <https://doi.org/10.3166/ejc.10.478-496>.
- [31] P. Holland, "Hamiltonian theory of wave and particle in quantum mechanics I. Liouville's theorem and the interpretation of the de Broglie-Bohm theory," *Il Nuovo Cimento B*, vol. 116, Sep. 2001.
- [32] V. Rastogi, A. Mukherjee, and A. Dasgupta, "A review on extension of Lagrangian-Hamiltonian mechanics," *J. Braz. Soc. Mech. Sci. Eng.*, vol. 33, no. 1, pp. 22–33, Mar. 2011, <https://doi.org/10.1590/S1678-58782011000100004>.
- [33] C. R. Galley, "Classical Mechanics of Nonconservative Systems," *Phys. Rev. Lett.*, vol. 110, no. 17, p. 174301, Apr. 2013, <https://doi.org/10.1103/PhysRevLett.110.174301>.
- [34] J.-T. Xing, "Generalised energy conservation law for chaotic phenomena," *Acta Mech. Sin.*, vol. 35, no. 6, pp. 1257–1268, Dec. 2019, <https://doi.org/10.1007/s10409-019-00886-7>.
- [35] R. Trudeau, "Euclidean Geometry," 2001, pp. 22–105. [https://doi.org/10.1007/978-1-4612-2102-9\\_2](https://doi.org/10.1007/978-1-4612-2102-9_2).
- [36] C. Sasaki, "The Géométrie of 1637," in *Descartes's Mathematical Thought*, vol. 237, in *Boston Studies in the Philosophy of Science*, vol. 237, Dordrecht: Springer Netherlands, 2003, pp. 205–280. [https://doi.org/10.1007/978-94-017-1225-5\\_6](https://doi.org/10.1007/978-94-017-1225-5_6).
- [37] M. Panza, "Rethinking geometrical exactness," *Hist. Math.*, vol. 38, no. 1, pp. 42–95, Feb. 2011, <https://doi.org/10.1016/j.hm.2010.09.001>.
- [38] A. Ostermann and G. Wanner, "The Elements of Euclid," in *Geometry by Its History*, in *Undergraduate Texts in Mathematics*, Berlin, Heidelberg: Springer Berlin Heidelberg, 2012, pp. 27–59. [https://doi.org/10.1007/978-3-642-29163-0\\_2](https://doi.org/10.1007/978-3-642-29163-0_2).
- [39] R. Hartshorne, "Teaching Geometry According to Euclid," *Not. Am. Math. Soc.*, vol. 47, Jan. 2000.
- [40] A. M. Kimuya, "Constructability and Rigor of Angles Multiples of 3 in Euclidean Geometry," *Trends J. Sci. Res.*, vol. 2, no. 1, pp. 1–27, Jan. 2024, <https://doi.org/10.31586/jml.2024.841>.
- [41] N. F. Shul'ga, V. V. Syshchenko, A. I. Tarnovsky, V. I. Dronik, and A. Yu. Isupov, "Regular and chaotic motion domains in the channeling electron's phase space and mean level density for its transverse motion energy," *J. Instrum.*, vol. 14, no. 12, pp. C12022–C12022, Dec. 2019, <https://doi.org/10.1088/1748-0221/14/12/C12022>.
- [42] F. Borceux, "Euclid's Elements," in *An Axiomatic Approach to Geometry*, Cham: Springer International Publishing, 2014, pp. 43–110. [https://doi.org/10.1007/978-3-319-01730-3\\_3](https://doi.org/10.1007/978-3-319-01730-3_3).
- [43] R. J. Trudeau, "Euclidean Geometry," in *The Non-Euclidean Revolution*, Boston, MA: Birkhäuser Boston, 2001, pp. 22–105. [https://doi.org/10.1007/978-1-4612-2102-9\\_2](https://doi.org/10.1007/978-1-4612-2102-9_2).
- [44] P. Mancosu, "Descartes and Mathematics," in *A Companion to Descartes*, John Wiley & Sons, Ltd, 2007, pp. 103–123. <https://doi.org/10.1002/9780470696439.ch7>.
- [45] G. Kalies, "Fundamental laws of nature confirmed by free fall," *Jun.* 18, 2021. <https://doi.org/10.21203/rs.3.rs-624477/v1>.
- [46] L. Guzzardi, "Energy, Metaphysics, and Space: Ernst Mach's Interpretation of Energy Conservation as the Principle of Causality," *Sci. Educ.*, vol. 23, no. 6, pp. 1269–1291, Jun. 2014, <https://doi.org/10.1007/s11191-012-9542-9>.
- [47] C. R. Palmerino, "Law of Free Fall in Renaissance Science," in *Encyclopedia of Renaissance Philosophy*, M. Sgarbi, Ed., Cham: Springer International Publishing, 2019, pp. 1–7. [https://doi.org/10.1007/978-3-319-02848-4\\_939-1](https://doi.org/10.1007/978-3-319-02848-4_939-1).
- [48] E. Goren and I. Galili, "Newton's Law - A Theory of motion or force?," *J. Phys. Conf. Ser.*, vol. 1287, no. 1, p. 012061, Aug. 2019, <https://doi.org/10.1088/1742-6596/1287/1/012061>.
- [49] J. Avigad, E. DEAN, and J. Mumma, "A Formal System for Euclid'S Elements," *Rev. Symb. Log.*, vol. 2, pp. 700–768, Dec. 2009, <https://doi.org/10.1017/S1755020309990098>.
- [50] M. Bunge, "Energy: Between Physics and Metaphysics," *Sci. Educ.*, vol. 9, no. 5, pp. 459–463, Sep. 2000, <https://doi.org/10.1023/A:1008784424048>.
- [51] P. Davies and N. H. Gregersen, Eds., *Information and the Nature of Reality: From Physics to Metaphysics*, 1st ed. Cambridge University Press, 2014. <https://doi.org/10.1017/CBO9781107589056>.
- [52] C. Annamalai and A. M. D. O. Siqueira, "Mass-Energy Equivalence derived from Newtonian mechanics," *J. Eng. Exact Sci.*, vol. 9, no. 8, pp. 15963–01e, Jun. 2023, <https://doi.org/10.18540/jcecvl9iss8pp15963-01e>.
- [53] G. D'Abramo, "Mass–energy connection without special relativity," *Eur. J. Phys.*, vol. 42, no. 1, p. 015606, Jan. 2020, <https://doi.org/10.1088/1361-6404/abbca2>.
- [54] B. Muhyedeen, "New Concept of Mass-Energy Equivalence," *Eur. J. Sci. Res.*, vol. ISSN 1450-216X Vol.26 No.2 (2009), pp.161–175, Feb. 2009.
- [55] R. Gobato, A. Gobato, and D. F. G. Fedrigo, "Energy and matter," Sep. 02, 2015, arXiv: arXiv:1509.02892. <https://doi.org/10.48550/arXiv.1509.02892>.
- [56] C. Barreiro, J. M. Barreiro, J. A. Lara, D. Lizcano, M. A. Martínez, and J. Pazos, "The Third Construct of the Universe: Information," *Found. Sci.*, vol. 25, no. 2, pp. 425–440, Jun. 2020, <https://doi.org/10.1007/s10699-019-09630-7>.
- [57] T. R. Mongan, "Origin of the Universe, Dark Energy, and Dark Matter," *J. Mod. Phys.*, vol. 09, no. 05, pp. 832–850, 2018, <https://doi.org/10.4236/jmp.2018.95054>.
- [58] N. Raos, "Atomism in greek philosophy," *Kem. U Ind. Chem. Chem. Eng.*, vol. 51, pp. 385–392, Jan. 2002.

- [59] C. Masolo and L. Vieu, "Atomicity vs. Infinite Divisibility of Space," in *Spatial Information Theory. Cognitive and Computational Foundations of Geographic Information Science*, vol. 1661, C. Freksa and D. M. Mark, Eds., in *Lecture Notes in Computer Science*, vol. 1661, Berlin, Heidelberg: Springer Berlin Heidelberg, 1999, pp. 235–250. [https://doi.org/10.1007/3-540-48384-5\\_16](https://doi.org/10.1007/3-540-48384-5_16).
- [60] V. Villani, "The Way Ahead," in *Perspectives on the Teaching of Geometry for the 21st Century*, vol. 5, C. Mammana and V. Villani, Eds., in *New ICMI Study Series*, vol. 5, Dordrecht: Springer Netherlands, 1998, pp. 319–327. [https://doi.org/10.1007/978-94-011-5226-6\\_11](https://doi.org/10.1007/978-94-011-5226-6_11).
- [61] A. Oliveira, "Coriolis' Theory of Machines and Mechanisms," Jan. 1980.
- [62] "Descartes, Rene | Internet Encyclopedia of Philosophy." Accessed: Jan. 10, 2025. [Online]. Available: <https://iep.utm.edu/rene-descartes/>.
- [63] R. Descartes, *The geometry of René Descartes*. New York, NY: Dover Publications, 1996.
- [64] R. Hershkowitz et al., "Reasoning in Geometry," in *Perspectives on the Teaching of Geometry for the 21st Century*, vol. 5, C. Mammana and V. Villani, Eds., in *New ICMI Study Series*, vol. 5, Dordrecht: Springer Netherlands, 1998, pp. 29–83. [https://doi.org/10.1007/978-94-011-5226-6\\_3](https://doi.org/10.1007/978-94-011-5226-6_3).
- [65] D. Lomas, "Geometry starting with Euclid," *Can. J. Sci. Math. Technol. Educ.*, vol. 5, no. 2, pp. 271–276, Apr. 2005, <https://doi.org/10.1080/14926150509556659>.
- [66] W. Halbfäß, "Descartes, René: Principia philosophiae," in *Kindlers Literatur Lexikon (KLL)*, H. L. Arnold, Ed., Stuttgart: J.B. Metzler, 2020, pp. 1–3. [https://doi.org/10.1007/978-3-476-05728-0\\_9540-1](https://doi.org/10.1007/978-3-476-05728-0_9540-1).
- [67] E. Mach, "ON THE PRINCIPLE OF THE CONSERVATION OF ENERGY," *The Monist*, vol. 5, no. 1, pp. 22–54, 1894.
- [68] J.-P. Anfray, "Leibniz and Descartes," in *The Oxford Handbook of Descartes and Cartesianism*, S. Nadler, T. M. Schmalz, and D. Antoine-Mahut, Eds., Oxford University Press, 2019, pp. 720–737. <https://doi.org/10.1093/oxfordhb/9780198796909.013.45>.
- [69] Y. Kato and K. Sakamoto, "Between Cartesianism and orthodoxy: God and the problem of indifference in Christoph Wittich's Anti-Spinoza," *Intellect. Hist. Rev.*, pp. 1–19, Dec. 2020, <https://doi.org/10.1080/17496977.2020.1852373>.
- [70] G. E. Smith, "The vis viva dispute: A controversy at the dawn of dynamics," *Phys. Today*, vol. 59, no. 10, pp. 31–36, Oct. 2006, <https://doi.org/10.1063/1.2387086>.
- [71] M. N. Hidayat, S. P. Chairandy, and F. Ronilaya, "Design and Analysis of A Perpetual Motion Machine Using Neodymium Magnets as A Prime Mover," *J. Southwest Jiaotong Univ.*, vol. 56, no. 2, pp. 211–219, Apr. 2021, <https://doi.org/10.35741/issn.0258-2724.56.2.17>.
- [72] S. V. Kukhlevsky, "Breaking of Energy Conservation Law: Creating and Destroying of Energy by Subwavelength Nanosystems," 2006, arXiv. <https://doi.org/10.48550/ARXIV.PHYSICS/061000>.
- [73] J. F. Rodríguez-León, I. Cervantes, E. Castillo-Castañeda, G. Carbone, and D. Cafolla, "Design and Preliminary Testing of a Magnetic Spring as an Energy-Storing System for Reduced Power Consumption of a Humanoid Arm," *Actuators*, vol. 10, no. 6, p. 136, Jun. 2021, <https://doi.org/10.3390/act10060136>.
- [74] A. P. David, "Electro-Magnetic Induction: Free Electricity Generator," May 18, 2017, Social Science Research Network, Rochester, NY: 3486740. <https://doi.org/10.2139/ssrn.3486740>.
- [75] N. Coppedge, "TOP PERPETUAL MOTION MACHINES," May 2022.
- [76] M. S. Berman, "On the Zero-Energy Universe," *Int. J. Theor. Phys.*, vol. 48, no. 11, pp. 3278–3286, Nov. 2009, <https://doi.org/10.1007/s10773-009-0125-8>.
- [77] M. Berman, "On the Zero-Energy Universe," *Int. J. Theor. Phys.*, vol. 48, May 2006, <https://doi.org/10.1007/s10773-009-0125-8>.
- [78] "Descartes, Rene: Scientific Method | Internet Encyclopedia of Philosophy." Accessed: Jul. 16, 2022. [Online]. Available: <https://iep.utm.edu/rene-descartes-scientific-method/>.
- [79] J. F. Scott, *The scientific work of René Descartes (1596-1650)*. in *Routledge library editions: René Descartes*, no. volume 3. London: Routledge, 2017.
- [80] A. Micheli and P. Iturralde, "[On the evolution of scientific thought]," *Arch. Cardiol. Mex.*, vol. 85, Aug. 2015, <https://doi.org/10.1016/j.acmx.2015.06.003>.
- [81] Y. Guan et al., "Burden of the global energy price crisis on households," *Nat. Energy*, vol. 8, no. 3, Art. no. 3, Mar. 2023, <https://doi.org/10.1038/s41560-023-01209-8>.
- [82] M. Farghali et al., "Strategies to save energy in the context of the energy crisis: a review," *Environ. Chem. Lett.*, vol. 21, no. 4, pp. 2003–2039, Aug. 2023, <https://doi.org/10.1007/s10311-023-01591-5>.
- [83] J. Mitali, S. Dhinakaran, and A. A. Mohamad, "Energy storage systems: a review," *Energy Storage Sav.*, vol. 1, no. 3, pp. 166–216, Sep. 2022, <https://doi.org/10.1016/j.enss.2022.07.002>.
- [84] R. Machotka, "Euclidean Model of Space and Time," *J. Mod. Phys.*, vol. 09, pp. 1215–1249, Jan. 2018, <https://doi.org/10.4236/jmp.2018.96073>.
- [85] O. Ericok and J. Mason, *Foundations of a Finite Non-Equilibrium Statistical Thermodynamics: Extrinsic Quantities*. 2022.
- [86] U. Seifert, "First and Second Law of Thermodynamics at Strong Coupling," *Phys. Rev. Lett.*, vol. 116, no. 2, p. 020601, Jan. 2016, <https://doi.org/10.1103/PhysRevLett.116.020601>.



- [87] Y.-F. Chang, "Entropy Decrease in Isolated Systems: Theory, Fact and Tests: Physics," *Int. J. Fundam. Phys. Sci.*, vol. 10, no. 2, Art. no. 2, Jun. 2020, <https://doi.org/10.14331/ijfps.2020.330137>.
- [88] H. Choi, "Size and Expansion of the Universe in Zero Energy Universe (Logical defenses for the Model 'We are living in a black hole' )," Nov. 2016.
- [89] P. Halpern and N. Tomasello, "Size of the Observable Universe," *Adv. Astrophys.*, vol. 1, Nov. 2016, <https://doi.org/10.22606/adap.2016.13001>.
- [90] R. Hershkowitz et al., "Reasoning in Geometry," in *Perspectives on the Teaching of Geometry for the 21st Century: An ICMI Study*, C. Mammana and V. Villani, Eds., in *New ICMI Study Series.*, Dordrecht: Springer Netherlands, 1998, pp. 29–83. [https://doi.org/10.1007/978-94-011-5226-6\\_3](https://doi.org/10.1007/978-94-011-5226-6_3).
- [91] "Euclid's Elements, Book II, Proposition 10." Accessed: Jun. 29, 2023. [Online]. Available: <http://aleph0.clarku.edu/~djoyce/elements/bookII/propII10.html>.
- [92] C. Masolo and L. Vieu, "Atomicity vs. Infinite Divisibility of Space," in *COSIT*, 1999. [https://doi.org/10.1007/3-540-48384-5\\_16](https://doi.org/10.1007/3-540-48384-5_16).
- [93] N. Raos, "Atomism in greek philosophy," *Kem. U Ind. Chem. Chem. Eng.*, vol. 51, pp. 385–392, Jan. 2002.
- [94] S. W. Gaukroger, "Descartes' Conception of Inference," in *Metaphysics and Philosophy of Science in the Seventeenth and Eighteenth Centuries: Essays in honour of Gerd Buchdahl*, R. S. Woolhouse, Ed., in *The University of Western Ontario Series in Philosophy of Science.*, Dordrecht: Springer Netherlands, 1988, pp. 101–132. [https://doi.org/10.1007/978-94-009-2997-5\\_6](https://doi.org/10.1007/978-94-009-2997-5_6).
- [95] Heath, Thomas L, *The Thirteen Books of Euclid's Elements*, translated from the text of Heiberg, with introduction and commentary, 2nd ed., vol. 3 vols. Cambridge (available in Dover reprint): University Press, 1926.
- [96] N. F. Shul'ga, V. V. Syshchenko, A. I. Tarnovsky, V. I. Dronik, and A. Y. Isupov, "Regular and chaotic motion domains in the channeling electron's phase space and mean level density for its transverse motion energy," *J. Instrum.*, vol. 14, no. 12, pp. C12022–C12022, Dec. 2019, <https://doi.org/10.1088/1748-0221/14/12/C12022>.
- [97] B. T. Utelbayev, E. Suleimenov, and U. A.B., "Elementary Particles and Properties of Material Objects Review Article," Dec. 2018.
- [98] S. Reucroft and E. Williams, "The Structure and Properties of Elementary Particles," Oct. 2019.
- [99] R. Abreu and V. Guerra, "The concepts of work and heat and the first and second laws of thermodynamics," Mar. 2012.
- [100] S. Shahsavari and P. Torkaman, "Energy Conservation Principle from the Perspective of the Energy Structure Theory," *Asian J. Appl. Sci.*, vol. 10, no. 5, Nov. 2022, <https://doi.org/10.24203/ajas.v10i5.6950>.
- [101] B. Xia, Z. Chen, C. Mi, and B. Robert, "External short circuit fault diagnosis for lithium-ion batteries," in *2014 IEEE Transportation Electrification Conference and Expo (ITEC)*, Dearborn, MI: IEEE, Jun. 2014, pp. 1–7. <https://doi.org/10.1109/ITEC.2014.6861806>.
- [102] Z. Chen, R. Xiong, J. Tian, X. Shang, and J. Lu, "Model-based fault diagnosis approach on external short circuit of lithium-ion battery used in electric vehicles," *Appl. Energy*, vol. 184, pp. 365–374, Dec. 2016, <https://doi.org/10.1016/j.apenergy.2016.10.026>.
- [103] A. Berizzi, A. Silvestri, D. Zaninelli, and S. Massucco, "Short-circuit current calculation: A comparison between methods of IEC and ANSI standards using dynamic simulation as reference," *IEEE Trans. Ind. Appl. Inst. Electr. Electron. Eng. U. S.*, vol. 30:4, <https://doi.org/10.1109/IAS.1993.299168>.
- [104] F. V. Conte, P. Gollob, and H. Lacher, "Safety in the battery design: The short circuit," *World Electr. Veh. J.*, vol. 3, Dec. 2009, <https://doi.org/10.3390/wevj3040719>.
- [105] M. F. Moad, "On Thevenin's and Norton's Equivalent Circuits," *IEEE Trans. Educ.*, vol. 25, no. 3, pp. 99–102, Aug. 1982, <https://doi.org/10.1109/TE.1982.4321556>.
- [106] J. D. Enderle, "Thévenin's and Norton's Theorems," in *Bioinstrumentation*, in *Synthesis Lectures on Biomedical Engineering.*, Cham: Springer International Publishing, 2006, pp. 53–61. [https://doi.org/10.1007/978-3-031-01616-5\\_6](https://doi.org/10.1007/978-3-031-01616-5_6).
- [107] R. V. Jensen, "Classical Chaos," *Am. Sci.*, vol. 75, no. 2, pp. 168–181, 1987.
- [108] M. C. Gutzwiller, "Soft Chaos and the KAM Theorem," in *Chaos in Classical and Quantum Mechanics*, M. C. Gutzwiller, Ed., in *Interdisciplinary Applied Mathematics.*, New York, NY: Springer, 1990, pp. 116–141. [https://doi.org/10.1007/978-1-4612-0983-6\\_10](https://doi.org/10.1007/978-1-4612-0983-6_10).
- [109] G. F. R. Ellis, U. Kirchner, and W. R. Stoeger, "Multiverses and physical cosmology," *Mon. Not. R. Astron. Soc.*, vol. 347, no. 3, pp. 921–936, Jan. 2004, <https://doi.org/10.1111/j.1365-2966.2004.07261.x>.
- [110] J. Wisniak, "Conservation of Energy: Readings on the Origins of the First Law of Thermodynamics. Part I," *Educ. Quím.*, vol. 19, pp. 159–171, Jan. 2008, <https://doi.org/10.22201/fq.18708404e.2008.2.25806>

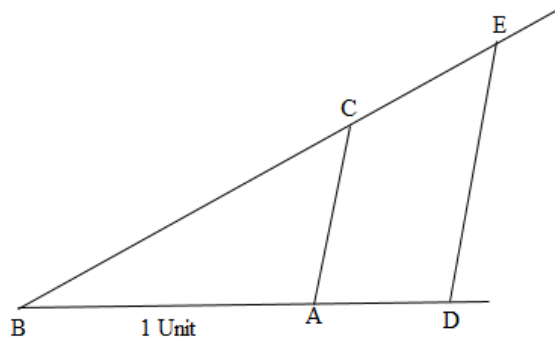


### Appendix I. (Rene' Descartes' multiplication with geometric construction method)

Descartes [36] presents a mechanical method for multiplying straight-line segments through geometric constructions. To simplify, we deviate slightly from Euclid's strict construction by introducing measurements and assuming a unity measure throughout. This scientific technique contrasts with and serves as a source of inspiration for the earlier developed straightedge and compass geometric operations.

**Definition 11 (Geometric multiplication of a straight line segment  $r_2$  and a given baseline  $r_1$ ).** Given a baseline  $r_1$  between two distinct basepoints points  $B$  and  $D$  and an arbitrary line segment  $r_2$  contained between two distinct points  $B$  and  $C$ , the geometric multiplication of  $r_1$  and  $r_2$  is obtained through the following construction starting from  $\{r_1, r_2\}$ .

1. Construct the point  $A$ , a unit between point  $B$  and point  $D$  on the side of the point  $D$ .
2. Construct line  $L_1$  through the points  $A$  and  $C$ .
3. Construct line  $L_2$  that is parallel to  $L_1$  through the point  $D$ .
4. Construct an extension of  $BC$  to intersect  $L_2$  at a point,  $E$ .



**Figure 11.** An Illustration of Descartes' Geometric Multiplication of Points in a Euclidean Plane. (This figure illustrates Descartes' geometric multiplication of points in a Euclidean Plane. The construction involves a baseline  $r_1$  between basepoints  $B$  and  $D$  and a line segment  $r_2$  between points  $B$  and  $C$ . Points  $A$ ,  $C$ ,  $D$ , and  $E$  are constructed accordingly, demonstrating the steps for geometric multiplication as per Definition 11).

**Claim 3.**  $\overline{BD} \otimes \overline{BC} = \overline{BE}$

**Proof.**  $L_2$  is parallel to  $L_1$ , implying  $\triangle ABC$  is similar to  $\triangle DBE$ . We set, as  $1$  is to  $L_1$  as  $r_1 = 1 + AD$  is to  $L_2$ .

If  $L_1 = (1 + AD) : L_2$ , then  $L_2 = (1 + AD) \times L_1$ .

Also, let  $BE = r_p$  so that  $r_p : L_2 = r_2 : L_1$ .

In this case;

$$r_p = \frac{r_2 \times L_2}{L_1} = \frac{r_2 \times (1 + AD) \times L_1}{L_1} = r_2 \times (1 + AD) = r_2 \times r_1$$

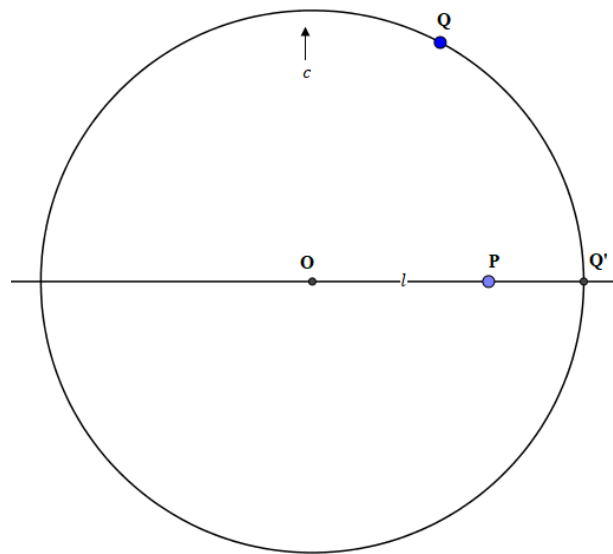
Thus,  $r_p = r_2 \times r_1$ , hence claim 3} is proven.

## Appendix 2. Point Rotation by Straightedge-Compass Construction

**Definition 12 (Rotation of a point to a baseline through  $O$  and  $P$ ):** Given two distinct basepoints points  $O$  and  $P$  and an arbitrary point  $Q$ , the rotation of  $Q$  to the baseline through point  $O$  and point  $P$  can be defined by a construction starting from  $\{O, P, Q\}$  as follows.

1. Construct the baseline  $l$  through the points  $O$  and  $P$ .
2. Construct a circle  $c$  centered at the point  $P$  through point  $Q$ .
3. Label  $Q'$  the intersection point between  $c$  and  $l$ .

The point  $Q'$  is a geometric rotation of the point  $Q$  to the baseline. By Definition, the magnitude  $\overline{OQ} \cong \overline{OQ'}$ .



**Figure 12.** Geometric Rotation of a point in a Euclidean Plane.

**Appendix 3 Important Notations.** The following shorthand convention is employed throughout the paper workflow.

$PMM$	: Perpetual Motion Machines
$LEC$	: Law of Energy conservation
$ETIS$	: Euclidean – Thermodynamic Isolated System
$TIS$	: Thermodynamics Isolated System
$N^{nth}$	: A Newton's Law and $n = 1, 2, \text{ and } 3$
$\Delta ABC$	: Triangle $ABC$
$\overline{L_1} \parallel \overline{L_2}$	: Two parallel lines $L_1$ and $L_2$
$\overline{OA}$	: Straight – line through points $O$ and $A$
$A > B$	: Magnitude $A$ is greater than magnitude $B$

